

GUGGENHEIM AERONAUTICAL LABORATORY

CALIFORNIA INSTITUTE OF TECHNOLOGY

STRESS DISTRIBUTION IN TWO
INTERSECTING CYLINDERS UNDER PRESSURE

Thesis by

Lt. Cmdr. Vernon E. Teig, USN

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1949

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SUMMARY

The experimental studies presented here were undertaken in an effort to determine the stress distribution in two circular cylinders intersecting at right angles and under internal pressure. The investigation was limited to tests of two specimens in the thick-walled cylinder range.

The experimental analysis led to the following conclusions:

1. The highest stress concentrations are located at an angle of about 14.5 degrees from the crotch centerline, measured in the plane of the intersection.
2. The critical stress causing rupture is the tangential stress in the plane of the ellipse.
3. For the R/t ratios tested, the strength reduction as compared with a straight closed cylinder is approximately 50%.
4. It appears probable that bending effects for these thick-wall d cylinders are of relatively minor importance.

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EXPLANATION OF SYMBOLS

| | |
|----------------|--|
| E | Young's Modulus of Elasticity (assumed = 30×10^6 psi) |
| R | Strain gage reading |
| b | Strain gage constant (-200) |
| p | Internal pressure - lbs./sq.in. |
| ϵ_a | Axial strain - in./in. |
| ϵ_r | Radial strain - in./in. |
| ϵ_t | Tangential strain - in./in. |
| ϵ_1 | Principal strain - in./in. |
| σ_a | Axial stress - lbs./sq.in. |
| σ_r | Radial stress - lbs./sq.in. |
| σ_t | Tangential stress - lbs./sq.in. |
| $\sigma_{1,2}$ | Principal stresses - lbs./sq.in. |
| μ | Poisson's ratio - (assumed = 0.3) |

INTRODUCTION

This investigation was prompted by certain problems which have arisen in systems employing high pressure piping. The construction of ducting for high speed wind tunnels involves cylindrical intersections of large diameter and similar problems, though on a smaller scale, may be found in various industrial applications. For piping which is highly stressed tangentially it has been the practice to furnish heavy ribs or other devices to take the bending stresses of the elliptical intersection. This procedure ignores bending stiffness of the pipe itself and some doubt has arisen as to the actual necessity for such ribs. Further, in some cases there was evidence that the reinforcing might in reality be harmful to the strength of the joint.

The tests presented here are steps toward a complete investigation of the problem. Some tests of this nature were made preliminary to the design and construction of the 20-inch supersonic wind tunnel of the Jet Propulsion Laboratory (CIT) (Ref. 1). The specimens tested in that project were of various shapes, materials, and Radius/thickness ratios. For the present approach to the problem it was decided to reduce the number of variable parameters to just one--the wall thickness. The steel to be used, the internal diameter, and other specifications were held constant. For this series it was originally planned to make tests on 90-degree elbows of at least four wall thicknesses, but difficulties in the manufacture of suitable specimens and time limitations forced a reduction in scope to only two specimens.

A search was made both in applicable textbooks and in the many engineering publications for previous work, either theoretical or experimental, on this subject. Considerable information was found on pipe bends, pipe elbows, and the like, but nothing on stresses to be found at or near a welded cylindrical intersection. This problem is of a type possessing mixed boundary conditions and as such is very difficult to solve from a purely theoretical approach.

The tests whose results are presented herein were conducted in the Structures Laboratory of the Guggenheim Graduate School of Aeronautics, California Institute of Technology.

EQUIPMENT AND PROCEDURE

The test specimens were made of eight-inch National Extra Strong welded steel pipe, ASTM Spec. 53-47. This steel has a yield point of 30,000 psi. and ultimate strength of 48,000 psi. The pipe was first machined inside and out to remove any eccentricity and to obtain a uniform wall thickness. Inside diameter was held constant for both specimens and was 7.68 inches. The wall thickness of the first specimen was 0.4 inch and the second was 0.3 inch.

After machining, the pipe was cut and welded so as to form a 90-degree elbow as shown in Fig. 6. Care was taken in machining off excess weld metal in the joint in order to have smooth fillets of small radius so that the finished product would approximate as closely as possible a cylindrical intersection machined from a single billet. Standard eight-inch pipe caps were welded on the ends and threaded studs welded in these caps. The studs were drilled and tapped to provide pressure connections and were threaded to receive lugs intended for use in applying either tension or compression across the ends by means of a turnbuckle. The turnbuckle was not used, however. Complete details of manufacture and assembly are shown in Figs. 5 and 6.

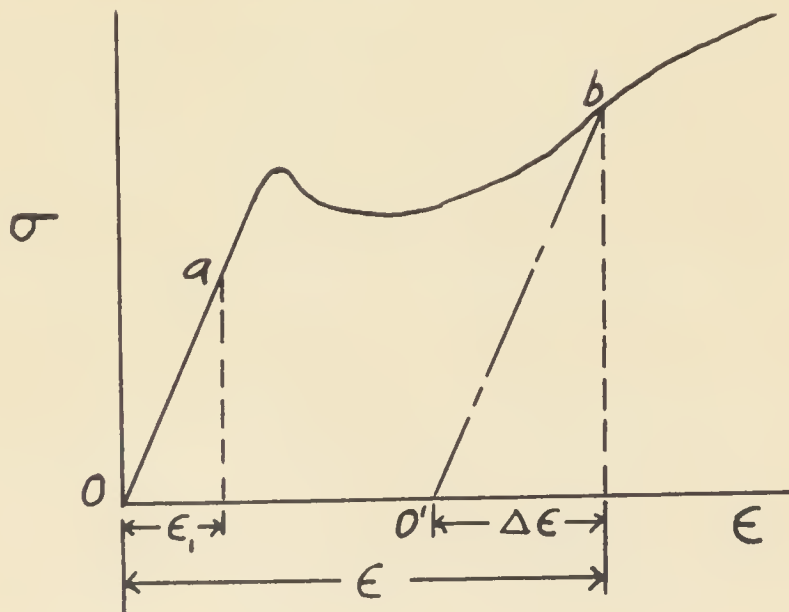
Pressure was applied by means of a Blackhawk hand-operated hydraulic pump. Pressure was measured by a standard high pressure gage. The variable resistance wire strain gages used were Baldwin-Southwark A-8 rectangular gages and AR-7 rectangular rosettes. The location and orientation of these gages is shown in Figs. 7, 8, and 9. Other equipment included a potentiometer and Wheatstone Bridge circuit, a switch

panel, 6-volt battery, and the necessary wiring and plumbing. The specimen was placed on wooden block supports spaced approximately 6 and 16 inches from each end.

The same procedure was followed in both tests. Within the elastic limit the following procedure was observed:

- (1) Zero readings were taken on all gages.
- (2) Load was applied and load readings taken.
- (3) Load was removed and a second zero reading taken.
- (4) Increased load was applied, readings taken, followed again by zero readings, etc.

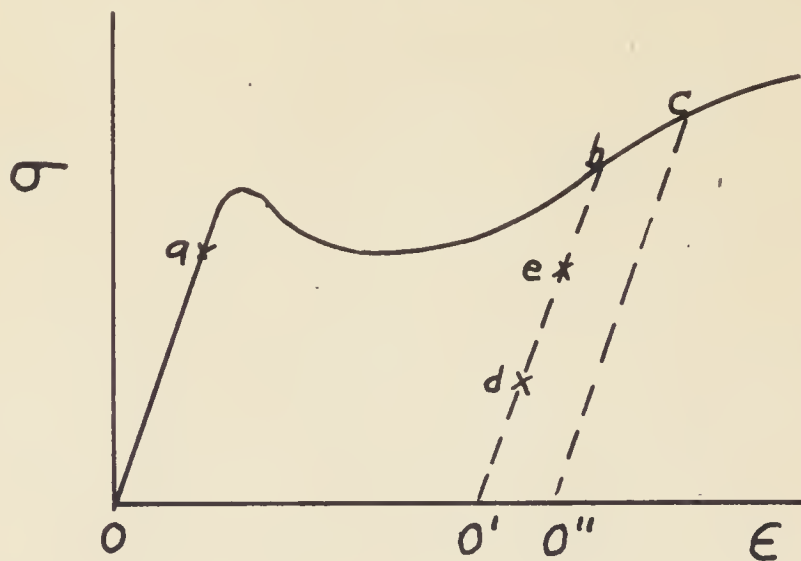
After the elastic limit had been exceeded, zero readings were taken only after the load readings. The reason for this can be seen by considering the curve below.



Assume that under the applied load, the metal at some given position reaches point "a" on the stress-strain diagram. This is below the elastic limit and when the load is removed both the stress and the

strain (ϵ) return to zero. Now if a sufficiently high load to cause yielding is applied, some point "b" on the curve will be reached. When the load is now removed, the line bo' will be followed ending at zero stress but with a permanent set $o-o'$. This permanent set can be computed by comparing strain gage readings at o and at o' . The strain at point "b" cannot now be referred directly to the zero strain at o but must be referred to the new "zero" at o' . Doing this gives the value of $\Delta\epsilon$ and adding this strain increment to the permanent set $o-o'$ gives the total strain ϵ at point "b".

Theoretically the line bo' of the preceding diagram is parallel to oa . In order to check on the reliability of strain gage readings beyond the specimen elastic limit, this parallelism was utilized by taking readings at points d and e on the way up to point c .



the next higher load reading above b . Since stress was not measured directly, a stress versus strain curve could not be plotted. Points

d and e were plotted on the load versus strain curves where the same reasoning as above applies. Therefore it was assumed that if points o', d, e, and b on the load-strain curves plotted a straight line parallel to oa, the strain gages were giving useful readings.

Punch marks were made in the stud in each end cap and a trammel bar and points used to measure the distance between the punch marks both in the unloaded condition and for each loading applied.

At the higher loadings where considerable yielding occurred it was necessary to maintain pressure constant for some time until a condition of equilibrium was reached and readings held substantially constant.

RESULTS AND DISCUSSION

The results of the two series of tests have been plotted on curves of loading versus tangential strain and axial strain for the several strain gage locations. The axial and tangential components were plotted since these were the strain components actually measured and also to facilitate comparison with the curves applying to a straight tube and the curves derived from previous tests on specimens having larger R/t ratios than those used in the present investigation. The principal strains and the principal axis orientation were computed within the elastic limit and are included in the tables. The maximum pressure held by the first specimen (0.4" wall) was 3350. psi. The maximum pressure held by the second specimen was 2950. psi.

The results of the two tests as shown in Tables I - XVIII and Figs. 22 and 27 show that the axial strains at position #5 are only very slightly smaller than the tangential strains at position #9 for all loadings under the elastic limit. Above the elastic limit, however, the tangential strains in the crotch increase much more rapidly than do those at any other point measured. For the locations investigated in these tests then, the critical strains occur in the crotch and are the tangential strains.

The type and location of ruptures obtained in the two tests were almost exactly identical as can be seen in Figs. 2, 4, and 50. In each case the failure was a crack perpendicular to the line of the weld at a distance of $1\frac{1}{2}$ " up from the crotch centerline. In both cases audible cracks and snaps were heard at irregular intervals as

the internal pressure was increased. In the first test these noises started at a pressure of about 2600 psi and were accompanied by the appearance of fine, hair-line cracks in the weld and perpendicular to the line of the weld as shown in Fig. 50. In the second test no such cracks appeared, but roughened stress lines approximately parallel to the weld appeared in the parent metal near the weld.

In specimen #2, cracks between the parent metal and the weld metal started widening perceptibly at loads below the elastic limit. As in specimen #1, however, when rupture finally occurred, the break was in the weld and at right angles to both the line of the weld and the initial cracks. Since the two breaks were so exactly similar, it seems quite possible that a point of stress concentration existed between positions #6 and #9. This possibility should be investigated in any further tests of this nature. Further evidence of this high stress area was given by the extremely high strains measured at position #6. The tangential gage in the crotch failed fairly early, but up to the time of failure indicated strains even higher than those at position #6.

Rosettes 1, 2, and 4 all were located some distance from the weld. (Fig. 7) The test results from both specimens as plotted in Figs. 10 and 12 show that the tangential strains did not become large until high loadings were applied. When these strains did begin to increase, the magnitudes of the strains and the rates of increase at these three locations remained quite close to each other. The axial strains show no such uniformity but all remained relatively small as

compared with the tangential strains. A comparison of strains at these three locations with the theoretical strains in a straight pipe follows: $p = 1,000$. psi.

$$\begin{array}{llll}
 \text{I: } \epsilon_{a_{th}} = .0608 \times 10^{-3} & \epsilon_{a_1} = .0865 \times 10^{-3} & \epsilon_{a_2} = .0318 \times 10^{-3} & \epsilon_{a_4} = .0764 \times 10^{-3} \\
 \epsilon_{\tau_{th}} = .2586 \times 10^{-3} & \epsilon_{\tau_1} = .1896 \times 10^{-3} & \epsilon_{\tau_2} = .2694 \times 10^{-3} & \epsilon_{\tau_4} = .3274 \times 10^{-4} \\
 \text{II: } \epsilon_{a_{th}} = .0822 \times 10^{-3} & \epsilon_{a_1} = .1392 \times 10^{-3} & \epsilon_{a_2} = .0299 \times 10^{-3} & \epsilon_{a_4} = .0946 \times 10^{-3} \\
 \epsilon_{\tau_{th}} = .3490 \times 10^{-3} & \epsilon_{\tau_1} = .3305 \times 10^{-3} & \epsilon_{\tau_2} = .3048 \times 10^{-3} & \epsilon_{\tau_4} = .4313 \times 10^{-3}
 \end{array}$$

Previous testing and experience had indicated an appreciable bending effect in this type of joint as evidenced by an opening of the original ninety-degree angle. For both specimens tested in this investigation no measurable amount of bending was found until the rupture point was reached. This would seem to indicate, at least for R/t ratios close to these, that the bending effects are much less important than had been believed and that for a properly welded joint there is sufficient inherent stiffness to eliminate the necessity for stiffening webs.

In making these tests it was desirable to get strain readings insofar as possible right up to the point of rupture. It was not known to what extent the strain gage readings would prove reliable once the yield point of the steel was passed. As a result of these tests it appears that the gage readings gave reliable qualitative results throughout the range of readings. Since the physical properties of the strain gages themselves are not known, it is impossible to state definitely at what total strain the gage accuracy underwent a change. Quantitatively, therefore, the

results are of an unknown degree of accuracy. It is probable that the close agreement of the curves for the two test specimens at each location would not have been obtained if the gages had become unreliable at the high loadings. In order to check the gage action at the higher loads, intermediate readings were taken between the unloaded condition and the high loads as previously explained in "PROCEDURE". These points as plotted in Figs. 16, 19, 22, 23, 25, 27, 28, and 31 give a straight line parallel to that obtained within the elastic region and the gages were therefore assumed to be giving useful readings. At some locations gages were broken under high loadings. This fact was immediately apparent due to the inability to obtain a balance in the bridge circuit.

From the strain readings taken, stresses at the various locations were computed within the elastic region and recorded in Tables I-XVIII. Since the strain gages can measure only two-dimensional strains, stresses were computed using two-dimensional theory. The third-dimensional strains while known to be present could not be accounted for in these tests. When yielding first occurred anywhere in the specimen, the resultant permanent deformation imposed residual stresses throughout the specimen when the load was removed. This was shown by an apparent permanent set indicated by all gages at approximately the same loading even though local load stresses had not risen sufficiently to reach the yield stress of the metal. This is the reason why all the load-strain curves deviate from a linear relation at about the same loading. Above the elastic limit the strains measured cannot be

transformed to other axes since the usual transformation equations are invalid outside the elastic range. Considerable work is now being done toward developing stress and strain relations for use in the plastic region (Ref. 2), but no attempt was made to apply any of those theories here.

The curves plotted from the results of the tests on the two specimens agree quite closely with three exceptions. The tangential strain curves at position #8 diverge, and the axial strain curves for positions 7 and 8 also diverge. The reason for this divergence is not known but may be due to the change in thickness ratio. Further tests on specimens of various R/t ratios would indicate whether the divergence is a trend established by the change in wall thickness.

For the wall thicknesses used in these tests it is believed that gravity effects were of very minor importance. In any further tests using thin-walled specimens of similar dimensions it would be better to provide supports which distribute the load uniformly along the length of the specimen rather than supporting it at four points as was done here.

Considering the fact that first yielding occurred at approximately 54% of maximum load in the first test and at about 42% of maximum load in the second test, use of the theory of limit design in actual construction is indicated. At the same time the large difference in yield loads observed compared with the theoretical yield load for a straight pipe should be considered.

Specimen I: $P_{\text{yield-str. pipe}} = 3288. \text{ psi.}$
 $P_{\text{yield-actual}} = 1800. \text{ psi.}$

Specimen II: $P_{\text{yield-str. pipe}} = 2435. \text{ psi.}$
 $P_{\text{yield-actual}} = 1200. \text{ psi.}$

This shows a reduction in strength of 45% for the first specimen, and 51% for the second.

A measurement of the intersection cross section shape was made after rupture in the tests described in Ref. 1. The original elliptical cross section was found to have been deformed into an egg shape with the greatest outward deviation located approximately midway between the crotch and the 90 degree point of the intersection. This contour is typical of deformations suffered by such intersections and was observed in the present tests.

Figs. 32 to 49 were plotted to show the measured strain distribution both along the cylinder axis and along the elliptical intersection. Examination of these figures (for instance Fig. 39 and Fig. 40) shows that axial strains are highest at position #5 and tangential strains are highest in the crotch. All strains are relatively low at the outside of the elbow for all loadings. There are relatively high

tangential and axial strains in the region between positions 6 and 9 so that the principal strains will be highest in that region.

CONCLUSIONS

1. The results of this investigation indicate that the highest stress concentration in a right angle cylindrical intersection under internal pressure occurs at an angle of about 14.5 degrees from the notch centerline measured in the plane of the ellipse.
2. The critical stress causing rupture is the tangential stress in the plane of the ellipse.
3. For the R/t ratios tested, the strength reduction as compared with a straight closed cylinder is approximately 50%.
4. It appears probable that bending effects for these thick walled cylinders are of relatively minor importance.

RECOMMENDATIONS

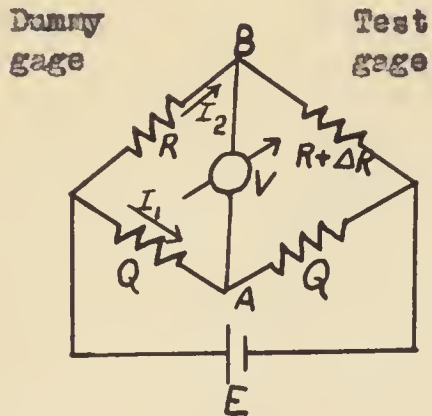
1. An analysis of the tangential stresses in the plane of the elliptical intersection should be made.
2. A study should be made of the variation of these tangential stresses through the wall thickness.
3. Analytical studies of bending effects and shearing stresses should be made.
4. In any further experimental work, the critical area as determined in this investigation should be thoroughly examined by strain gages or other means.
5. Further experimental work should check on the differing axial strains observed in the two specimens on the outside of the elbow.

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REDUCTION OF STRAIN GAGE DATA

The test gage mounted on the specimen and a dummy gage mounted on identical, unstrained material are included in a Wheatstone Bridge



circuit. The opposite sides of the circuit are two precision resistances of magnitude Q .

Under load the potentiometer is varied so that no current flows between points A and B. We wish to determine

the relation between the voltage V , across AB and the unit strain, ϵ , in the test specimen.

From the circuit diagram, we determine that

$$I_1(2Q) = E \quad I_2(2R + \Delta R) = E \quad V = I_1Q - I_2R$$

Hence

$$V = \frac{E}{2} - \frac{ER}{2R + \Delta R} = \frac{E}{4} \frac{\Delta R}{R} \left[1 + \frac{\Delta R}{2R} \right]^{-1} \approx \frac{E}{4} \frac{\Delta R}{R}$$

To eliminate the ratio $\Delta R/R$, the following relation for resistivity of a conductor is employed.

$$R = K \frac{L}{A}$$

where K is a resistivity constant, L the length of the conductor, and A its cross-sectional area. Then

$$\ln R = \ln K + \ln L - \ln A$$

Hence

$$\frac{\Delta R}{R} = \frac{\Delta L}{L} - \frac{\Delta A}{A}$$

For a cylindrical conductor

$$\frac{\Delta A}{A} = 2 \frac{\Delta r}{r} = -2\nu \frac{\Delta L}{L} = -2\nu \epsilon \quad \begin{array}{l} r \text{ is the radius} \\ \text{of the cross section} \end{array}$$

Therefore

$$\frac{\Delta R}{R} = (1 + 2\nu)\epsilon$$

ν is the Poisson's ratio for the strain gage material.

Substituting directly into the equation for the voltage reading V ,

$$\text{Hence} \quad v = \frac{E}{4} (1 + 2\nu)\epsilon$$

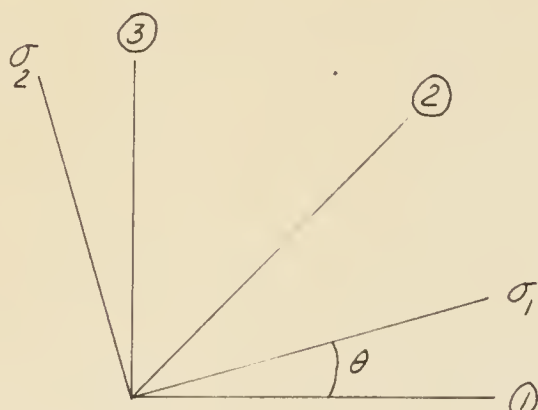
$$\epsilon = \frac{4v}{(1 + 2\nu)E}$$

This equation is usually employed in the form

$$\epsilon = \frac{4 \text{ (milli volts)}}{(\text{gage factor})(\text{battery reading})}$$

where ϵ is obtained in inches per inch times 10^{-3} .

Within the elastic region the average of zero readings taken before and after loading was used in getting the gage readings. Application of gage factor and battery reading gave apparent strains in the case of the rosettes, so these readings were further corrected as follows:



$$\Delta \epsilon_1 = R_1 - \frac{1}{b} R_3$$

$$\Delta \epsilon_2 = 1.02 R_2 - \frac{1}{b} (R_1 + R_3)$$

$$\Delta \epsilon_3 = R_3 - \frac{1}{b} R_1$$

$b = -200$ where b is a factor furnished by the manufacturer for each gage lot.

Having the strains at a given point, the axial and tangential stresses were computed from the usual two-dimensional equations:

$$\sigma_a = \frac{E}{1-\mu^2} [\epsilon_a + \mu \epsilon_t] \quad \sigma_t = \frac{E}{1-\mu^2} [\epsilon_t + \mu \epsilon_a]$$

These stresses could be computed only up to the load where yielding first occurred at any point in the specimen.

To compute principal stresses the following equations were used:

$$\sigma_{1,2} = \frac{E}{2(1-\mu)(1+b)} \left[(R_1 + R_3) \pm \frac{(1-\mu)(1+b)}{(1+\mu)(1-b)} \cdot r \right]$$

where $r = \left| \frac{R_1 + R_3 - 2R_2}{\sin 2\theta} \right|$

$$\tan 2\theta = - \frac{R_1 + R_3 - 2R_2}{R_1 - R_3}$$

Having the principal stresses, principal strains could then be computed.

$$\epsilon_1 = \frac{1}{E} (\sigma_1 - \mu \sigma_2)$$

Principal stresses and strains were computed only within the elastic region.

For test number one it was necessary to transform the measured strains at positions 5 and 7 to get the tangential strains due to the orientation of those two gages. (Fig. 8). This was done by using Mohr's circle. The transformation was performed only within the elastic region.

TABLE I

VARIATION OF TANGENTIAL AND AXIAL STRAINS WITH VARIATION OF INTERNAL PRESSURE

| Test I | Position #1 | | | | | | | | | | Gages 2,3 | |
|--------|----------------------------|-------|-------|-------|-------|--|----------|--------|-------|--------|-----------------------------------|--------|
| | $\leftarrow R \rightarrow$ | | | | | $\leftarrow \Delta \epsilon \rightarrow$ | | | | | $\leftarrow \epsilon \rightarrow$ | |
| Press. | Axial | Tang. | Diag. | Axial | Tang. | Princ. | θ | Princ. | Axial | Tang. | Axial | Tang. |
| 500 | .0430 | .1133 | - | .0436 | .1135 | - | - | - | .2560 | .4170 | .0436 | .1135 |
| 750 | .0645 | .1416 | - | .0652 | .1419 | - | - | - | .3550 | .5320 | .0652 | .1419 |
| 1000 | .0856 | .1892 | - | .0865 | .1896 | - | - | - | .4725 | .7100 | .0865 | .1896 |
| 1250 | .1068 | .2381 | - | .1080 | .2386 | - | - | - | .5910 | .8930 | .1080 | .2386 |
| 1500 | .1284 | .2890 | - | .1298 | .2896 | - | - | - | .7140 | 1.0830 | .1298 | .2896 |
| 1600 | .1325 | .3003 | - | .1340 | .3010 | - | - | - | .7400 | 1.1240 | .1340 | .3010 |
| 1700 | .1398 | .3160 | - | .1414 | .3167 | - | - | - | .7800 | 1.1840 | .1414 | .3167 |
| 1800 | .1468 | .3335 | - | .1485 | .3342 | - | - | - | - | - | .1460 | .7388 |
| 1900 | .1546 | .3552 | - | .1564 | .3560 | - | - | - | - | - | .1704 | .7403 |
| 2000 | .1627 | .3856 | - | .1646 | .3864 | - | - | - | - | - | .2075 | .7209 |
| 2050 | .1674 | .3899 | - | .1693 | .3907 | - | - | - | - | - | .2227 | .7092 |
| 2150 | .1809 | .4807 | - | .1833 | .4816 | - | - | - | - | - | .2449 | .7873 |
| 750 | .0616 | .1480 | - | .0623 | .1483 | - | - | - | - | - | .1239 | .4540 |
| 1700 | .1420 | .3337 | - | .1437 | .3344 | - | - | - | - | - | .2053 | .6401 |
| 2200 | .1850 | .4263 | - | .1871 | .4356 | - | - | - | - | - | .2581 | .7481 |
| 2300 | .1941 | .4474 | - | .1963 | .4484 | - | - | - | - | - | .2861 | .7438 |
| 2400 | .1993 | .4922 | - | .2018 | .4932 | - | - | - | - | - | .2938 | .8333 |
| 2500 | .2135 | .4801 | - | .2159 | .4812 | - | - | - | - | - | .2953 | .9880 |
| 2600 | .0804 | .3915 | - | .0824 | .3955 | - | - | - | - | - | .3602 | 2.2024 |
| 2800 | .2096 | .5993 | - | .2126 | .6003 | - | - | - | - | - | .9139 | 4.1237 |
| 3000 | .2146 | .6726 | - | .2161 | .6937 | - | - | - | - | - | 1.1340 | 5.5106 |
| 3250 | .2411 | .7970 | - | .2451 | .7982 | - | - | - | - | - | 1.3111 | 6.8218 |

Pressures and stresses in lb./sq.in. Strains given in inches per inch $\times 10^3$

TABLE II

Pages 4, 5, 6

Test I

Position #2

| Press. | $\longleftrightarrow R \longrightarrow$ | | Diag. | $\longleftrightarrow \Delta \epsilon \longrightarrow$ | | $\longleftrightarrow \sigma \longrightarrow$ | | $\longleftrightarrow \epsilon \longrightarrow$ | | |
|--------|---|-------|-------|---|-------|--|----------|--|-------|-------|
| | Axial | Tang. | | Axial | Tang. | Princ. | θ | Princ. | Axial | Tang. |
| 500 | .0181 | .1318 | .0696 | .0188 | .1319 | .1322 | 2-42 | 4540 | 1889 | 4530 |
| 750 | .0234 | .1908 | .1052 | .0244 | .1909 | .1909 | 0-39 | 6534 | 2690 | 6540 |
| 1000 | .0305 | .2693 | .1489 | .0318 | .2694 | .2690 | 0-15 | 9189 | 3707 | 9177 |
| 1250 | .0474 | .3300 | .1780 | .0480 | .3302 | .3306 | 2-10 | 11382 | 4855 | 11340 |
| 1500 | .0576 | .4050 | .2194 | .0596 | .4053 | .4058 | 1-58 | 13964 | 5973 | 13920 |
| 1600 | .0522 | .4300 | .2360 | .0543 | .4303 | .4302 | 0-47 | 14722 | 6045 | 14690 |
| 1700 | .0531 | .4600 | .2510 | .0554 | .4603 | .4601 | 0-47 | 15719 | 6380 | 15700 |
| 1800 | .0580 | .4807 | .2619 | .0604 | .4810 | - | - | - | - | - |
| 1900 | .0657 | .4976 | .2736 | .0682 | .4979 | - | - | - | - | - |
| 2000 | .0644 | .5211 | .2866 | .0670 | .5214 | - | - | - | - | - |
| 2050 | .0690 | .5319 | .2935 | .0717 | .5322 | - | - | - | - | - |
| 2150 | .0608 | .5297 | .2921 | .0634 | .5300 | - | - | - | - | - |
| 750 | .0197 | .2410 | .1035 | .0209 | .2411 | - | - | - | - | - |
| 1700 | .0528 | .4400 | .2409 | .0550 | .4403 | - | - | - | - | - |
| 2200 | .0693 | .5643 | .3106 | .0721 | .5646 | - | - | - | - | - |
| 2300 | .0718 | .4518 | .2357 | .0741 | .4522 | - | - | - | - | - |
| 2400 | .0754 | .5411 | .2932 | .0781 | .5415 | - | - | - | - | - |
| 2500 | .0878 | .5583 | .3058 | .0906 | .5587 | - | - | - | - | - |
| 2600 | .0955 | .6440 | .3646 | .0987 | .6445 | - | - | - | - | - |
| 2800 | .1176 | .6632 | .3796 | .1209 | .6688 | - | - | - | - | - |
| 3000 | .1336 | .8351 | .4486 | .1378 | .8358 | - | - | - | - | - |
| 3250 | .1358 | .9513 | .5011 | .1406 | .9520 | - | - | - | - | - |

TABLE III

Test I

Position #3

Pages 7,8,9

| Press. | $\leftarrow R \rightarrow$ | | Diag. | $\leftarrow \Delta \epsilon \rightarrow$ | | Princ. | θ | Princ. | $\leftarrow \sigma \rightarrow$ | | $\leftarrow \epsilon \rightarrow$ | |
|--------|----------------------------|--------|--------|--|--------|--------|----------|--------|---------------------------------|-------|-----------------------------------|---------|
| | Axial | Tang. | | Axial | Tang. | | | | Axial | Tang. | | |
| 500 | -0.0127 | 0.1562 | 0.0623 | -0.0119 | 0.1561 | .1566 | 86-59 | 5041 | 1151 | 5025 | -0.0119 | 0.1561 |
| 750 | -0.0167 | 0.2350 | 0.0910 | -0.0155 | 0.2349 | .2362 | 85-54 | 7621 | 1813 | 7595 | - .0155 | 0.2349 |
| 1000 | -0.0161 | 0.3273 | 0.1320 | - .0145 | 0.3272 | .3289 | 86-06 | 10684 | 2760 | 10650 | - .0145 | 0.3272 |
| 1250 | -0.0273 | 0.4080 | 0.1487 | - .0253 | 0.4079 | .4117 | 87-17 | 13286 | 3200 | 13200 | - .0253 | 0.4079 |
| 1500 | -0.0368 | 0.4970 | 0.1875 | -0.0343 | 0.4968 | .5002 | 85-28 | 16118 | 3775 | 16050 | - .0343 | 0.4968 |
| 1600 | - .0397 | 0.5420 | 0.2098 | -0.0370 | 0.5418 | .5446 | 85-57 | 17561 | 4135 | 17500 | - .0370 | 0.5418 |
| 1700 | - .0487 | 0.5810 | 0.2221 | -0.0458 | 0.5808 | .5836 | 86-01 | 18760 | 4235 | 18700 | - .0458 | 0.5808 |
| 1800 | - .0421 | 0.6126 | 0.2367 | - .0390 | .6124 | - | - | - | - | - | - .2812 | .8435 |
| 1900 | - .0007 | 0.5102 | .2010 | .0019 | .5102 | - | - | - | - | - | - .4396 | 1.2756 |
| 2000 | - .0641 | 0.7296 | .2511 | - .0605 | .7293 | - | - | - | - | - | - .7452 | 3.1196 |
| 2050 | - .0600 | 0.6597 | .2101 | - .0567 | .6594 | - | - | - | - | - | - .7604 | 3.2577 |
| 2150 | - .0648 | 0.7677 | .2941 | - .0610 | .7674 | - | - | - | - | - | -1.0346 | 5.3378 |
| 750 | - .0176 | 0.2486 | .1007 | - .0164 | .2484 | - | - | - | - | - | - .9900 | 4.8188 |
| 1700 | - .0552 | 0.6031 | .2356 | - .0522 | .6028 | - | - | - | - | - | -1.0258 | 5.1732 |
| 2200 | - .0888 | 0.8357 | .3172 | - .0846 | .8353 | - | - | - | - | - | -1.0363 | 5.3448 |
| 2300 | - .0333 | 0.9655 | .3673 | - .0285 | .9653 | - | - | - | - | - | -1.3724 | 8.2622 |
| 2400 | - .0485 | 0.9982 | .3958 | - .0435 | .9980 | - | - | - | - | - | -1.8190 | 10.7686 |
| 2500 | - .0661 | 1.0539 | .4339 | - .0608 | 1.0536 | - | - | - | - | - | -2.2653 | 12.7903 |
| 2600 | - .0889 | 1.1337 | .4893 | - .0832 | 1.1333 | - | - | - | - | - | -2.9376 | 15.1911 |
| 2800 | - .0841 | NG | .5448 | - | - | - | - | - | - | - | - | - |
| 3000 | - .1180 | NG | .6350 | - | - | - | - | - | - | - | - | - |
| 3250 | - .1311 | NG | NG | - | - | - | - | - | - | - | - | - |

TABLE IV

Test I

Position #4

Gages 10,11,12

| Press. | $\leftarrow R \rightarrow$ | | $\leftarrow \Delta \epsilon \rightarrow$ | | $\leftarrow \text{Princ. } \theta \rightarrow$ | | $\leftarrow \text{Princ. } \sigma \rightarrow$ | | $\leftarrow \epsilon \rightarrow$ | |
|--------|----------------------------|--------|--|-------|--|--------|--|--------|-----------------------------------|--------|
| | Axial | Tang. | Diag. | Axial | Tang. | Princ. | θ | Princ. | Axial | Tang. |
| 500 | .0369 | .1582 | .1411 | .0377 | .1584 | .1723 | -17-51 | 5916 | .0377 | .1584 |
| 750 | .0565 | .2183 | .2070 | .0576 | .2186 | .2443 | -20-22 | 8369 | .0576 | .2186 |
| 1000 | .0748 | .3270 | .2862 | .0764 | .3274 | .3533 | -17-03 | 12148 | .0764 | .3274 |
| 1250 | .0996 | .3977 | .3467 | .1016 | .3982 | .4274 | -16-40 | 14808 | .1016 | .3982 |
| 1500 | .1150 | .4890 | .4240 | .1174 | .4896 | .5257 | -16-34 | 18136 | .1174 | .4896 |
| 1600 | .1502 | .5220 | .4620 | .1528 | .5228 | .5611 | -17-04 | 19632 | .1528 | .5228 |
| 1700 | 0.1549 | 0.5520 | 0.4820 | .1577 | .5528 | .5905 | -16-28 | 20655 | .1577 | .5528 |
| 1800 | .1429 | .5841 | .5168 | .1458 | .5848 | - | - | - | .1562 | .5833 |
| 1900 | .1595 | .6040 | .5370 | .1625 | .6048 | - | - | - | .1532 | .6169 |
| 2000 | .1650 | .6164 | .5539 | .1681 | .6172 | - | - | - | .1345 | .7743 |
| 2050 | .1738 | .6133 | .5646 | .1769 | .6142 | - | - | - | .1422 | .8531 |
| 2150 | .1893 | .6289 | .5878 | .1924 | .6298 | - | - | - | .1570 | 1.3555 |
| 750 | .0650 | .2287 | .2057 | .0661 | .2290 | - | - | - | .0302 | 0.9547 |
| 1700 | .1481 | .5132 | .4655 | .1507 | .5139 | - | - | - | .1148 | 1.2396 |
| 2200 | .1944 | .6584 | .5990 | .1977 | .6554 | - | - | - | .1725 | 1.3850 |
| 2300 | .1821 | .5772 | .5305 | .1850 | .5781 | - | - | - | .4297 | 2.0265 |
| 2400 | .2165 | .6072 | .5714 | .2195 | .6083 | - | - | - | .7248 | 2.7650 |
| 2500 | .2469 | .6392 | .6210 | .2501 | .6322 | - | - | - | .9061 | 3.3265 |
| 2600 | .2667 | .7040 | .6368 | .2702 | .7053 | - | - | - | 1.0969 | 3.9296 |
| 2800 | .2931 | .7206 | .652 | .2967 | .7221 | - | - | - | 1.5359 | 5.2937 |
| 3000 | .3268 | .7730 | .6833 | .3307 | .7746 | - | - | - | 2.1318 | 6.9961 |
| 3250 | .3630 | .8555 | .6837 | .3673 | .8573 | - | - | - | 2.6431 | 8.6785 |

TABLE V

Test I

Position #5

Pages 13,14,15

| Press. | $\longleftrightarrow R \longrightarrow$ | | | $\longleftrightarrow \Delta \epsilon \longrightarrow$ | | | $\longleftrightarrow \sigma \longrightarrow$ | | | $\longleftrightarrow \epsilon \longrightarrow$ | | |
|--------|---|------------|----------------|---|--------|--------|--|--------|-------|--|---------|--------|
| | Axial | Along Weld | Normal to Weld | Axial | Tang. | Princ. | θ | Princ. | Axial | Tang. | Axial | Tang. |
| 500 | 0.2150 | 0.1288 | 0.2170 | 0.2210 | 0.1293 | .2344 | 66-45 | 8847 | 8474 | 6420 | 0.2210 | .1293 |
| 750 | 0.3265 | 0.1955 | 0.3286 | 0.3356 | 0.1970 | .3555 | 67-01 | 13415 | 12816 | 9758 | .3356 | .1970 |
| 1000 | 0.4380 | 0.2633 | 0.4440 | .4503 | 0.2655 | .4783 | 66-31 | 18070 | 17306 | 13158 | .4503 | .2655 |
| 1250 | 0.5324 | 0.3163 | 0.5420 | .5473 | .3190 | .5834 | 66-16 | 21996 | 21076 | 15892 | .5473 | .3190 |
| 1500 | 0.6515 | 0.3854 | 0.6590 | 0.6698 | .3887 | .7120 | 66-43 | 26814 | 25634 | 19350 | .6698 | .3887 |
| 1600 | 0.7020 | 0.415 | 0.7140 | 0.7216 | .4185 | .7694 | 66-19 | 28979 | 27748 | 20880 | .7216 | .4185 |
| 1700 | 0.7370 | 0.4330 | 0.7580 | 0.7576 | .4343 | .8128 | 65-32 | 30596 | 29381 | 21917 | .7576 | .4343 |
| 1800 | 0.7797 | 0.4558 | 0.7959 | .8016 | .4599 | - | - | - | - | - | .8933 | .4476 |
| 1900 | 0.8272 | 0.4849 | 0.8498 | .8504 | .4892 | - | - | - | - | - | 1.1027 | .4711 |
| 2000 | 0.8738 | 0.5068 | 0.8907 | .8983 | .5115 | - | - | - | - | - | 1.3280 | .4510 |
| 2050 | 0.8844 | 0.5203 | 0.9001 | .9092 | .5249 | - | - | - | - | - | 1.4455 | .4866 |
| 2150 | 0.9243 | 0.5438 | 0.9376 | .9502 | .5486 | - | - | - | - | - | 1.8839 | .6597 |
| 750 | 0.3123 | 0.1795 | 0.3096 | .3209 | .1811 | - | - | - | - | - | 1.2546 | .2922 |
| 1700 | 0.7164 | 0.4150 | 0.7269 | .7364 | .4187 | - | - | - | - | - | 1.6701 | .5298 |
| 2200 | 0.9250 | 0.5356 | 0.9381 | .9509 | .5404 | - | - | - | - | - | 1.9229 | .6762 |
| 2300 | 0.9648 | 0.5649 | 1.0095 | .9920 | .5700 | - | - | - | - | - | 2.9586 | 1.1058 |
| 2400 | 1.0026 | 0.5841 | 1.0292 | 1.0307 | .5615 | - | - | - | - | - | 3.6251 | 1.3387 |
| 2500 | 1.0108 | 0.5920 | 1.0229 | 1.0391 | .7058 | - | - | - | - | - | 4.2130 | 1.7047 |
| 2600 | 1.0683 | 0.6175 | 1.0510 | 1.0980 | .6229 | - | - | - | - | - | 5.0013 | 1.8820 |
| 2800 | 1.0585 | 0.6775 | 1.0585 | 1.0884 | .6829 | - | - | - | - | - | 6.8464 | 2.4601 |
| 3000 | 1.0871 | 0.7703 | 1.0629 | 1.1180 | .7770 | - | - | - | - | - | 8.9184 | 2.9686 |
| 3250 | 1.1626 | 0.9040 | 1.0636 | 1.1956 | .9095 | - | - | - | - | - | 10.7605 | 3.5506 |

TABLE VI

Test I

Position #6

Pages 16,17,18

| Press. | $\longleftrightarrow R \longrightarrow$ | | Diag. | $\longleftrightarrow \Delta \epsilon \longrightarrow$ | | $\longleftrightarrow \sigma \longrightarrow$ | | $\longleftrightarrow \epsilon \longrightarrow$ | | | | |
|--------|---|--------|--------|---|--------|--|----------|--|-------|-------|--------|---------|
| | Axial | Tang. | | Axial | Tang. | Princ. | θ | Princ. | Axial | Tang. | | |
| 500 | -.0101 | .2050 | .0429 | -.0091 | .2045 | .2180 | 13-28 | 6970 | 1725 | 6650 | -.0091 | .2045 |
| 750 | -.0127 | .3055 | .0408 | -.0112 | .3054 | .3371 | 16-47 | 10691 | 2650 | 9950 | -.0112 | .3054 |
| 1000 | -.0141 | 0.4170 | 0.0554 | -.0120 | .4169 | .4615 | 17-04 | 14655 | 3730 | 13640 | -.0120 | .4169 |
| 1250 | -.0126 | 0.5090 | 0.0717 | -.0101 | .5089 | .5627 | 17-03 | 17920 | 4700 | 16690 | -.0101 | .5089 |
| 1500 | -.0126 | .6235 | .0873 | -.0095 | .6234 | .6907 | 17-14 | 22012 | 5850 | 20470 | -.0095 | .6234 |
| 1600 | -.0093 | 0.6720 | 0.0959 | -.0059 | .6720 | .7450 | 17-20 | 23780 | 6450 | 22100 | -.0059 | .6720 |
| 1700 | -.0162 | 0.7100 | 0.0987 | -.0126 | .7099 | .7862 | 17-11 | 25042 | 6610 | 23270 | -.0126 | .7099 |
| 1800 | -.0126 | 0.7495 | 0.1074 | -.0089 | .7494 | - | - | - | - | - | .0332 | .6988 |
| 1900 | -.0073 | 0.8001 | 0.1144 | -.0033 | .8001 | - | - | - | - | - | .0883 | .8339 |
| 2000 | .0056 | 0.8535 | 0.1308 | .0099 | .8535 | - | - | - | - | - | .2527 | 1.0209 |
| 2050 | .0053 | 0.8551 | 0.1434 | .0096 | .8551 | - | - | - | - | - | .2884 | .8756 |
| 2150 | .0260 | 0.9246 | 0.1562 | .0306 | .9247 | - | - | - | - | - | .6063 | 1.8557 |
| 750 | .0063 | .2957 | .0547 | .0078 | .2957 | - | - | - | - | - | .5835 | 1.2267 |
| 1700 | .0253 | .8017 | .1281 | .0293 | .8018 | - | - | - | - | - | .6050 | 1.7328 |
| 2200 | .0395 | .9467 | .1609 | .0442 | .9469 | - | - | - | - | - | .5930 | 1.9099 |
| 2300 | .0632 | 1.0085 | .1958 | .0682 | 1.0088 | - | - | - | - | - | 1.3146 | 3.8451 |
| 2400 | .1191 | 1.1052 | .2224 | .1246 | 1.1058 | - | - | - | - | - | 1.8874 | 5.2142 |
| 2500 | .1674 | 1.1740 | .2418 | .1733 | 1.1748 | - | - | - | - | - | 2.2353 | 6.2563 |
| 2600 | .2271 | 1.2371 | .2678 | .2333 | 1.2382 | - | - | - | - | - | 2.5718 | 7.4738 |
| 2800 | .3148 | 1.3137 | .3051 | .3214 | 1.3153 | - | - | - | - | - | 2.9714 | 9.8491 |
| 3000 | .3834 | 1.3148 | .3416 | .3900 | 1.3167 | - | - | - | - | - | 2.7935 | 12.0549 |
| 3250 | .3106 | NG | .3779 | .3106 | - | - | - | - | - | - | - | - |

TABLE VII

| Test I | $\leftarrow R \rightarrow$ | | $\leftarrow \Delta \epsilon \rightarrow$ | | $\leftarrow \sigma \rightarrow$ | | $\leftarrow \epsilon \rightarrow$ | | Gages 19, 20, 21 |
|--------|----------------------------|----------------|--|--------|---------------------------------|----------|-----------------------------------|-------|------------------|
| | Axial | Along Weld | Axial | Tang. | Princ. | θ | Princ. | Tang. | |
| Press. | | Normal to Weld | | | | | | | |
| 500 | .0700 | -.0385 | .0716 | -.0381 | .1015 | -63-06 | 2823 | 2479 | .0716 |
| 750 | .1045 | -.0615 | .1069 | -.0608 | .1451 | -63-55 | 4090 | 3518 | .1069 |
| 1000 | .1340 | -.0818 | .1372 | -.0809 | .2019 | -62-06 | 5594 | 4983 | .1372 |
| 1250 | .1732 | -.1040 | .1772 | -.1029 | .2488 | -64-00 | 6779 | 5827 | .1772 |
| 1500 | .2276 | -.1344 | .2328 | -.1386 | .3206 | -64-42 | 8681 | 7469 | .2328 |
| 1600 | .2382 | -.1400 | .2437 | -.1442 | .3368 | -64-30 | 9144 | 7901 | .2437 |
| 1700 | .2477 | -.1452 | .2534 | -.1438 | .3508 | -64-30 | 9534 | 8113 | .2534 |
| 1800 | .2549 | -.1508 | .2608 | -.1492 | - | - | - | - | .3051 |
| 1900 | .2690 | -.1542 | .2753 | -.1525 | - | - | - | - | .3469 |
| 2000 | .2753 | -.1650 | .2817 | -.1633 | - | - | - | - | .4062 |
| 2050 | .2941 | -.1581 | .3010 | -.1500 | - | - | - | - | .4235 |
| 2150 | .3064 | -.1632 | .3135 | -.1614 | - | - | - | - | .4603 |
| 750 | .1011 | -.0599 | .1034 | -.0623 | - | - | - | - | .2502 |
| 1700 | .2411 | -.0599 | .2471 | -.0584 | - | - | - | - | .3939 |
| 2200 | .3175 | -.1641 | .3249 | -.1622 | - | - | - | - | .4706 |
| 2300 | .3123 | -.1560 | .3197 | -.1520 | - | - | - | - | .4601 |
| 2400 | .3228 | -.1614 | .3304 | -.1595 | - | - | - | - | .4598 |
| 2500 | .3268 | -.1598 | .3346 | -.1578 | - | - | - | - | .4973 |
| 2600 | .3380 | -.1544 | .3462 | -.1523 | - | - | - | - | .5333 |
| 2800 | .3486 | -.1458 | .3572 | -.1435 | - | - | - | - | .6613 |
| 3000 | .3630 | -.1373 | .3722 | -.1344 | - | - | - | - | .7355 |
| 3250 | .4287 | -.1021 | .4397 | -.0991 | - | - | - | - | .8197 |

TABLE VIII

Gages 22&23

Test I

Position #8

| Press. | $\leftarrow R \rightarrow$ | | | $\leftarrow \Delta \epsilon \rightarrow$ | | | θ | $\leftarrow \sigma \rightarrow$ | | | $\leftarrow \epsilon \rightarrow$ | | |
|--------|----------------------------|--------|-------|--|--------|--------|----------|---------------------------------|-------|-------|-----------------------------------|--------|---------|
| | Axial | Tang. | Diag. | Axial | Tang. | Princ. | | Princ. | Axial | Tang. | Axial | Tang. | |
| 500 | .0058 | -.0613 | - | .0058 | -.0613 | .0058 | 0 | .0058 | -415 | -415 | -1965 | .0058 | -.0613 |
| 750 | .0054 | -.0875 | - | .0054 | -.0875 | .0054 | 0 | .0054 | -686 | -686 | -2832 | .0054 | -.0875 |
| 1000 | .0018 | -.1263 | - | .0018 | -.1263 | .0018 | 0 | .0018 | -1190 | -1190 | -4148 | .0018 | -.1263 |
| 1250 | .0118 | -.1675 | - | .0118 | -.1675 | .0118 | 0 | .0118 | -1266 | -1266 | -5407 | .0118 | -.1675 |
| 1500 | .0218 | -.1956 | - | .0218 | -.1956 | .0218 | 0 | .0218 | -1216 | -1216 | -6235 | .0218 | -.1956 |
| 1600 | .0352 | -.2100 | - | .0352 | -.2100 | .0352 | 0 | .0352 | -916 | -916 | -6574 | .0352 | -.2100 |
| 1700 | .0419 | -.2280 | - | .0419 | -.2280 | .0419 | 0 | .0419 | -874 | -874 | -7102 | .0419 | -.2280 |
| 1800 | .0417 | -.2425 | - | .0417 | -.2425 | - | - | - | - | - | - | .1019 | -.2680 |
| 1900 | .0474 | -.2563 | - | .0474 | -.2563 | - | - | - | - | - | - | .1469 | -.2941 |
| 2000 | .0597 | -.2696 | - | .0597 | -.2696 | - | - | - | - | - | - | .2184 | -.3303 |
| 2050 | .0640 | -.2696 | - | .0640 | -.2696 | - | - | - | - | - | - | .2329 | -.3382 |
| 2150 | .0720 | -.2891 | - | .0720 | -.2891 | - | - | - | - | - | - | .3098 | -.3850 |
| 750 | -.0003 | -.0825 | - | -.0003 | -.0825 | - | - | - | - | - | - | .2375 | -.1784 |
| 1700 | .0283 | -.2000 | - | .0283 | -.2000 | - | - | - | - | - | - | .2661 | -.2959 |
| 2200 | .0646 | -.2606 | - | .0646 | -.2606 | - | - | - | - | - | - | .3148 | -.3556 |
| 2300 | .0789 | -.2942 | - | .0789 | -.2942 | - | - | - | - | - | - | .4184 | -.4651 |
| 2400 | .0903 | -.3029 | - | .0903 | -.3029 | - | - | - | - | - | - | .5437 | -.6020 |
| 2500 | .1060 | -.3259 | - | .1060 | -.3259 | - | - | - | - | - | - | .7146 | -.8523 |
| 2600 | .1161 | -.3248 | - | .1161 | -.3248 | - | - | - | - | - | - | .7247 | -.8512 |
| 2800 | .1401 | -.3318 | - | .1401 | -.3318 | - | - | - | - | - | - | .9385 | -1.2150 |
| 3000 | .1855 | -.3549 | - | .1855 | -.3549 | - | - | - | - | - | - | 1.1440 | -1.7719 |
| 3250 | .2273 | -.3218 | - | .2273 | -.3218 | - | - | - | - | - | - | 1.2880 | -2.0626 |

TABLE NO. X

VARIATION OF TANGENTIAL AND AXIAL STRAINS WITH VARIATION OF INTERNAL PRESSURE

| Test II | Position #1 | | | | | | | | | | Gages 2,3 | |
|---------|----------------------------|--------|--|-------|---------------------------------|--------|---------------------------------|--------|-----------------------------------|-------|-----------|---------|
| | $\leftarrow R \rightarrow$ | | $\leftarrow \Delta \epsilon \rightarrow$ | | $\leftarrow \theta \rightarrow$ | | $\leftarrow \sigma \rightarrow$ | | $\leftarrow \epsilon \rightarrow$ | | | |
| Press. | Axial | Tang. | Diag. | Axial | Tang. | Princ. | θ | Princ. | Axial | Tang. | Axial | Tang. |
| 400 | .0600 | .1385 | - | .0670 | .1388 | - | - | - | .3580 | 5239 | .0670 | .1388 |
| 600 | .0815 | .1970 | - | .0825 | .1974 | - | - | - | .4672 | 7326 | .0825 | .1974 |
| 800 | .1142 | .2680 | - | .1155 | .2686 | - | - | - | .6465 | 9996 | .1155 | .2686 |
| 1000 | .1376 | .3298 | - | .1392 | .3305 | - | - | - | .7860 | 12275 | .1392 | .3305 |
| 1100 | .1535 | .3677 | - | .1553 | .3685 | - | - | - | .8767 | 13686 | .1553 | .3685 |
| 1200 | .1657 | .4020 | - | .1677 | .4028 | - | - | - | - | - | .1795 | .3831 |
| 1250 | .1724 | .4182 | - | .1745 | .4191 | - | - | - | - | - | .1905 | .3906 |
| 1300 | .1848 | .4316 | - | .1870 | .4325 | - | - | - | - | - | .2070 | .3978 |
| 500 | .0705 | .1632 | - | .0713 | .1636 | - | - | - | - | - | .0913 | .1289 |
| 900 | .1254 | .3019 | - | .1269 | .3025 | - | - | - | - | - | .1469 | .2678 |
| 1400 | .1940 | .4794 | - | .1964 | .4804 | - | - | - | - | - | .2531 | .3806 |
| 1600 | .2226 | .5814 | - | .2255 | .5825 | - | - | - | - | - | .3474 | .3389 |
| 600 | .0869 | .2171 | - | .0880 | .2175 | - | - | - | - | - | .2099 | -.0261 |
| 1200 | .1718 | .4421 | - | .1740 | .4430 | - | - | - | - | - | .2959 | .1994 |
| 1800 | .1989 | .6038 | - | .2019 | .6048 | - | - | - | - | - | .6174 | 1.7911 |
| 2000 | .2622 | .8185 | - | .2663 | .8198 | - | - | - | - | - | 1.1349 | 4.1168 |
| 2200 | .2623 | .9078 | - | .2668 | .9091 | - | - | - | - | - | 1.4475 | 6.6002 |
| 2400 | .2727 | 1.0532 | - | .2780 | 1.0546 | - | - | - | - | - | 1.7004 | 9.4359 |
| 2600 | .2848 | 1.1135 | - | .2904 | 1.1149 | - | - | - | - | - | 1.8471 | 12.5249 |
| 2800 | .2852 | NQ | - | - | - | - | - | - | - | - | - | - |

Pressures and stresses in lb./sq.in. Strains given in inches per inch x 10³

TABLE XI

| Test II | Position #2 | | | | | | | | | | Pages 4,5,6 | |
|---------|----------------------------|-------|--|-------|--|--------|--|--------|-----------------------------------|-------|-------------|-------|
| | $\leftarrow R \rightarrow$ | | $\leftarrow \Delta \epsilon \rightarrow$ | | $\leftarrow \text{Princ. } \theta \rightarrow$ | | $\leftarrow \text{Princ. } \sigma \rightarrow$ | | $\leftarrow \epsilon \rightarrow$ | | | |
| Press. | Axial | Tang. | Diag. | Axial | Tang. | Princ. | θ | Princ. | Axial | Tang. | Axial | Tang. |
| 400 | .0112 | .1296 | .0739 | .0118 | .1297 | .1296 | -1-28 | 4401 | .0118 | .1297 | .0118 | .1297 |
| 600 | .0172 | .1824 | .1164 | .0181 | .1825 | .1841 | -5-41 | 6234 | .0181 | .1825 | .0181 | .1825 |
| 800 | .0228 | .2475 | .1564 | .0240 | .2476 | .2497 | -5-21 | 8450 | .0240 | .2476 | .0240 | .2476 |
| 1000 | .0284 | .3047 | .1918 | .0299 | .3048 | .3070 | -5-11 | 10397 | .0299 | .3048 | .0299 | .3048 |
| 1100 | .0307 | .3374 | .2152 | .0324 | .3376 | .3408 | -5-45 | 11524 | .0324 | .3376 | .0324 | .3376 |
| 1200 | .0358 | .3708 | .2357 | .0377 | .3710 | - | - | - | .0377 | .3710 | .0377 | .3710 |
| 1250 | .0375 | .3804 | .2408 | .0394 | .3806 | - | - | - | .0394 | .3806 | .0394 | .3806 |
| 1300 | .0375 | .3944 | .2456 | .0395 | .3946 | - | - | - | .0395 | .3946 | .0395 | .3946 |
| 500 | .0140 | .1506 | .0941 | .0148 | .1507 | - | - | - | .0148 | .1507 | .0148 | .1507 |
| 900 | .0253 | .2773 | .1742 | .0267 | .2774 | - | - | - | .0267 | .2774 | .0267 | .2774 |
| 1400 | .0392 | .4182 | .2618 | .0413 | .4184 | - | - | - | .0413 | .4184 | .0413 | .4184 |
| 1600 | .0443 | .4806 | .3925 | .0467 | .4808 | - | - | - | .0467 | .4808 | .0467 | .4808 |
| 600 | .0166 | .1751 | .1109 | .0175 | .1752 | - | - | - | .0175 | .1752 | .0175 | .1752 |
| 1200 | .0296 | .3525 | .2184 | .0314 | .3526 | - | - | - | .0314 | .3526 | .0314 | .3526 |
| 1800 | .0653 | .5121 | .3289 | .0679 | .5124 | - | - | - | .0679 | .5124 | .0679 | .5124 |
| 2000 | .0794 | .6330 | .4089 | .0826 | .6334 | - | - | - | .0826 | .6334 | .0826 | .6334 |
| 2200 | .1129 | .7303 | .4958 | .1166 | .7309 | - | - | - | .1166 | .7309 | .1166 | .7309 |
| 2400 | .1365 | .8720 | .5836 | .1409 | .8727 | - | - | - | .1409 | .8727 | .1409 | .8727 |
| 2600 | .1419 | .9022 | .6138 | .1464 | .9029 | - | - | - | .1464 | .9029 | .1464 | .9029 |
| 2800 | .1772 | .9618 | .6995 | .1820 | .9627 | - | - | - | .1820 | .9627 | .1820 | .9627 |

TABLE XII

Test II

Position #3

Gages 7,8,9

| Press. | $\leftarrow R \rightarrow$ | | $\leftarrow \Delta \epsilon \rightarrow$ | | $\leftarrow \theta \rightarrow$ | | $\leftarrow \sigma \rightarrow$ | | $\leftarrow \epsilon \rightarrow$ | |
|--------|----------------------------|-------|--|--------|---------------------------------|--------|---------------------------------|--------|-----------------------------------|-------|
| | Axial | Tang. | Diag. | Axial | Tang. | Princ. | θ | Princ. | Axial | Tang. |
| 400 | -.0145 | .1962 | .0762 | -.0135 | .1961 | .1972 | +86-02 | 6356 | 1491 | 6334 |
| 600 | -.0211 | .2798 | .1095 | -.0197 | .2797 | .2811 | +86-14 | 9058 | 2117 | 9027 |
| 800 | -.0284 | .3848 | .1515 | -.0265 | .3847 | .3863 | +86-19 | 12459 | 2931 | 12420 |
| 1000 | -.0386 | .4796 | .1862 | -.0362 | .4794 | .4819 | +86-13 | 15504 | 3548 | 15446 |
| 1100 | -.0446 | .5384 | .2080 | -.0419 | .5382 | .5410 | +86-12 | 17394 | 3943 | 17329 |
| 1200 | -.0475 | .6036 | .2287 | -.0445 | .6034 | - | - | - | - | - |
| 1250 | -.0545 | .6186 | .2355 | -.0514 | .6183 | - | - | - | - | - |
| 1300 | -.0588 | .6543 | .2466 | -.0555 | .6540 | - | - | - | - | - |
| 500 | -.0186 | .2354 | .0948 | -.0174 | .2353 | - | - | - | - | - |
| 900 | -.0386 | .4492 | .1706 | -.0364 | .4490 | - | - | - | - | - |
| 1400 | -.0652 | .7153 | .2831 | -.0616 | .7150 | - | - | - | - | - |
| 1600 | -.1002 | .9984 | .3850 | -.0952 | .9979 | - | - | - | - | - |
| 600 | -.0303 | .3196 | .1352 | -.0287 | .3194 | - | - | - | - | - |
| 1200 | -.0583 | .6458 | .2583 | -.0551 | .6455 | - | - | - | - | - |
| 1800 | -.1563 | NG | .4931 | - | - | - | - | - | - | - |
| 2000 | -.1540 | NG | .3516 | - | - | - | - | - | - | - |
| 2200 | -.1809 | NG | .7002 | - | - | - | - | - | - | - |
| 2400 | -.2214 | NG | .8117 | - | - | - | - | - | - | - |
| 2600 | -.1979 | NG | NG | - | - | - | - | - | - | - |
| 2800 | -.0874 | NG | NG | - | - | - | - | - | - | - |

TABLE XIII

Test II

Position #4

Pages 10,11,12

| Press. | $\leftarrow R \rightarrow$ | | $\leftarrow \Delta \epsilon \rightarrow$ | | $\leftarrow \theta \rightarrow$ | | $\leftarrow \sigma \rightarrow$ | | $\leftarrow \epsilon \rightarrow$ | |
|--------|----------------------------|--------|--|--------|---------------------------------|--------|---------------------------------|-------|-----------------------------------|---------|
| | Axial | Tang. | Axial | Tang. | Princ. | Princ. | Axial | Tang. | Axial | Tang. |
| 400 | .0366 | .1817 | .0375 | .1819 | .2038 | -19-57 | 6873 | 3036 | .0375 | .1819 |
| 600 | .0567 | .2586 | .0580 | .2589 | .2907 | -20-18 | 9844 | 4474 | .0580 | .2589 |
| 800 | .0729 | .3511 | .0747 | .3515 | .3925 | -19-46 | 13273 | 5938 | .0747 | .3515 |
| 1000 | .0924 | .4308 | .0946 | .4313 | .4860 | -20-30 | 16418 | 7385 | .0946 | .4313 |
| 1100 | .1023 | .4780 | .1047 | .4785 | .5354 | -19-58 | 18124 | 8186 | .1047 | .4785 |
| 1200 | .1162 | .5226 | .1188 | .5232 | - | - | - | - | .1022 | .5148 |
| 1250 | .1212 | .5345 | .1239 | .5351 | - | - | - | - | .1017 | .5217 |
| 1300 | .1259 | .5470 | .1286 | .5476 | - | - | - | - | .0998 | .5286 |
| 500 | .0462 | .2125 | .0473 | .2127 | - | - | - | - | .0185 | .1937 |
| 900 | .0864 | .3890 | .0883 | .3894 | - | - | - | - | .0595 | .3704 |
| 1400 | .1404 | .5819 | .1433 | .5826 | - | - | - | - | .0795 | .5115 |
| 1600 | .1927 | .6107 | .1958 | .6117 | - | - | - | - | -.0536 | .5417 |
| 600 | .0649 | .2404 | .0661 | .2407 | - | - | - | - | -.1833 | .1707 |
| 1200 | .1375 | .4740 | .1399 | .4747 | - | - | - | - | -.1095 | .4047 |
| 1800 | .2279 | .6714 | .2313 | .6725 | - | - | - | - | .6633 | 2.4305 |
| 2000 | .3182 | .7103 | .3218 | .7119 | - | - | - | - | 1.6984 | 4.8164 |
| 2200 | .3792 | .8006 | .3832 | .8025 | - | - | - | - | 2.5154 | 7.0360 |
| 2400 | .4330 | .9358 | .4377 | .9380 | - | - | - | - | 3.5395 | 9.9191 |
| 2600 | .4897 | 1.0230 | .4948 | 1.0254 | - | - | - | - | 4.8255 | 13.2397 |
| 2800 | .5078 | 1.0089 | .5128 | 1.0114 | - | - | - | - | 6.9492 | 18.8651 |

TABLE XV

Test II

Position #6

Pages 16,17,18

| Press. | $\leftarrow R \rightarrow$ | | Diag. | $\leftarrow \Delta \epsilon \rightarrow$ | | Princ. | θ | $\leftarrow \sigma \rightarrow$ | | $\leftarrow \epsilon \rightarrow$ | |
|--------|----------------------------|--------|-------|--|--------|--------|----------|---------------------------------|-------|-----------------------------------|---------|
| | Axial | Tang. | | Axial | Tang. | | | Axial | Tang. | Axial | Tang. |
| 400 | -.0112 | .2513 | .0228 | -.0099 | .2512 | .2833 | +18-16 | 2160 | 8183 | -.0099 | .2512 |
| 600 | -.0327 | .3616 | .0356 | -.0309 | .3614 | .3997 | +16-35 | 2555 | 11609 | -.0309 | .3614 |
| 800 | -.0234 | .4904 | .0492 | -.0209 | .4903 | .5494 | +17-50 | 4161 | 15957 | -.0209 | .4903 |
| 1000 | -.0271 | .6189 | .0588 | -.0240 | .6188 | .6962 | +18-09 | 5328 | 20164 | -.0240 | .6188 |
| 1100 | -.0267 | .6813 | .0670 | -.0233 | .6812 | .7663 | +18-10 | 5971 | 22228 | -.0233 | .6812 |
| 1200 | -.0239 | .7516 | .0764 | -.0201 | .7515 | - | - | - | - | .0675 | .9130 |
| 1250 | -.0236 | .7700 | .0807 | -.0198 | .7699 | - | - | - | - | .1160 | .9642 |
| 1300 | -.0156 | .8065 | .0871 | -.0116 | .8064 | - | - | - | - | .1944 | 1.0455 |
| 500 | -.0123 | .3002 | .0269 | -.0108 | .3001 | - | - | - | - | .1952 | .5392 |
| 900 | -.0200 | .5619 | .0592 | -.0172 | .5618 | - | - | - | - | .1888 | .8009 |
| 1400 | -.0063 | .9046 | .1094 | .0108 | .9046 | - | - | - | - | .5171 | 1.5374 |
| 1600 | .0998 | 1.1515 | .1934 | .1056 | 1.1520 | - | - | - | - | 2.3334 | 5.4698 |
| 600 | .0223 | 0.3995 | .0636 | .0243 | .3996 | - | - | - | - | 2.0521 | 4.7174 |
| 1200 | .0383 | 0.7923 | .1262 | .0423 | .7925 | - | - | - | - | 2.0701 | 5.1103 |
| 1800 | .1779 | 1.3328 | .2289 | .1846 | 1.3337 | - | - | - | - | 2.6365 | 10.6465 |
| 2000 | .2632 | 1.4870 | .2820 | .2706 | 1.4883 | - | - | - | - | 2.9129 | 16.1530 |
| 2200 | .3718 | NG | .3126 | - | - | - | - | - | - | - | - |
| 2400 | .4696 | NG | .3324 | - | - | - | - | - | - | - | - |
| 2600 | .5635 | NG | .2928 | - | - | - | - | - | - | - | - |
| 2800 | .6793 | NG | .1957 | - | - | - | - | - | - | - | - |

TABLE XVI

Test II

Position #7

Pages 19,20,21

| Press. | $\leftarrow R \rightarrow$ | | | $\leftarrow \Delta \epsilon \rightarrow$ | | | $\leftarrow \sigma \rightarrow$ | | | $\leftarrow \epsilon \rightarrow$ | | |
|--------|----------------------------|--------|-------|--|--------|---------------|---------------------------------|--------|-------|-----------------------------------|---------|--------|
| | Axial | Tang. | Diag. | Axial | Tang. | Princ. | θ | Princ. | Axial | Tang. | Axial | Tang. |
| 400 | -.0066 | -.0336 | .0425 | -.0068 | -.0336 | .0435 + 38-55 | - | 605 | -557 | -1174 | -.0068 | -.0336 |
| 600 | -.0112 | -.0475 | .0614 | -.0114 | -.0476 | .0626 + 39-21 | - | 862 | -847 | -1681 | -.0114 | -.0476 |
| 800 | -.0175 | -.0640 | .0822 | -.0178 | -.0641 | .0836 + 39-29 | - | 1118 | -1220 | -2288 | -.0178 | -.0641 |
| 1000 | -.0224 | -.0759 | .1013 | -.0228 | -.0760 | .1026 + 39-58 | - | 1391 | -1503 | -2730 | -.0228 | -.0760 |
| 1100 | -.0244 | -.0838 | .1132 | -.0248 | -.0839 | .1147 + 38-58 | - | 1570 | -1648 | -3010 | -.0248 | -.0839 |
| 1200 | -.0242 | -.0896 | .1218 | -.0246 | -.0897 | - | - | - | - | - | -.0298 | -.1084 |
| 1250 | -.0269 | -.0860 | .1236 | -.0273 | -.0861 | - | - | - | - | - | -.0318 | -.1169 |
| 1300 | -.0276 | -.0930 | .1269 | -.0281 | -.0931 | - | - | - | - | - | -.0316 | -.1277 |
| 500 | -.0103 | -.0359 | .0499 | -.0105 | -.0360 | - | - | - | - | - | -.0140 | -.0706 |
| 900 | -.0203 | -.0678 | .0938 | -.0206 | -.0679 | - | - | - | - | - | -.0241 | -.1025 |
| 1400 | -.0333 | -.1031 | .1334 | -.0338 | -.1033 | - | - | - | - | - | -.0387 | -.1686 |
| 1600 | -.0493 | -.0998 | .1394 | -.0498 | -.1000 | - | - | - | - | - | -.0634 | -.2847 |
| 600 | -.0156 | -.0389 | .0509 | -.0158 | -.0390 | - | - | - | - | - | -.0294 | -.2237 |
| 1200 | -.0413 | -.0802 | .1015 | -.0417 | -.0804 | - | - | - | - | - | -.0553 | -.2651 |
| 1800 | -.0743 | -.1020 | .1379 | -.0748 | -.1024 | - | - | - | - | - | -.2306 | -.4977 |
| 2000 | -.1085 | -.0854 | .1229 | -.1089 | -.0859 | - | - | - | - | - | -.4937 | -.7576 |
| 2200 | -.1139 | -.0573 | .1440 | -.1142 | -.0579 | - | - | - | - | - | -.8624 | -.9176 |
| 2400 | -.1261 | -.0255 | .1821 | -.1262 | -.0261 | - | - | - | - | - | -1.0256 | -.8471 |
| 2600 | -.1211 | .0154 | .2083 | -.1210 | .0148 | - | - | - | - | - | -1.1384 | -.6243 |
| 2800 | -.0847 | .0710 | .2546 | -.0843 | .0706 | - | - | - | - | - | -1.5323 | -.1973 |

TABLE XVII

Gages 22 & 23

Position #8

Test II

| Press. | $\leftarrow R \rightarrow$ | | $\leftarrow \Delta \epsilon \rightarrow$ | | θ | $\leftarrow \sigma \rightarrow$ | | $\leftarrow \epsilon \rightarrow$ | |
|--------|----------------------------|--------|--|--------|----------|---------------------------------|--------|-----------------------------------|---------|
| | Axial | Tang. | Diag. | Axial | | Tang. | Princ. | Axial | Tang. |
| 400 | -.0390 | -.0307 | - | -.0390 | -.0307 | - | -1589 | -1398 | -.0390 |
| 600 | -.0579 | -.0432 | - | -.0579 | -.0432 | - | -2338 | -1998 | -.0579 |
| 800 | -.0730 | -.0597 | - | -.0730 | -.0597 | - | -2997 | -2690 | -.0730 |
| 1000 | -.0934 | -.0741 | - | -.0934 | -.0741 | - | -3811 | -3366 | -.0934 |
| 1100 | -.1023 | -.0801 | - | -.1023 | -.0801 | - | -4164 | -3653 | -.1023 |
| 1200 | -.1083 | -.0856 | - | -.1083 | -.0856 | - | - | - | -.1270 |
| 1250 | -.1145 | -.0896 | - | -.1145 | -.0896 | - | - | - | -.1355 |
| 1300 | -.1171 | -.0918 | - | -.1171 | -.0918 | - | - | - | -.1370 |
| 500 | -.0443 | -.0353 | - | -.0443 | -.0353 | - | - | - | -.0642 |
| 900 | -.0868 | -.0674 | - | -.0868 | -.0674 | - | - | - | -.1067 |
| 1400 | -.1255 | -.0963 | - | -.1255 | -.0963 | - | - | - | -.1465 |
| 1600 | -.1479 | -.0923 | - | -.1479 | -.0923 | - | - | - | -.2295 |
| 600 | -.0635 | -.0361 | - | -.0635 | -.0361 | - | - | - | -.1451 |
| 1200 | -.1248 | -.0754 | - | -.1248 | -.0754 | - | - | - | -.2064 |
| 1800 | -.1697 | -.0787 | - | -.1697 | -.0787 | - | - | - | -.3453 |
| 2000 | -.1945 | -.0733 | - | -.1945 | -.0733 | - | - | - | -.4368 |
| 2200 | -.1808 | -.0610 | - | -.1808 | -.0610 | - | - | - | -.6109 |
| 2400 | -.1527 | -.0502 | - | -.1527 | -.0502 | - | - | - | -.7606 |
| 2600 | -.1447 | -.0276 | - | -.1447 | -.0276 | - | - | - | -.9359 |
| 2800 | -.1137 | -.0113 | - | -.1137 | -.0113 | - | - | - | -1.2371 |
| | | | | | | | | | .5097 |

TABLE XVIII

Gages 1 & 24

Test II

Position #9

| Press. | $\leftarrow R \rightarrow$ | | Diag. | $\leftarrow \Delta E \rightarrow$ | | θ | $\leftarrow \rightarrow$ | | $\leftarrow \epsilon \rightarrow$ | | |
|--------|----------------------------|--------|-------|-----------------------------------|--------|----------|--------------------------|-------|-----------------------------------|---------|--------|
| | Axial | Tang. | | Axial | Tang. | | Princ. | Axial | Tang. | Axial | Tang. |
| 400 | .0379 | .2609 | - | .0379 | .2609 | - | - | 3831 | 8978 | .0379 | .2609 |
| 600 | .0586 | .3790 | - | .0586 | .3790 | - | - | 5681 | 13076 | .0586 | .3790 |
| 800 | .0790 | .5128 | - | .0790 | .5128 | - | - | 7675 | 17688 | .0790 | .5128 |
| 1000 | .1023 | .6519 | - | .1023 | .6519 | - | - | 9822 | 22505 | .1023 | .6519 |
| 1100 | .1174 | .7238 | - | .1174 | .7238 | - | - | 11028 | 25024 | .1174 | .7238 |
| 1200 | .0953 | .8185 | - | .0953 | .8185 | - | - | - | - | .2061 | 1.1963 |
| 1250 | .0911 | .8575 | - | .0911 | .8575 | - | - | - | - | .2821 | 1.4422 |
| 1300 | .0774 | .9016 | - | .0774 | .9016 | - | - | - | - | .4146 | 1.8942 |
| 500 | .0483 | .3181 | - | .0483 | .3181 | - | - | - | - | .3855 | 1.3107 |
| 900 | .0890 | .6071 | - | .0890 | .6071 | - | - | - | - | .4262 | 1.5997 |
| 1400 | .1186 | 1.0540 | - | .1186 | 1.0540 | - | - | - | - | .8126 | 4.1393 |
| 1600 | .1198 | NG | - | .1198 | - | - | - | - | - | 1.3072 | - |
| 600 | .0375 | NG | - | .0375 | - | - | - | - | - | 1.2249 | - |
| 1200 | .0563 | NG | - | .0563 | - | - | - | - | - | 1.2437 | - |
| 1800 | .1484 | NG | - | .1484 | - | - | - | - | - | 1.4052 | - |
| 2000 | .0664 | NG | - | .0664 | - | - | - | - | - | .7650 | - |
| 2200 | .0468 | NG | - | .0468 | - | - | - | - | - | -.0689 | - |
| 2400 | -.0429 | NG | - | -.0429 | - | - | - | - | - | -.7222 | - |
| 2600 | -.0440 | NG | - | -.0440 | - | - | - | - | - | -.7927 | - |
| 2800 | -.0856 | NG | - | -.0856 | - | - | - | - | - | -1.0672 | - |

TABLE NO. XIX

Relation of load to $p \cdot \frac{R}{t}$

$$\text{Test I: } \frac{R}{t} = \frac{3.84}{.4} = 9.6$$

$$\text{Test II: } \frac{R}{t} = \frac{3.84}{.3} = 12.8$$

| Test I | | Test II | |
|--------|-----------------------|---------|-----------------------|
| p | $p \cdot \frac{R}{t}$ | p | $p \cdot \frac{R}{t}$ |
| 500 | 4800 | 400 | 5120 |
| 750 | 7200 | 600 | 7680 |
| 1000 | 9600 | 800 | 10240 |
| 1250 | 12000 | 1000 | 12800 |
| 1500 | 14400 | 1100 | 14080 |
| 1600 | 15360 | 1200 | 15360 |
| 1700 | 16320 | 1250 | 16000 |
| 1800 | 17280 | 1300 | 16640 |
| 1900 | 18240 | 1400 | 17920 |
| 2000 | 19200 | 1600 | 20480 |
| 2050 | 19680 | 1800 | 23040 |
| 2150 | 20640 | 2000 | 25600 |
| 2200 | 21120 | 2200 | 28160 |
| 2300 | 22080 | 2400 | 30720 |
| 2400 | 23040 | 2600 | 33280 |
| 2500 | 24000 | 2800 | 35840 |
| 2600 | 24960 | | |
| 2800 | 26880 | | |
| 3000 | 28800 | | |
| 3250 | 31200 | | |

B-1

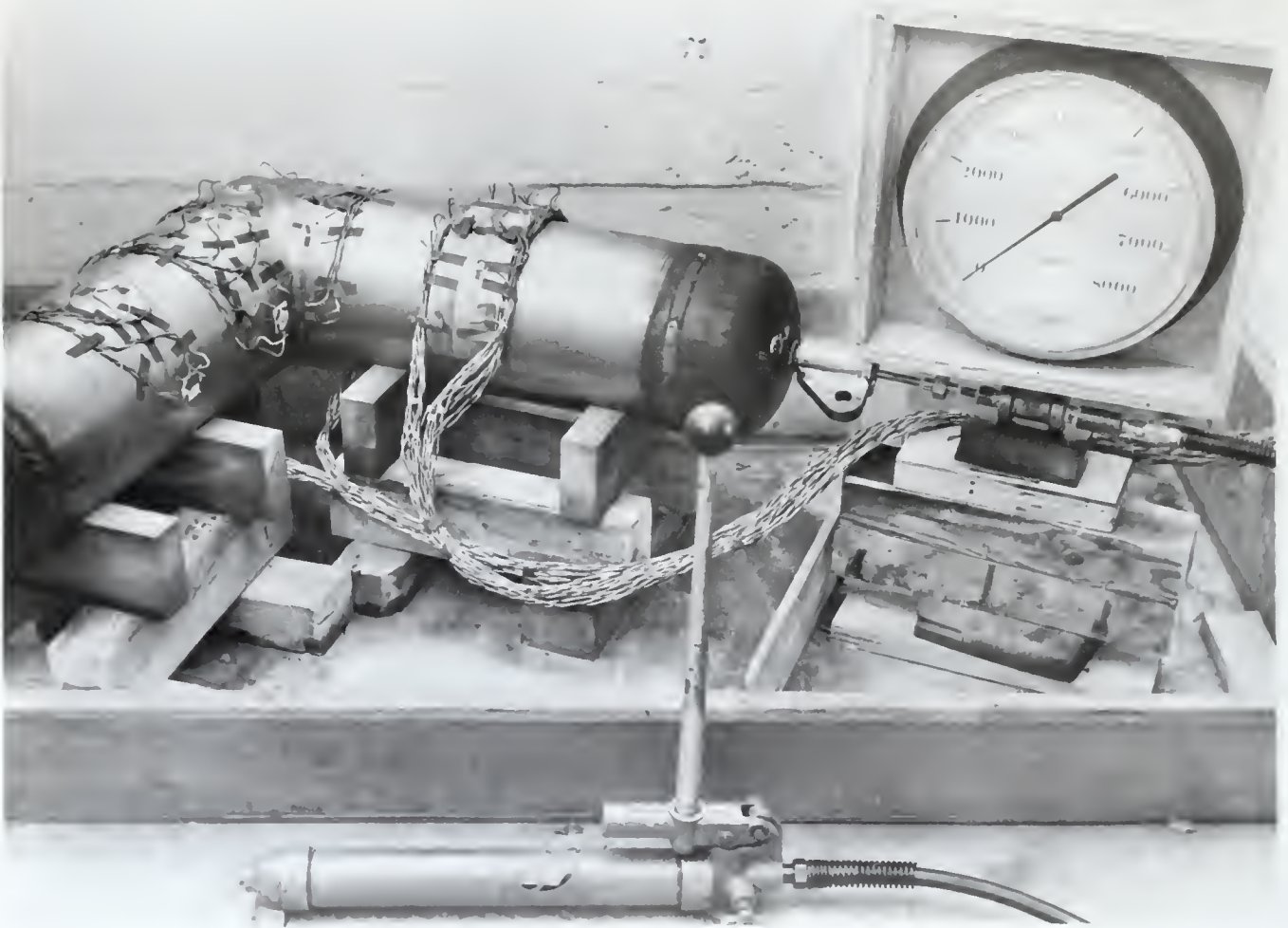


Fig. 1 First specimen and test setup.



Fig. 2 Closeup view of first specimen showing rupture.

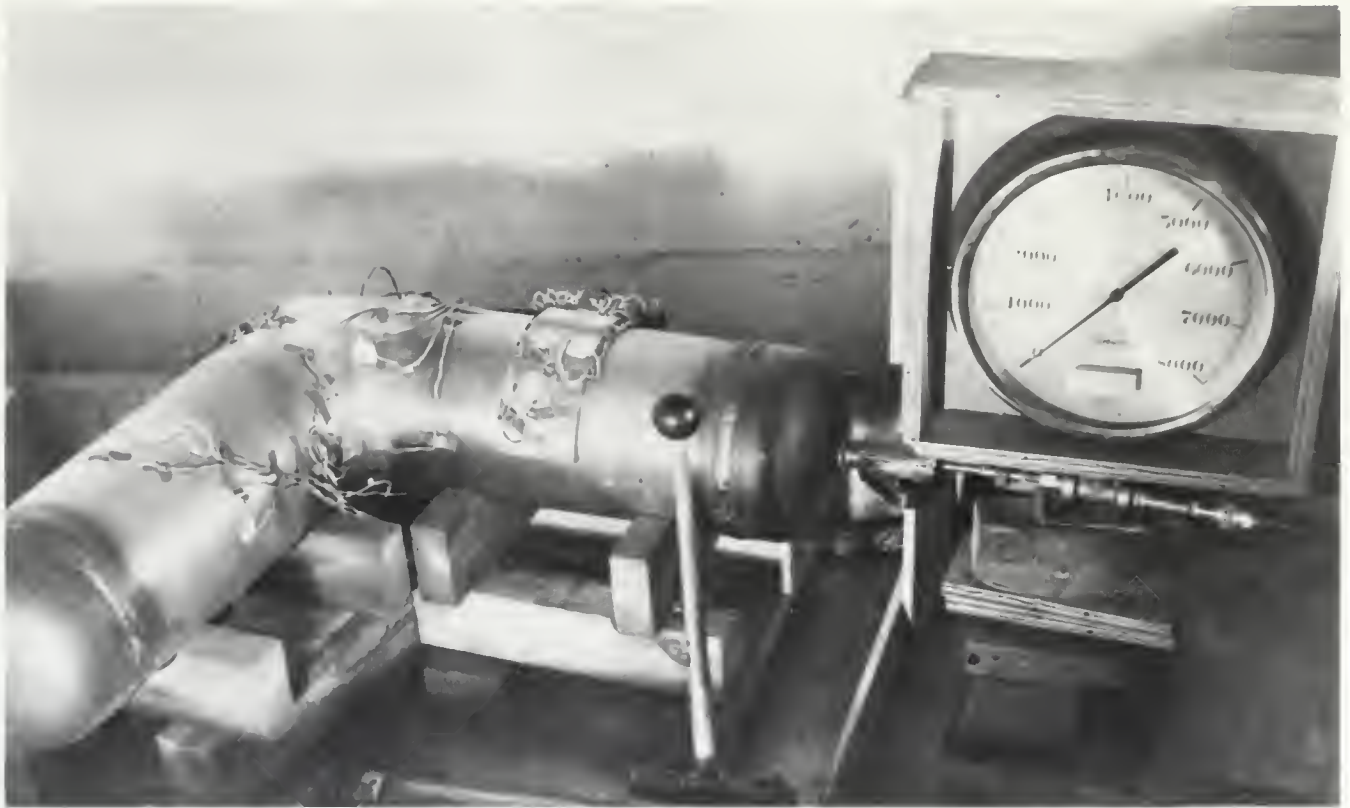


Fig. 3 Second specimen and test setup.

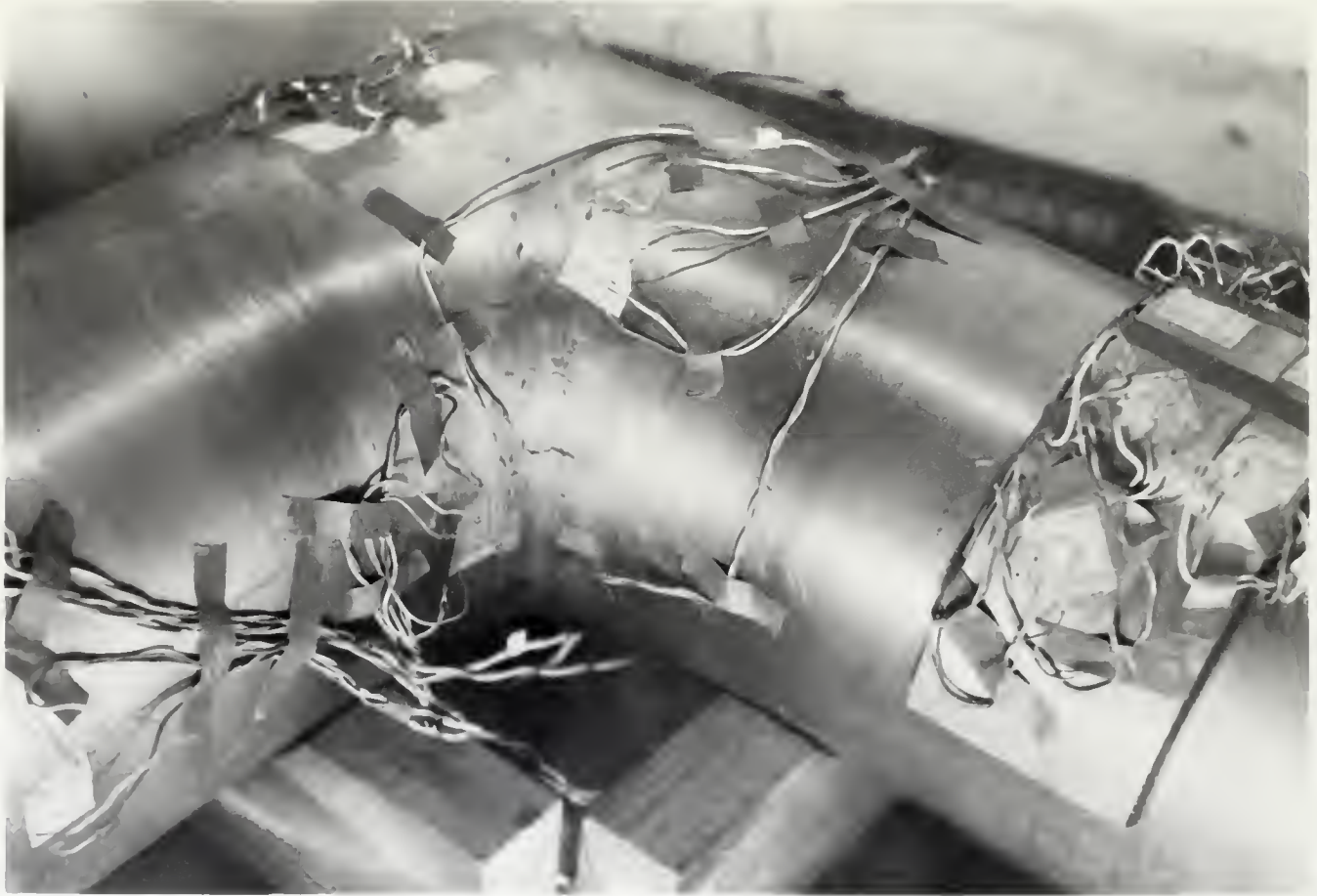


Fig. 4 Closeup view of second specimen showing rupture.

B-5



2 EACH: $t = 0.400''$
 $t = 0.300''$

| | | | | | | | | |
|--|--------|------------|---|---------|----------|----------|-------------|---|
| 8" STEEL TUBING | | MACHINE | | | | | | TOLERANCES - .010 OR $\frac{1}{64}$ UNLESS OTHERWISE NOTED |
| | | | | | | | | |
| MATERIAL | FINISH | HEAT TREAT | DRAFTSMAN | CHECKED | APPROVED | ENGINEER | | |
| GUGGENHEIM AERONAUTICAL LABORATORY CALIFORNIA INSTITUTE OF TECHNOLOGY | | | SPECIMENS FOR PRESSURE TESTS OF 90° CYLINDRICAL CORNER | | | | | |
| | | | NAME | | | | DRAWING NO. | |

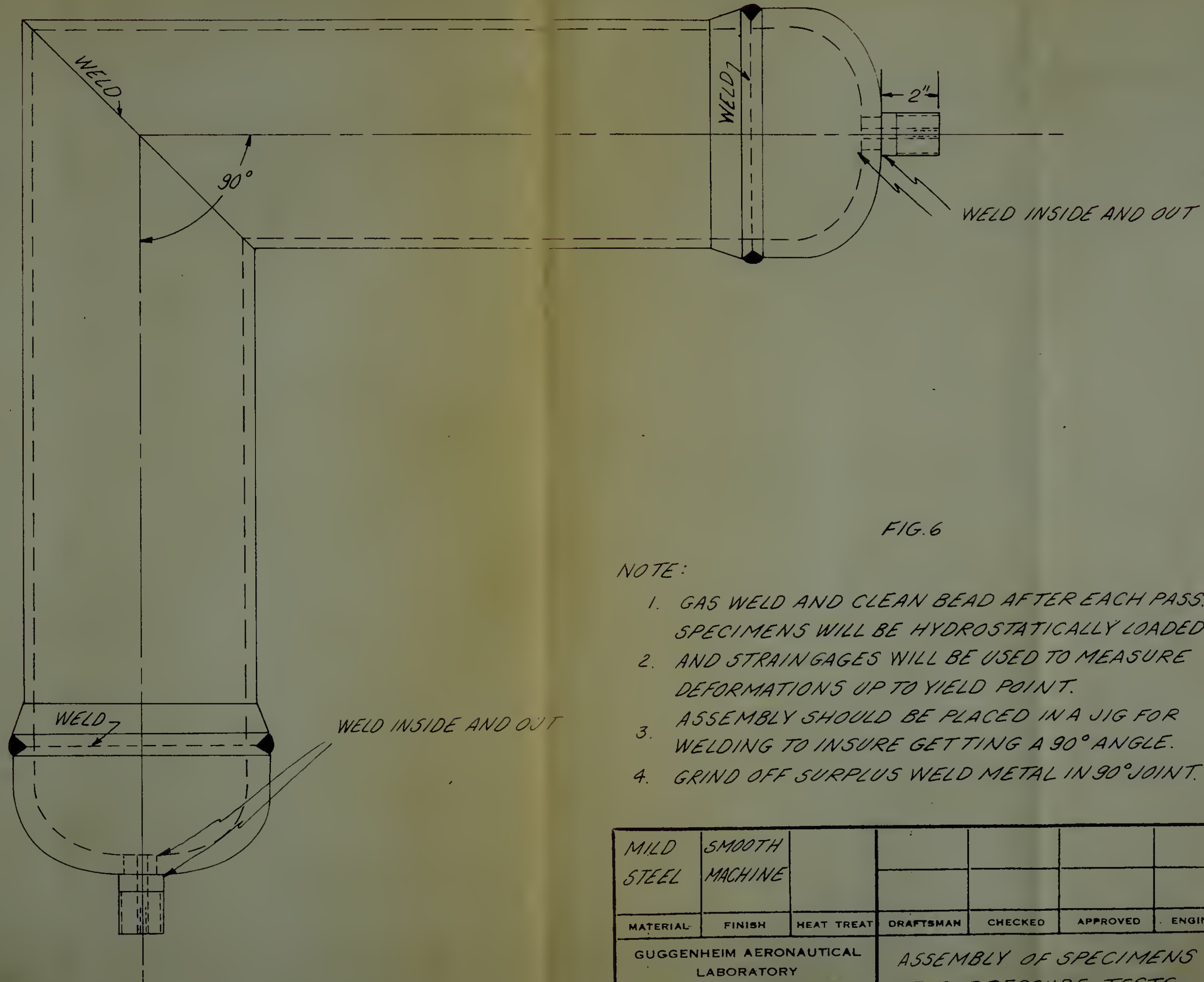


FIG. 6

NOTE:

1. GAS WELD AND CLEAN BEAD AFTER EACH PASS. SPECIMENS WILL BE HYDROSTATICALLY LOADED
2. AND STRAIN GAGES WILL BE USED TO MEASURE DEFORMATIONS UP TO YIELD POINT.
3. ASSEMBLY SHOULD BE PLACED IN A JIG FOR WELDING TO INSURE GETTING A 90° ANGLE.
4. GRIND OFF SURPLUS WELD METAL IN 90° JOINT.

| | | | | | | | |
|--|-------------------|------------|---|---------|----------|----------|---|
| MILD STEEL | SMOOTH MACHINE | | | | | | TOLERANCES = .010 OR $\frac{1}{64}$ UNLESS OTHERWISE NOTED |
| | | | | | | | SCALE: $\frac{1}{4}$ |
| MATERIAL | FINISH | HEAT TREAT | DRAFTSMAN | CHECKED | APPROVED | ENGINEER | |
| GUGGENHEIM AERONAUTICAL LABORATORY CALIFORNIA INSTITUTE OF TECHNOLOGY | | | ASSEMBLY OF SPECIMENS FOR PRESSURE TESTS | | | | |
| | | | NAME | | | | DRAWING NO. |

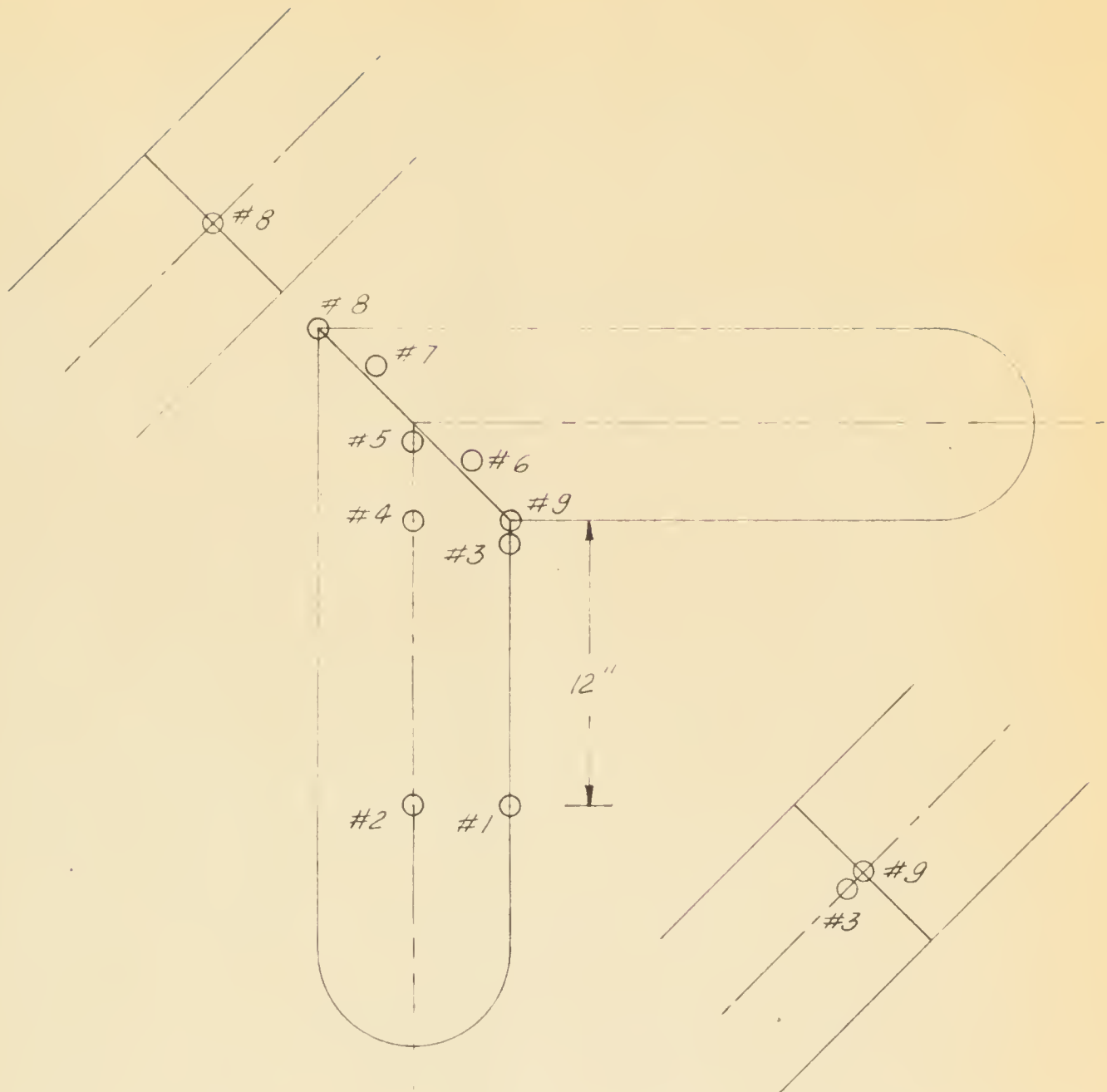


FIG. 7

LOCATION OF STRAIN GAGES
TESTS I AND II

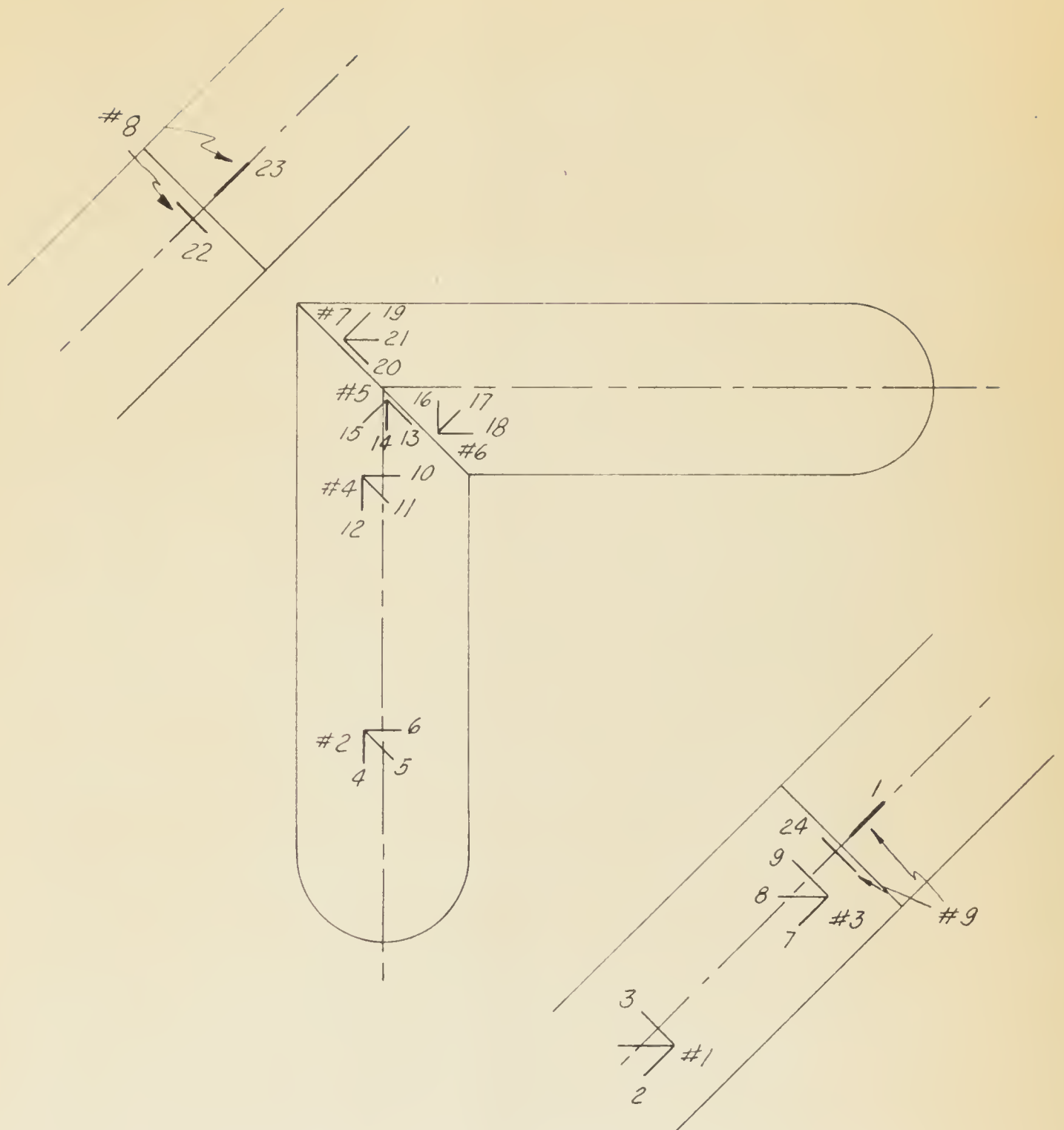


FIG. 8
ORIENTATION OF STRAIN GAGES, TEST I

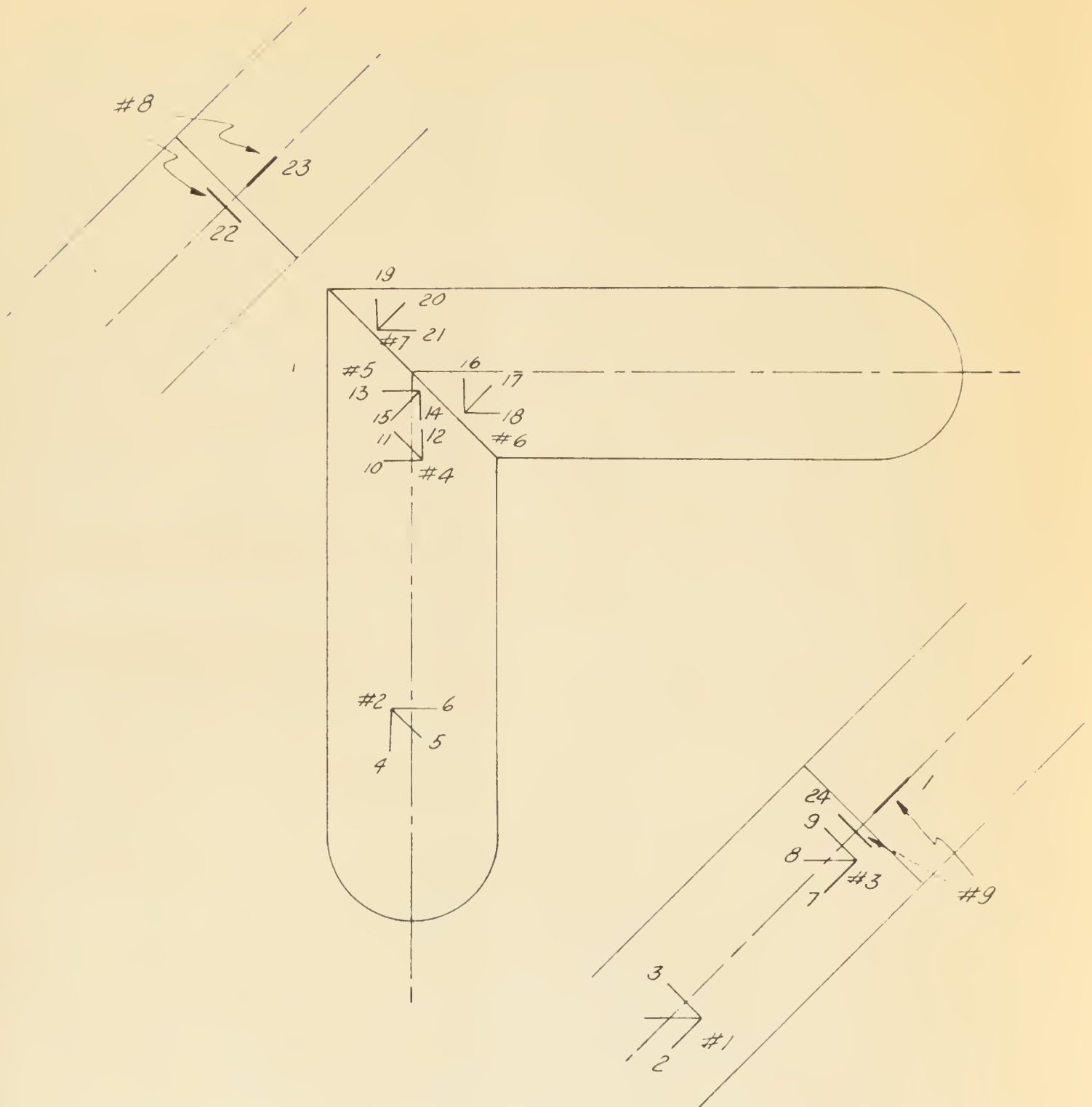
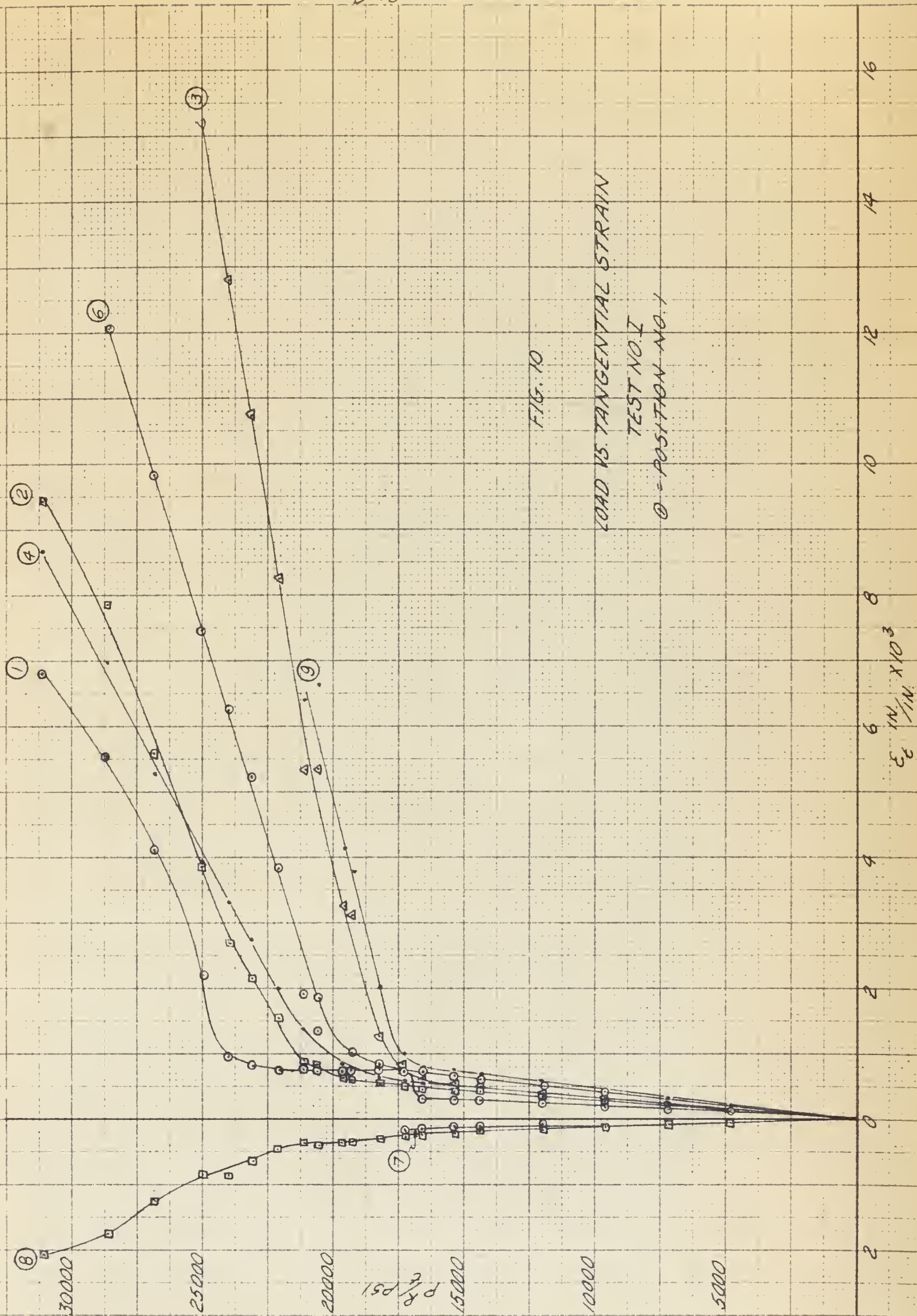
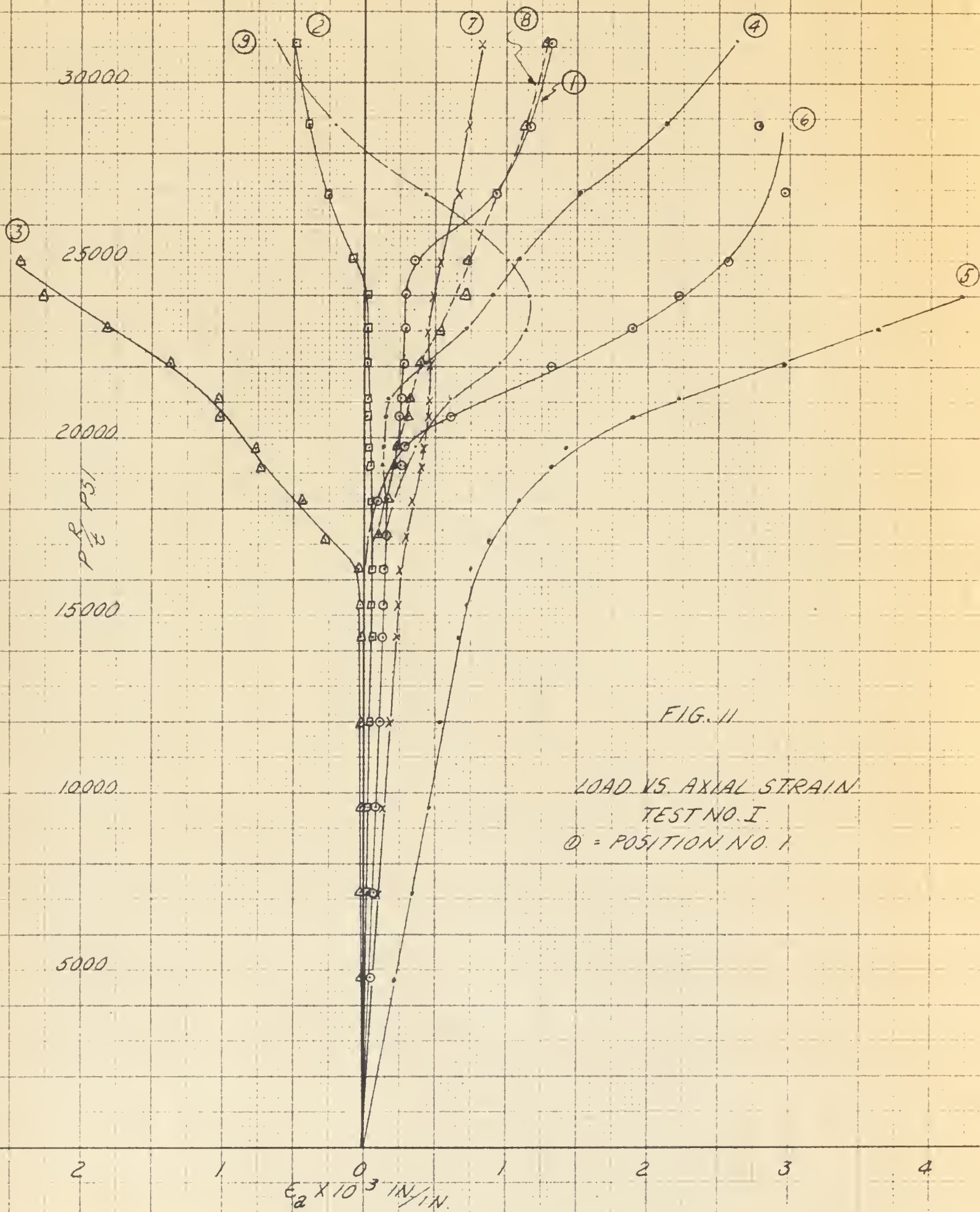


FIG. 9

ORIENTATION OF STRAIN GAGES, TEST II





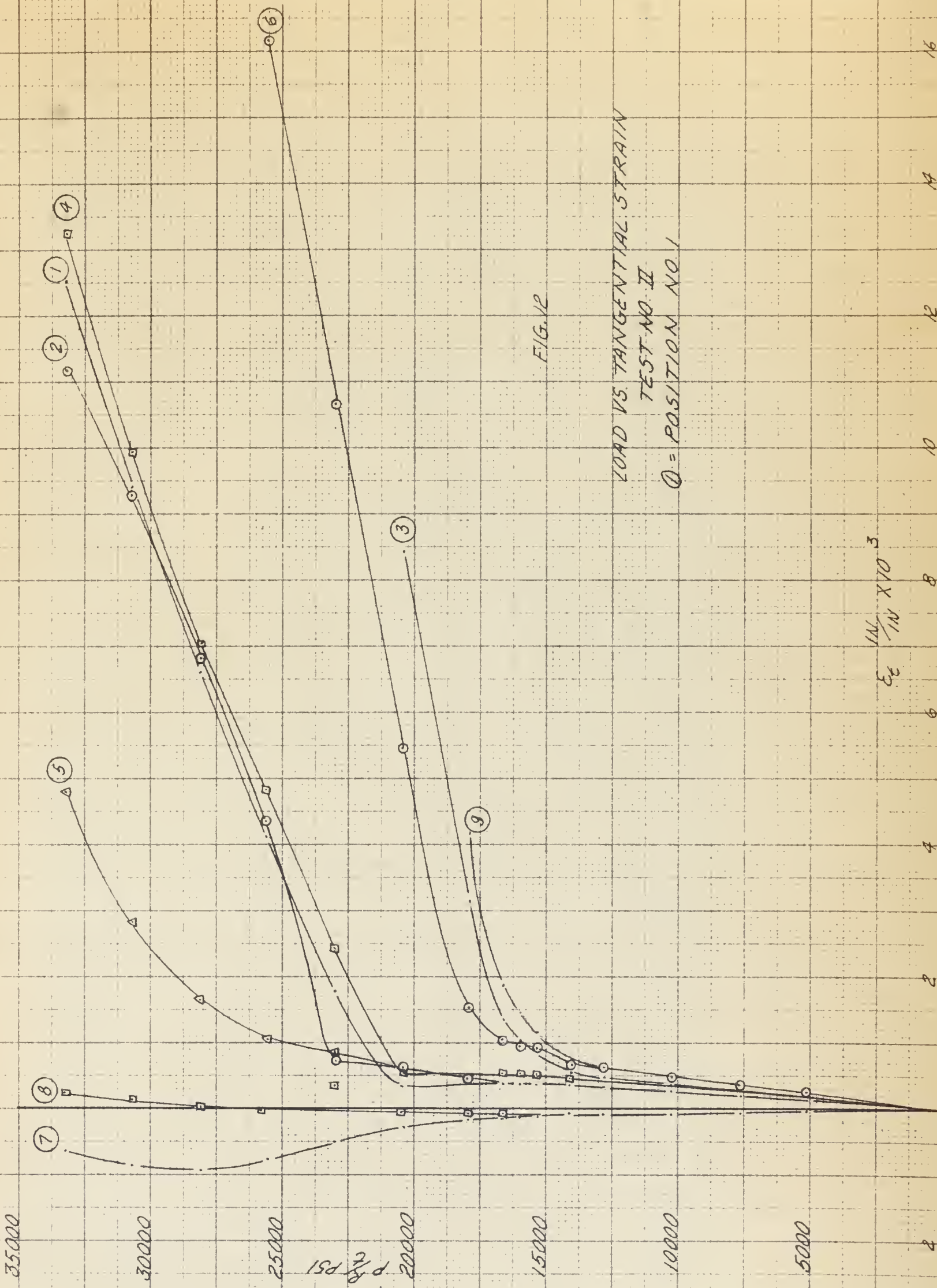
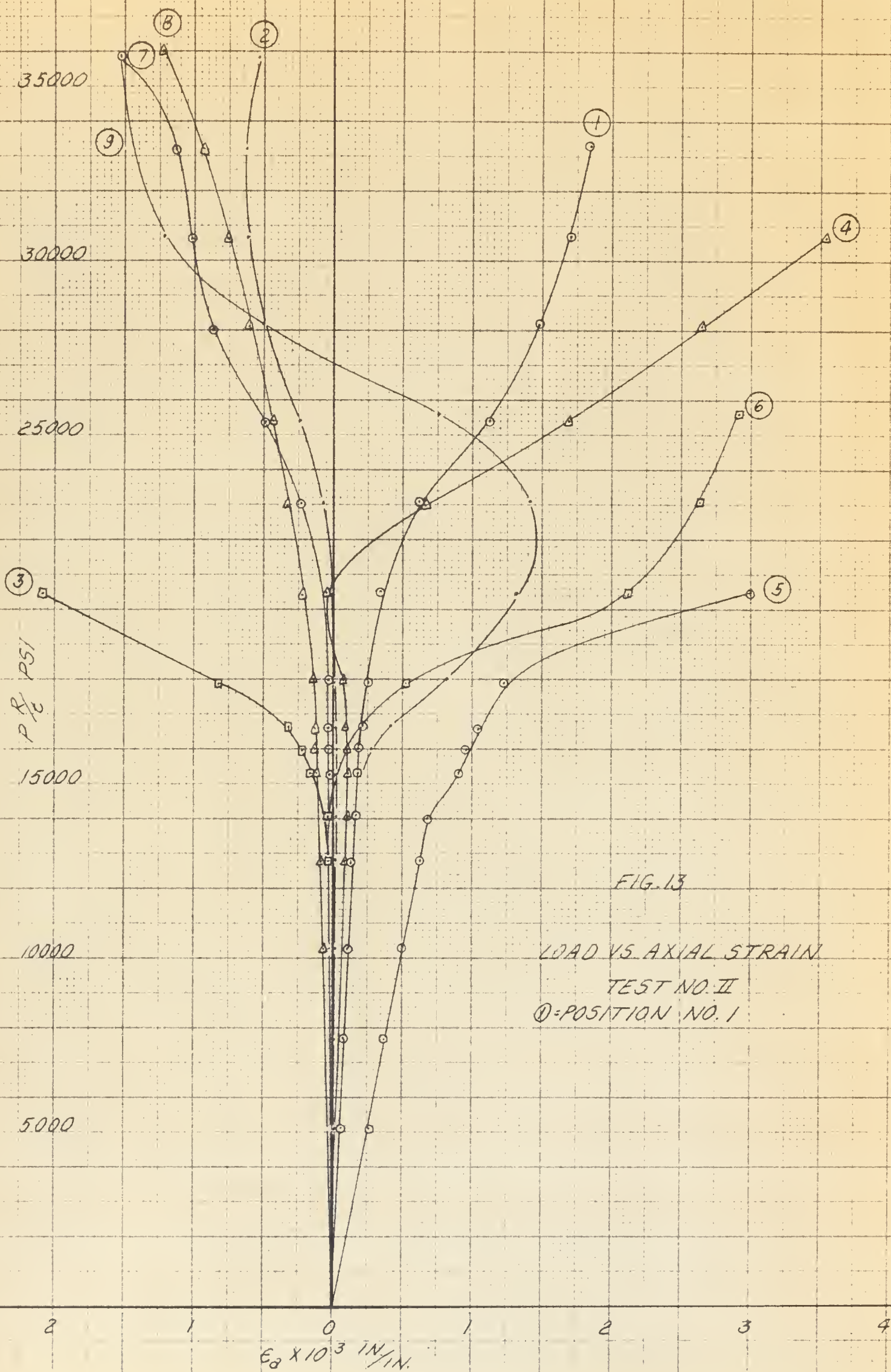


FIG. 12

LOAD VS. TANGENTIAL STRAIN
TEST NO. II
 $\textcircled{1} = \text{POSITION NO. 1}$



II

I

TANGENTIAL STRAIN
IN STRAIGHT CLOSED
TUBE

30000

25000

20000

15000

10000

5000

P/R PSI

FIG. 14

LOAD VS. TANGENTIAL STRAIN

POSITION NO. 1

① = TEST NO. 1

2

0

2

4

6

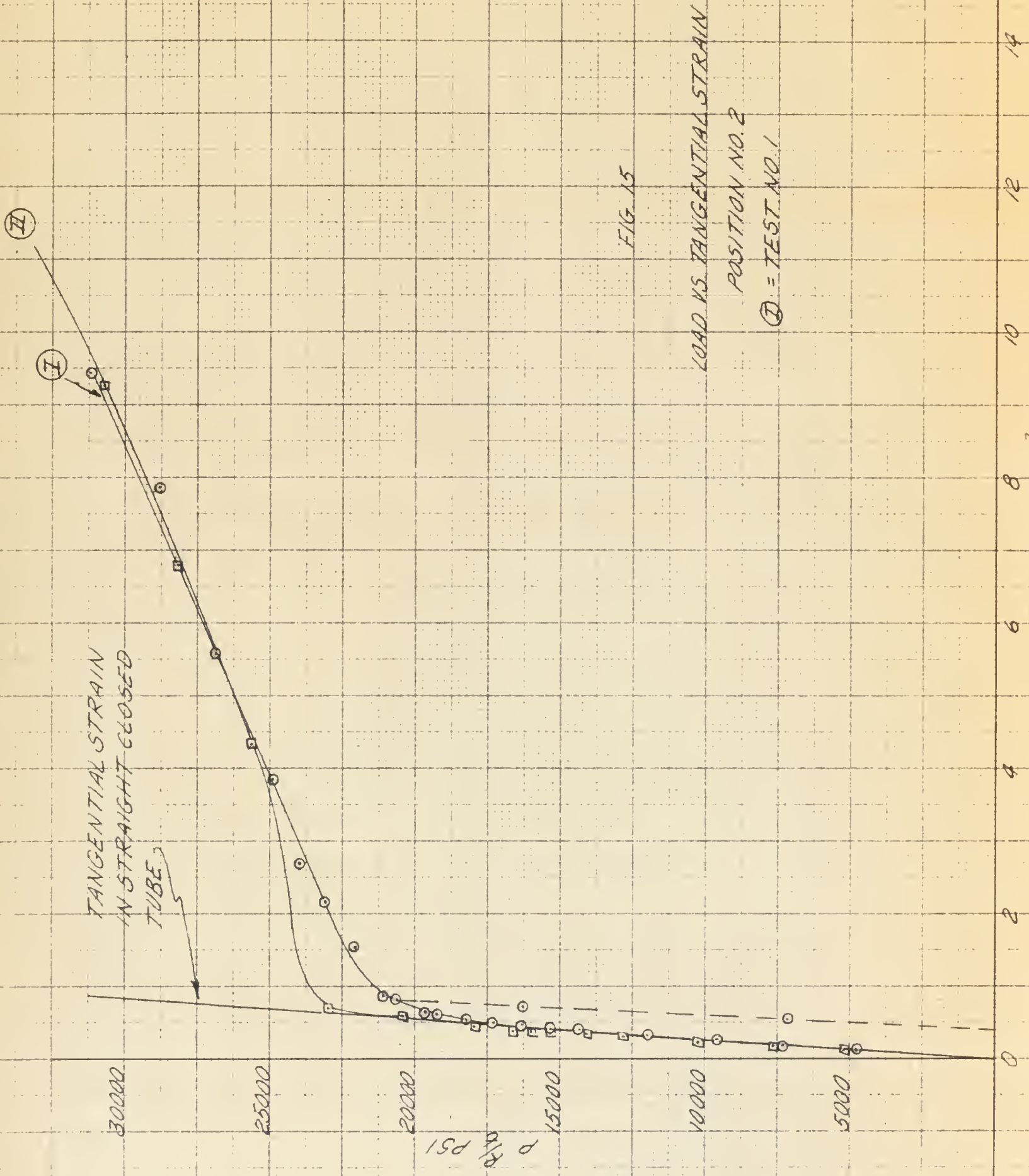
8

10

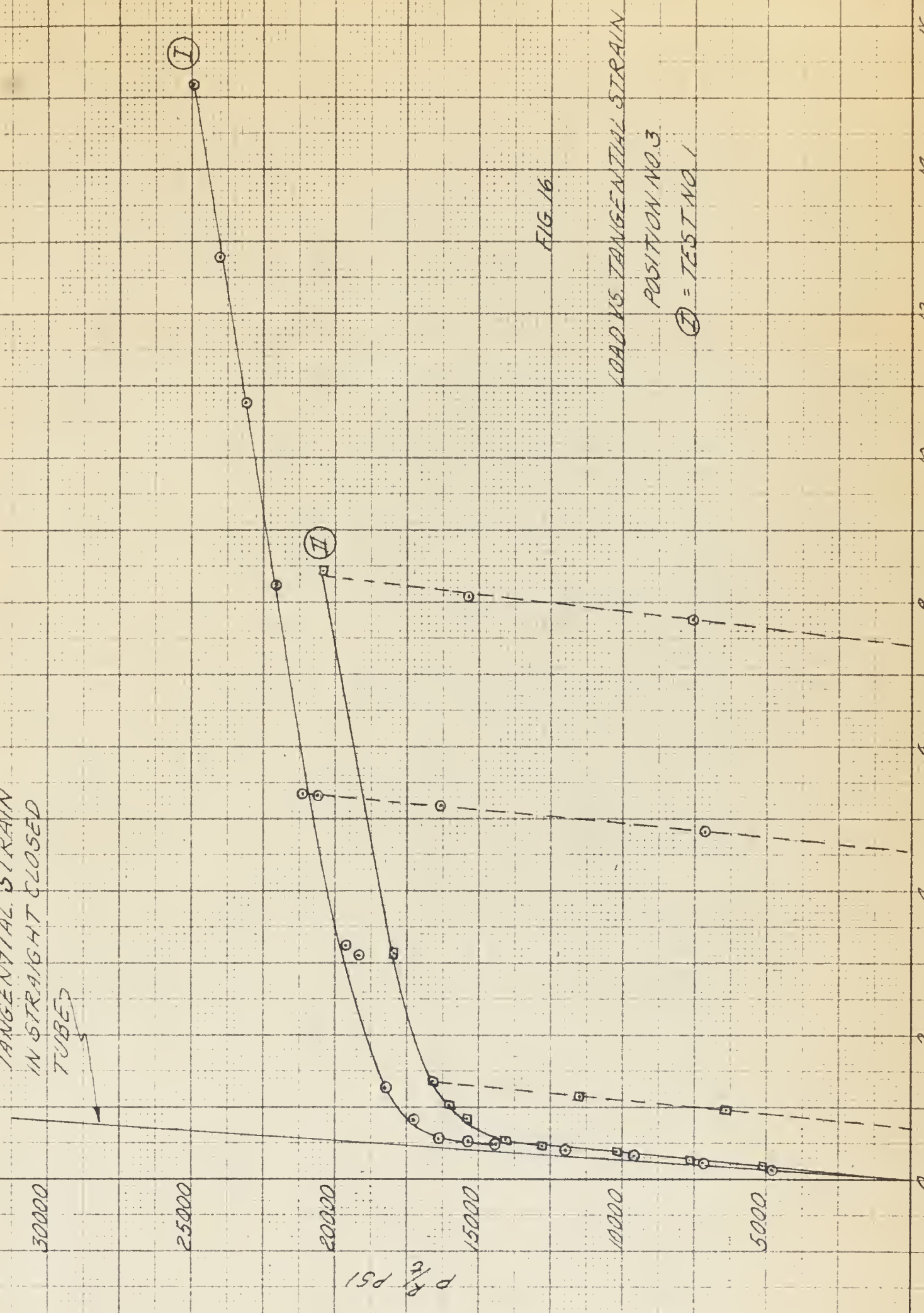
12

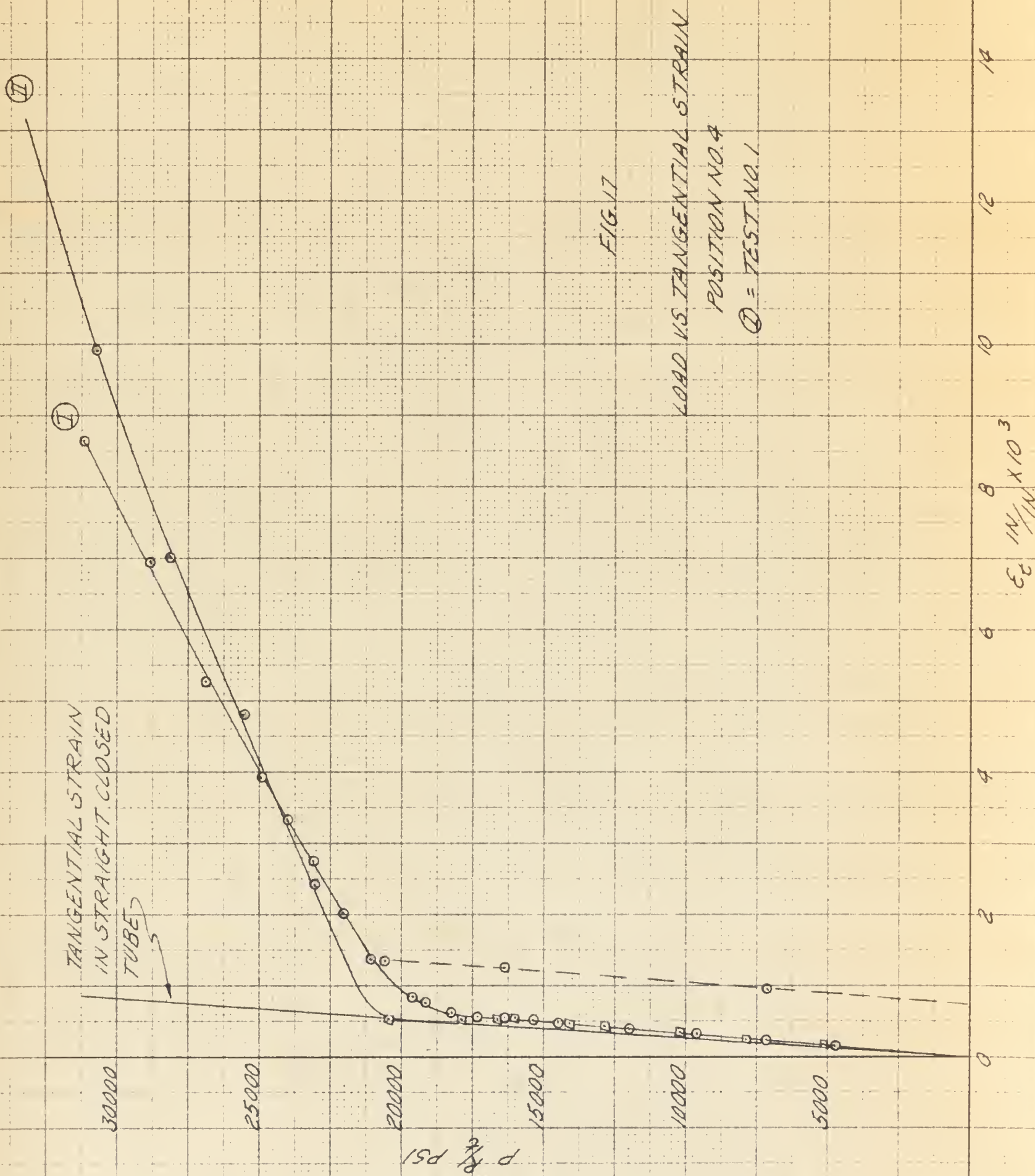
14

ϵ_t IN/IN $\times 10^3$



TANGENTIAL STRAIN
IN STRAIGHT CLOSED
TUBES





TANGENTIAL STRAIN
IN STRAIGHT CLOSED
TUBE

30000

25000

20000

15000

10000

5000

P x 10⁶ PSI

FIG. 18

LOAD VS. TANGENTIAL STRAIN

POSITION NO. 5

① = TEST NO. 1

2

4

6

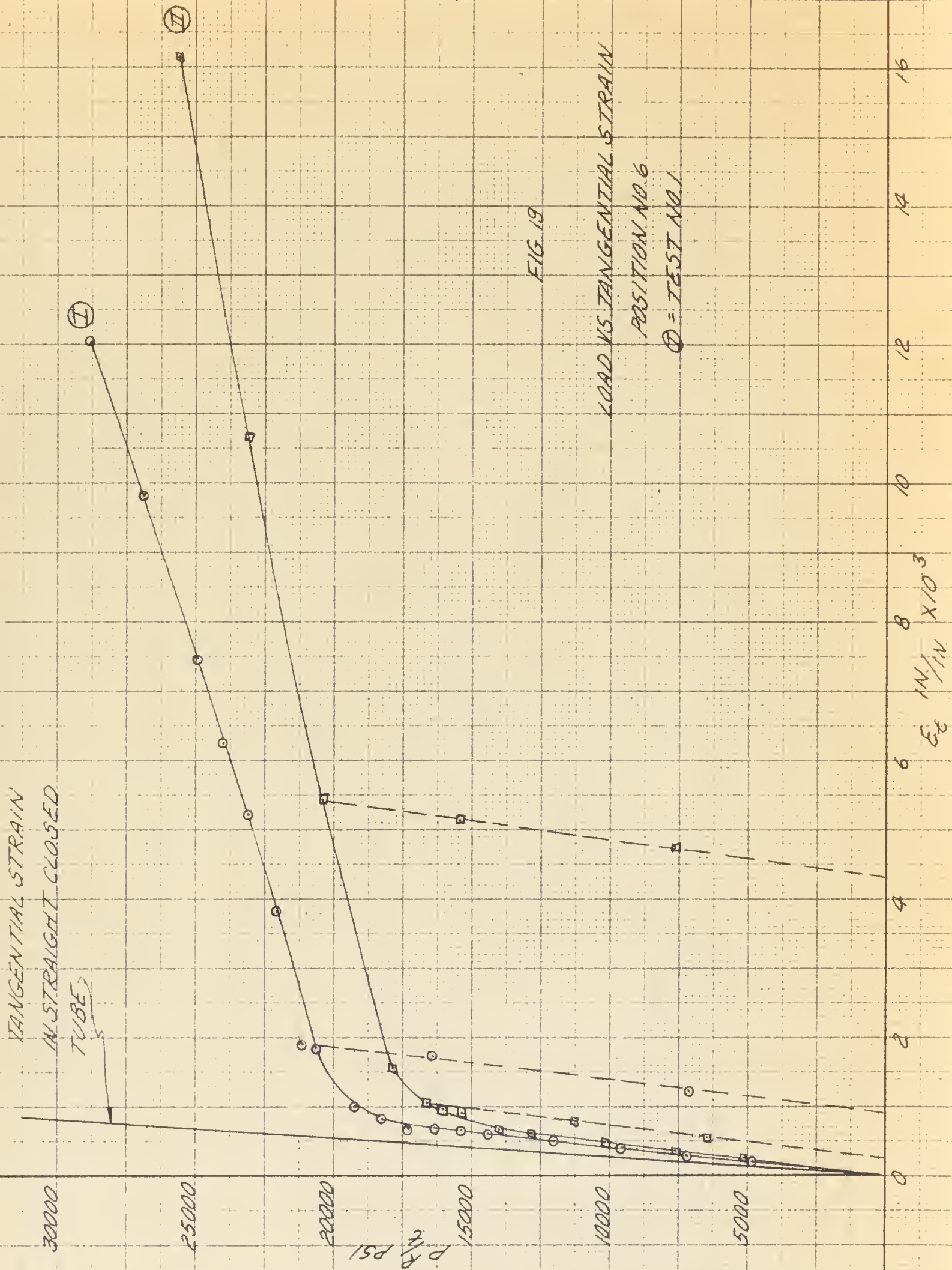
8

10

12

14

 $\epsilon \text{ IN/IN. } \times 10^3$



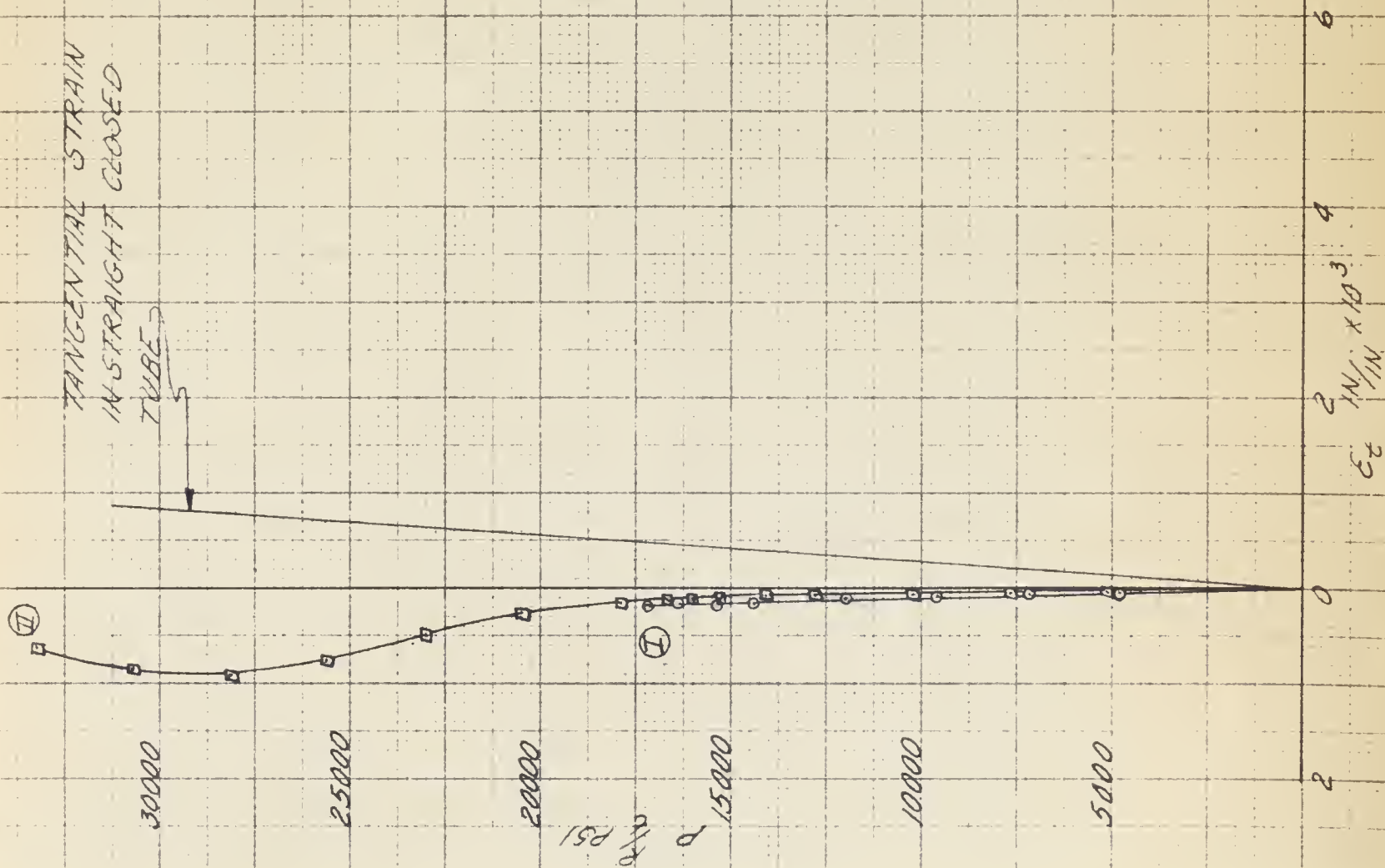
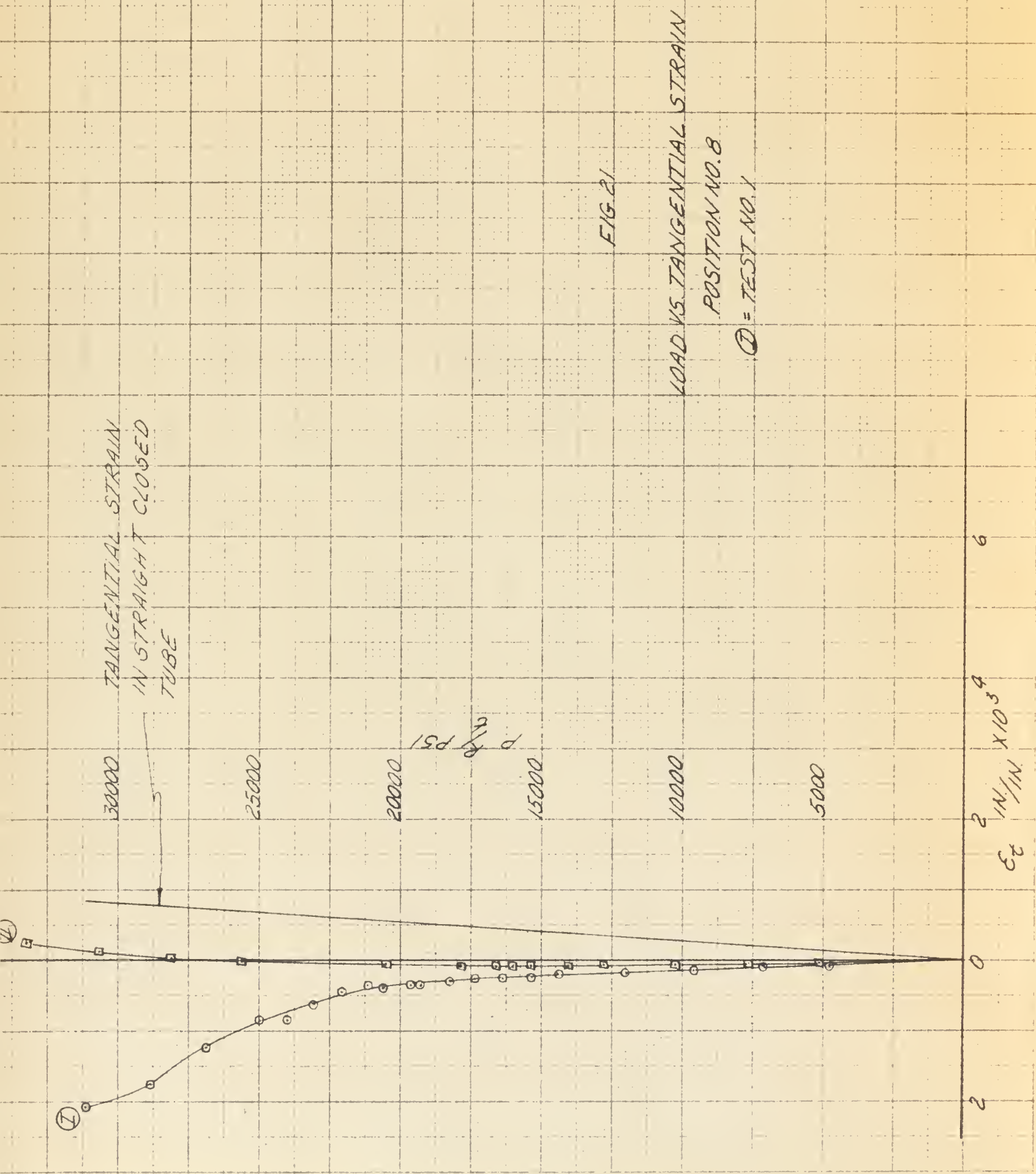


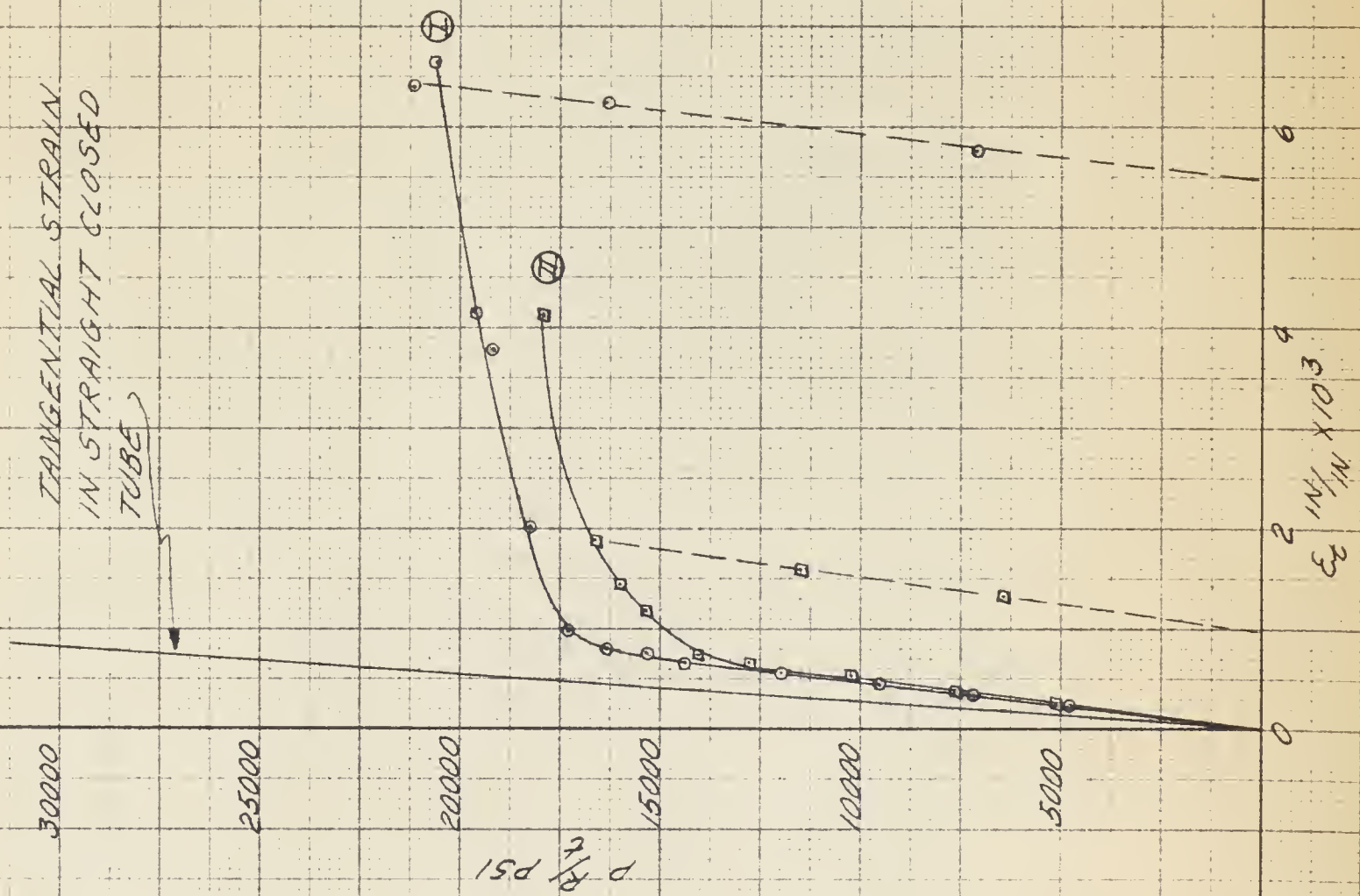
FIG. 20

LOAD VS. TANGENTIAL STRAIN

POSITION NO. 7

① = TEST NO. 1





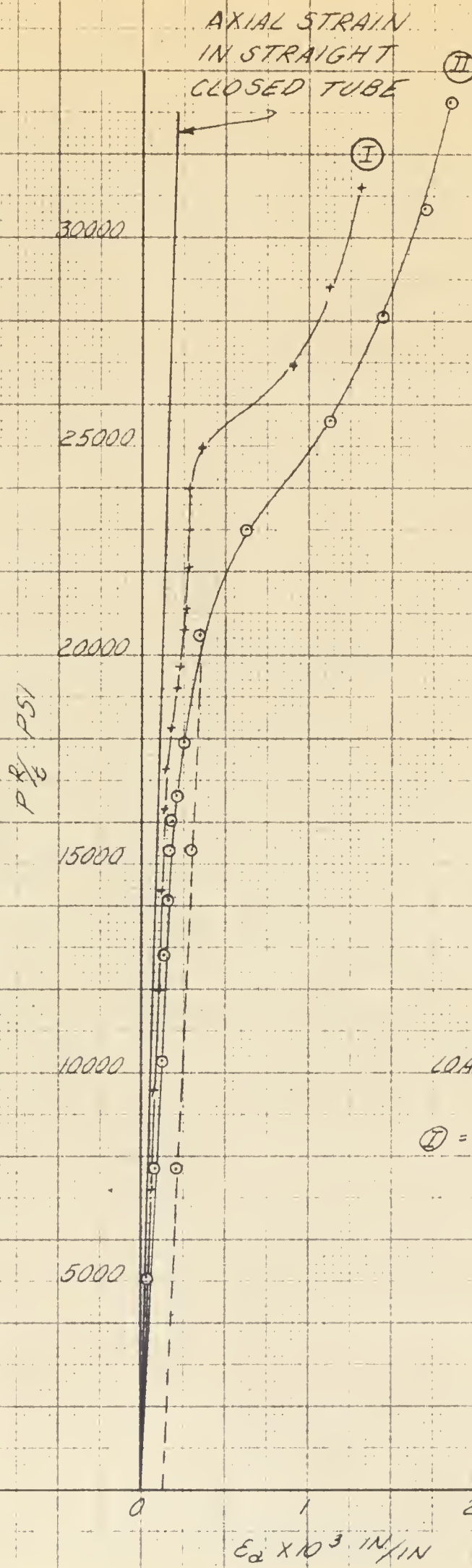


FIG. 23

LOAD VS. AXIAL STRAIN
POSITION NO. 1

① = TEST NO 1

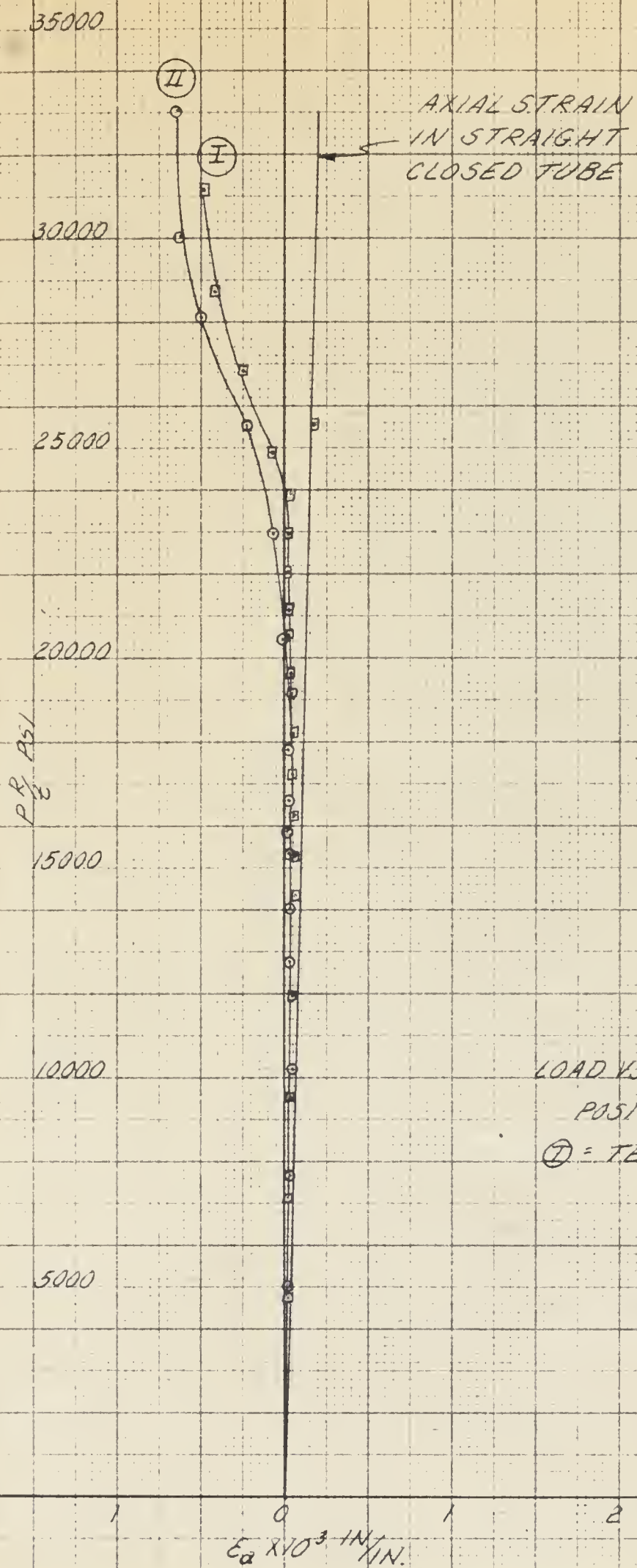


FIG. 24

LOAD VS. AXIAL STRAIN
POSITION NO. 2.
① = TEST NO. 1

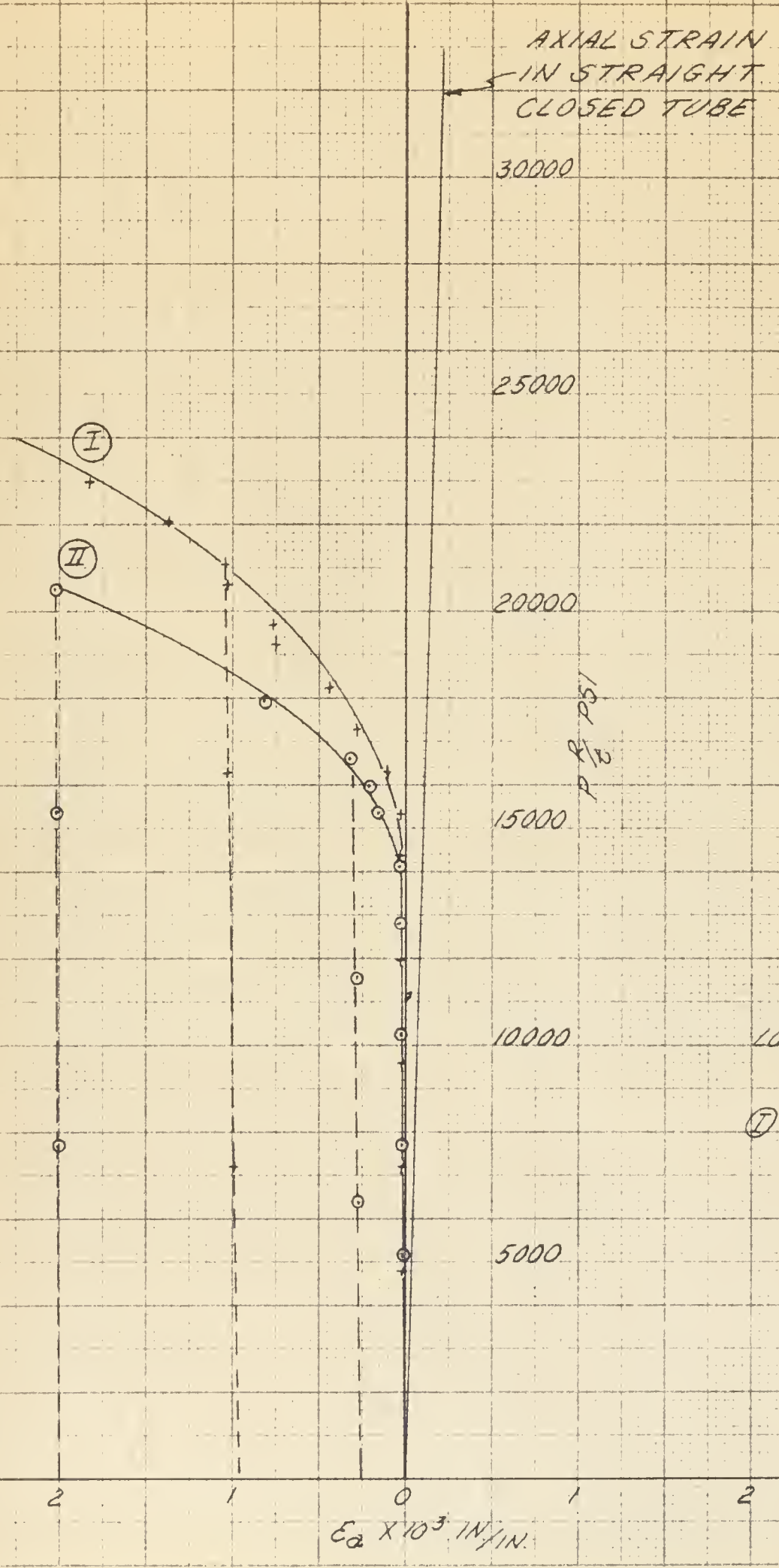
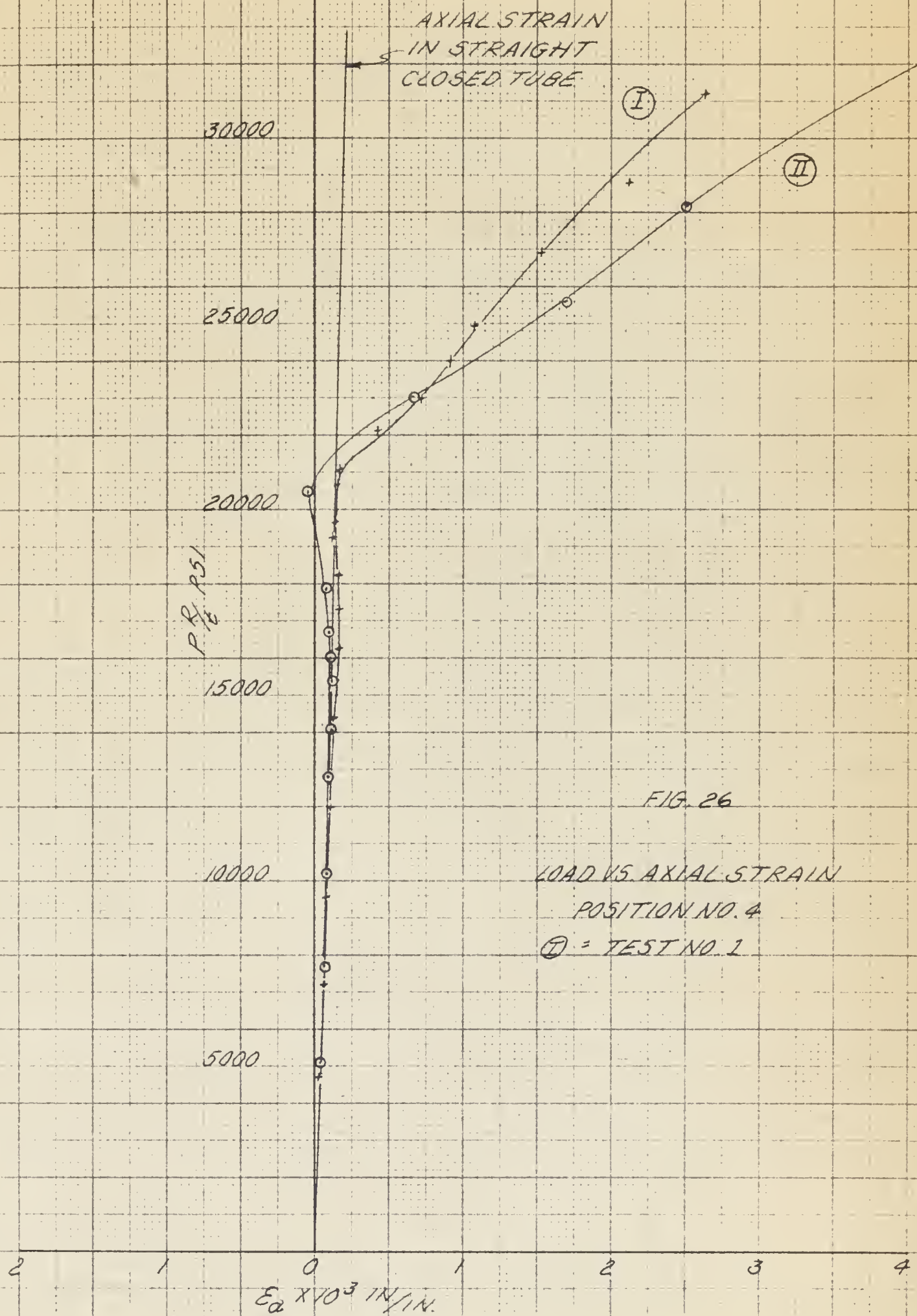
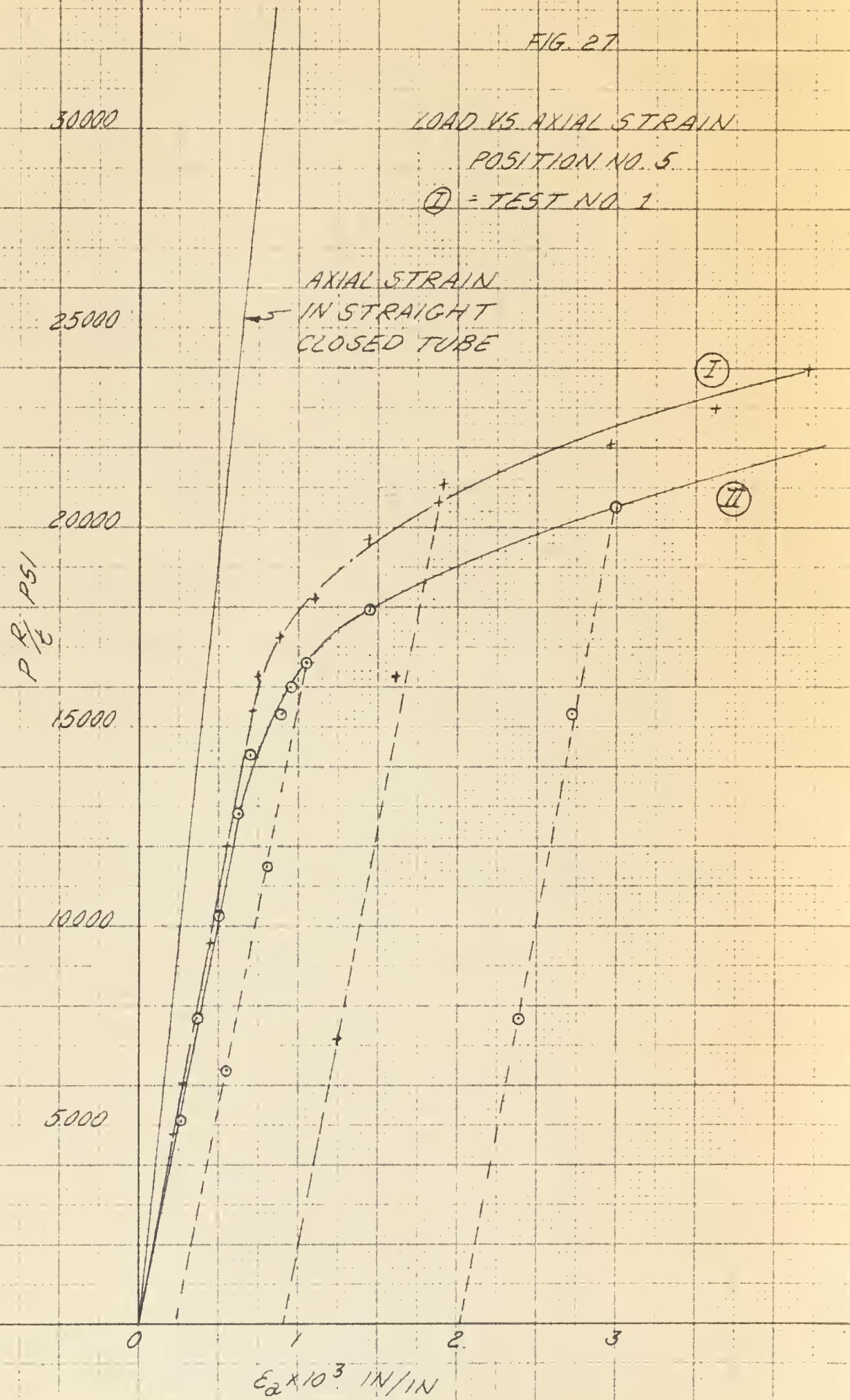


FIG. 25

LOAD VS. AXIAL STRAIN
POSITION NO. 3
① = TEST NO. 1

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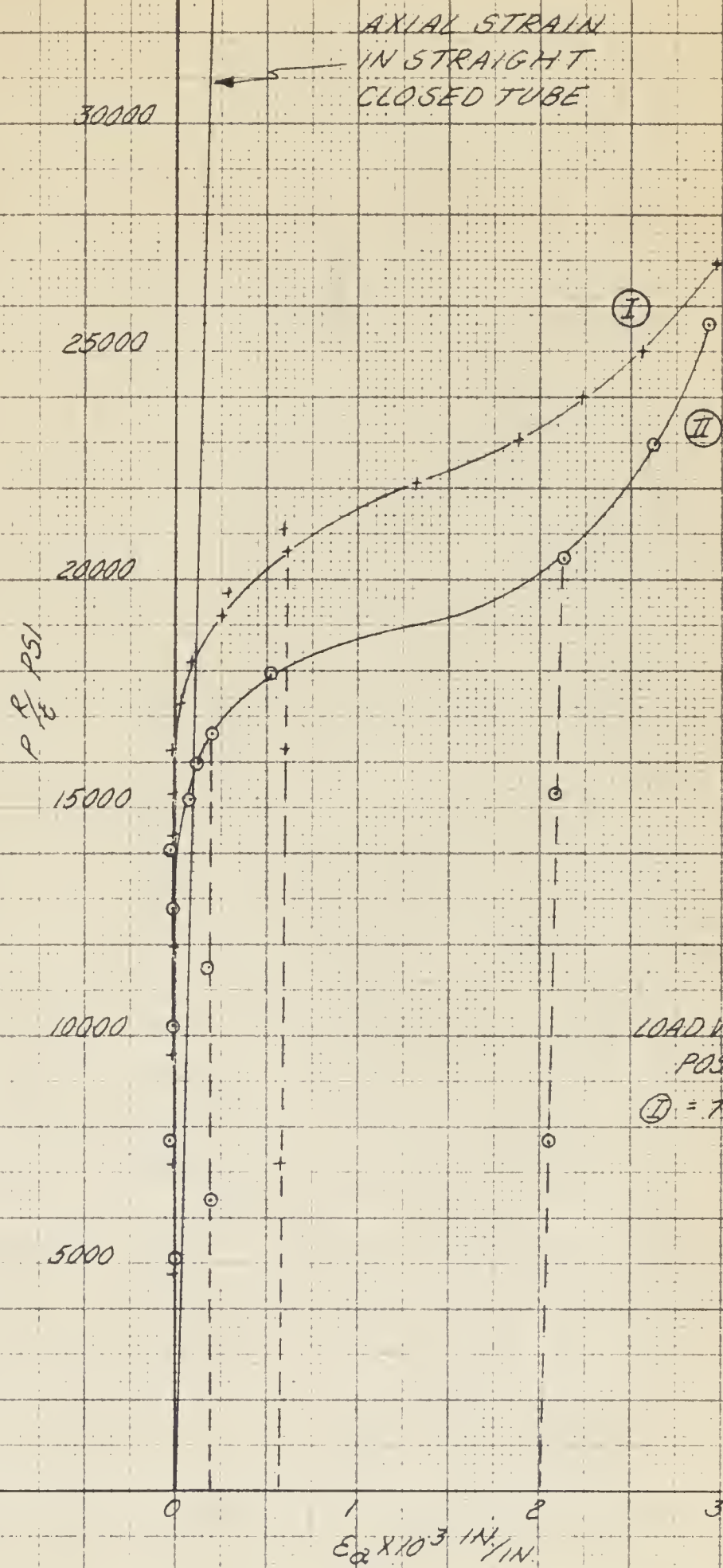
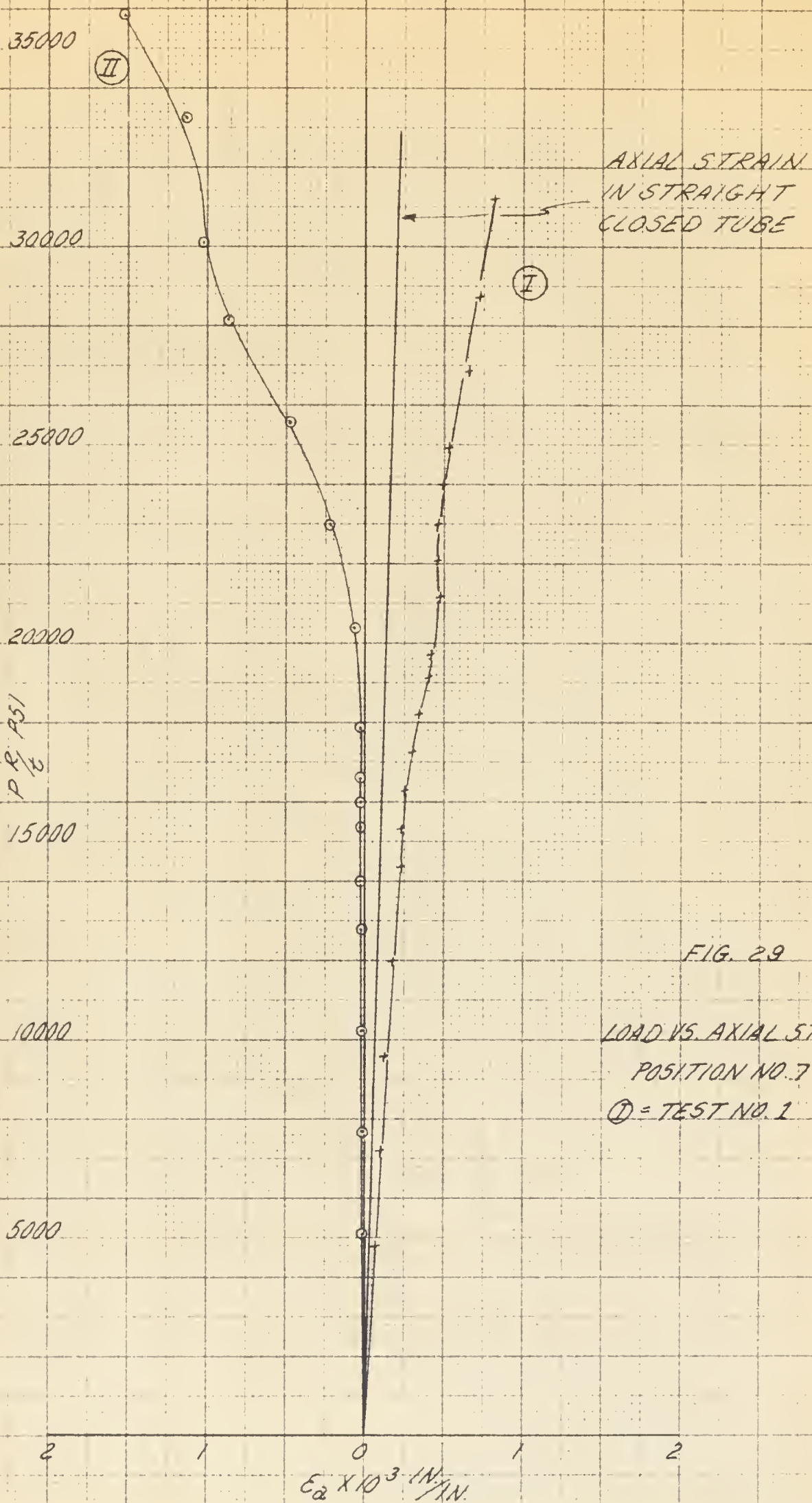


FIG. 28

LOAD VS. AXIAL STRAIN
POSITION NO. 6



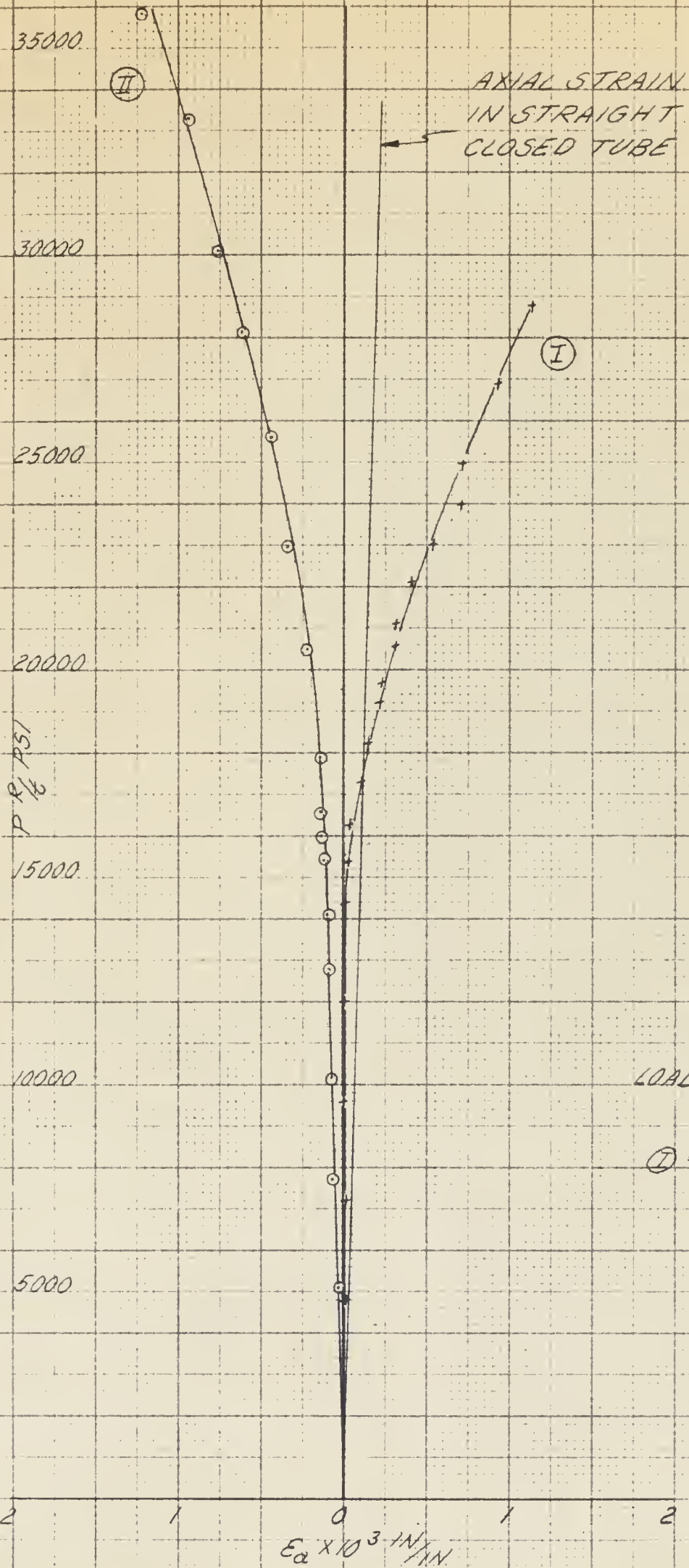


FIG. 30

LOAD VS. AXIAL STRAIN
POSITION NO. 8
① = TEST NO. 1

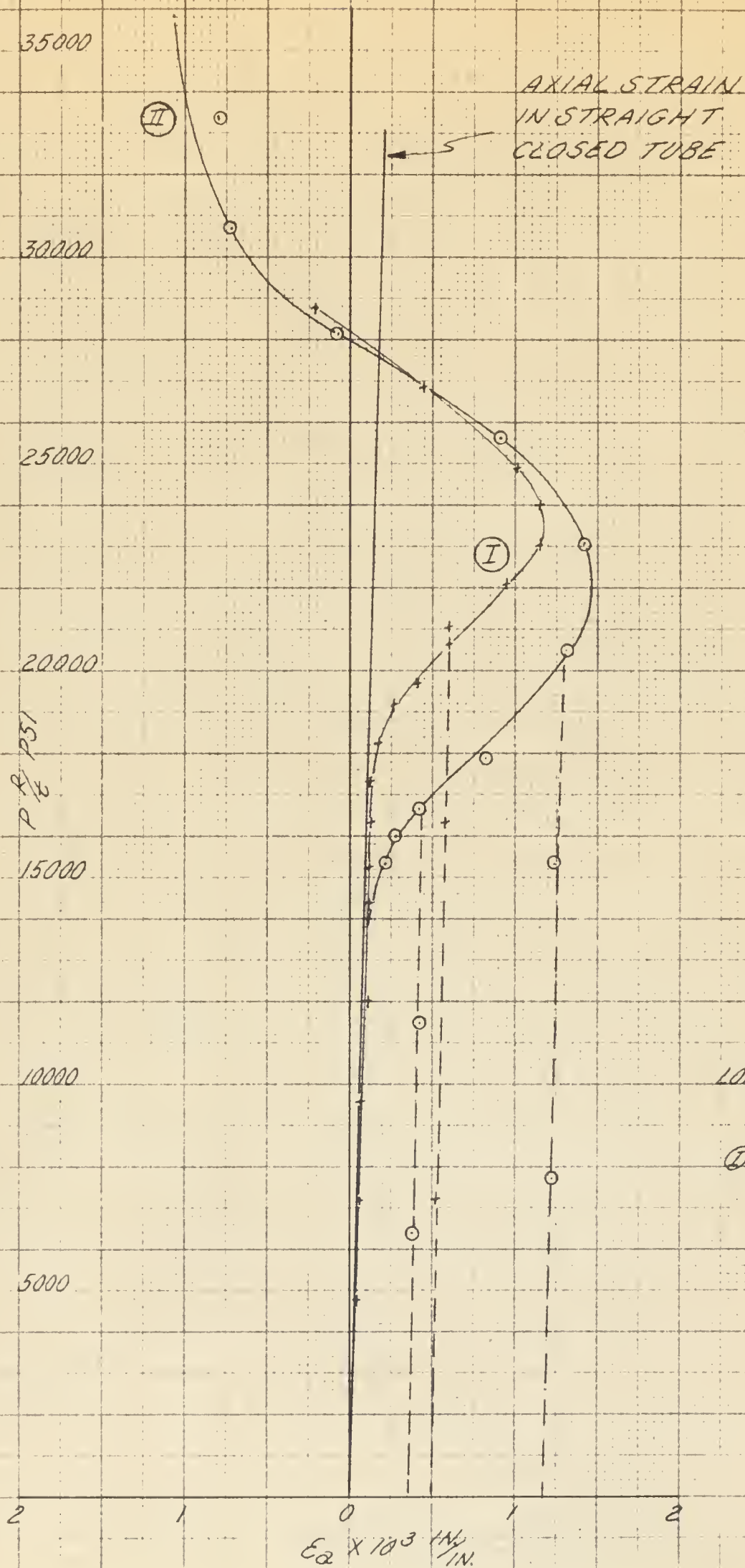


FIG. 31

LOAD VS. AXIAL STRAIN
POSITION NO. 9
① = TEST NO. 1

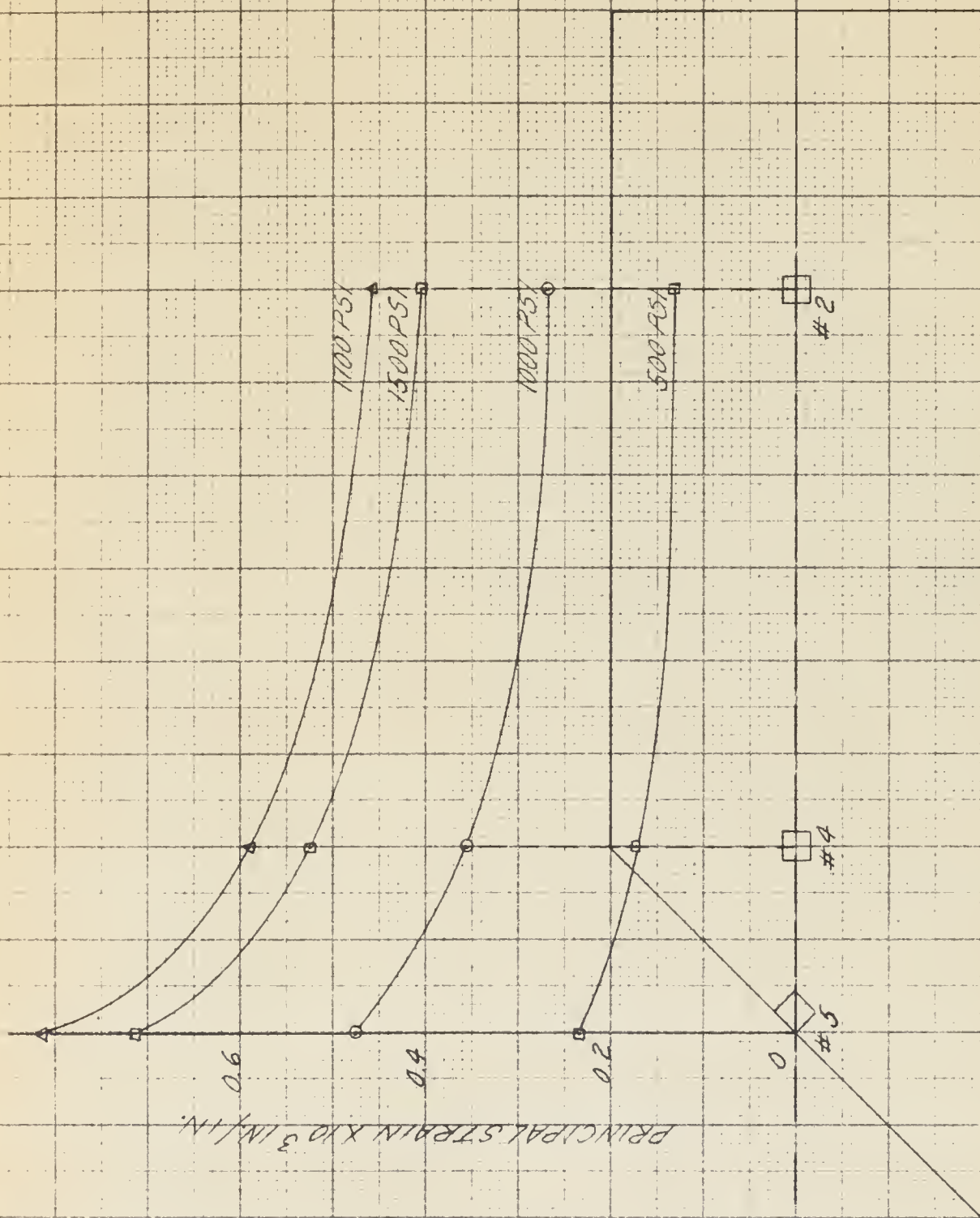


FIG 32

PRINCIPAL STRAIN VS AXIAL POSITION

TEST NO. I

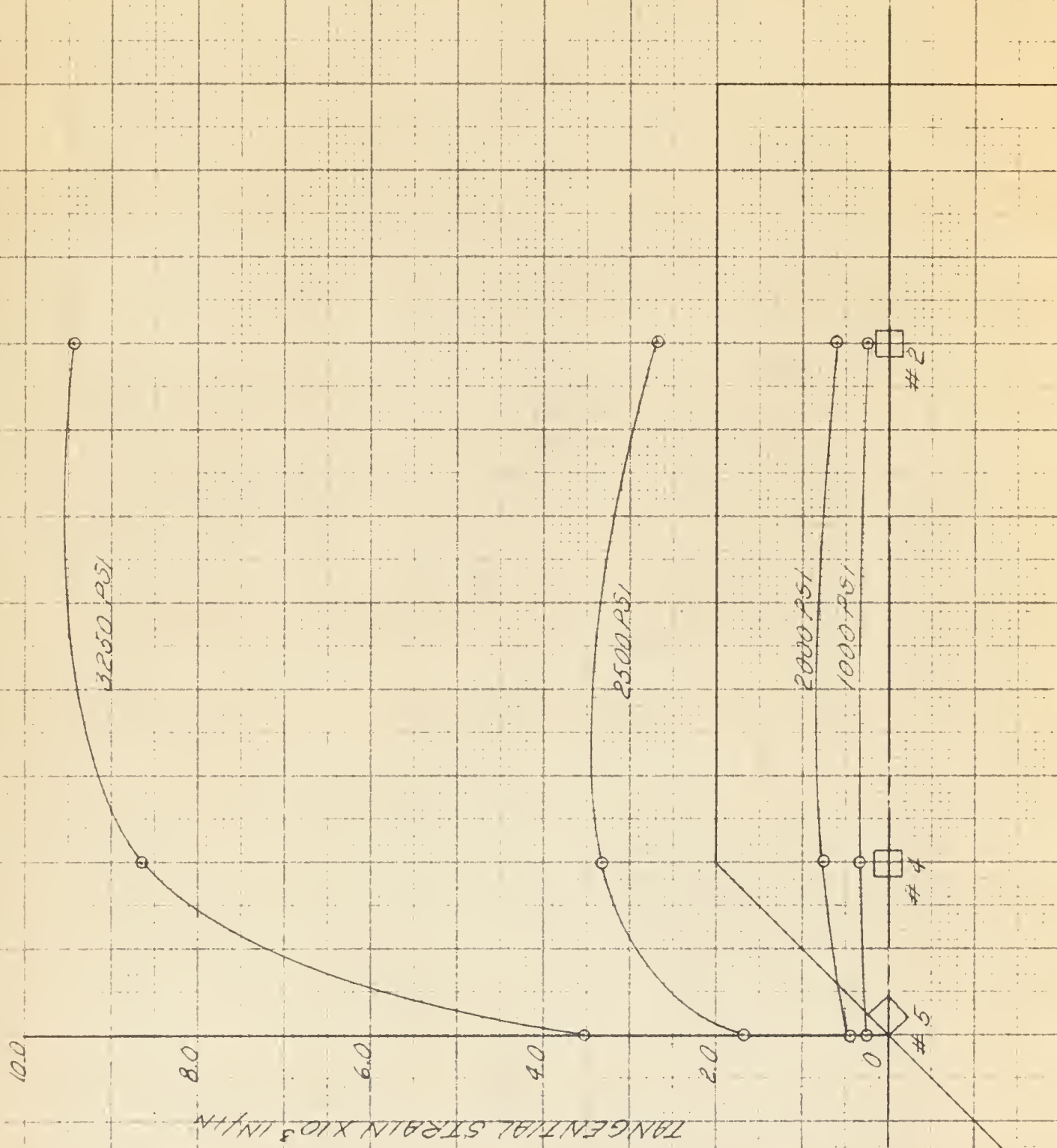


FIG. 33
TANGENTIAL STRAIN VS. AXIAL POSITION
TEST NO. 1

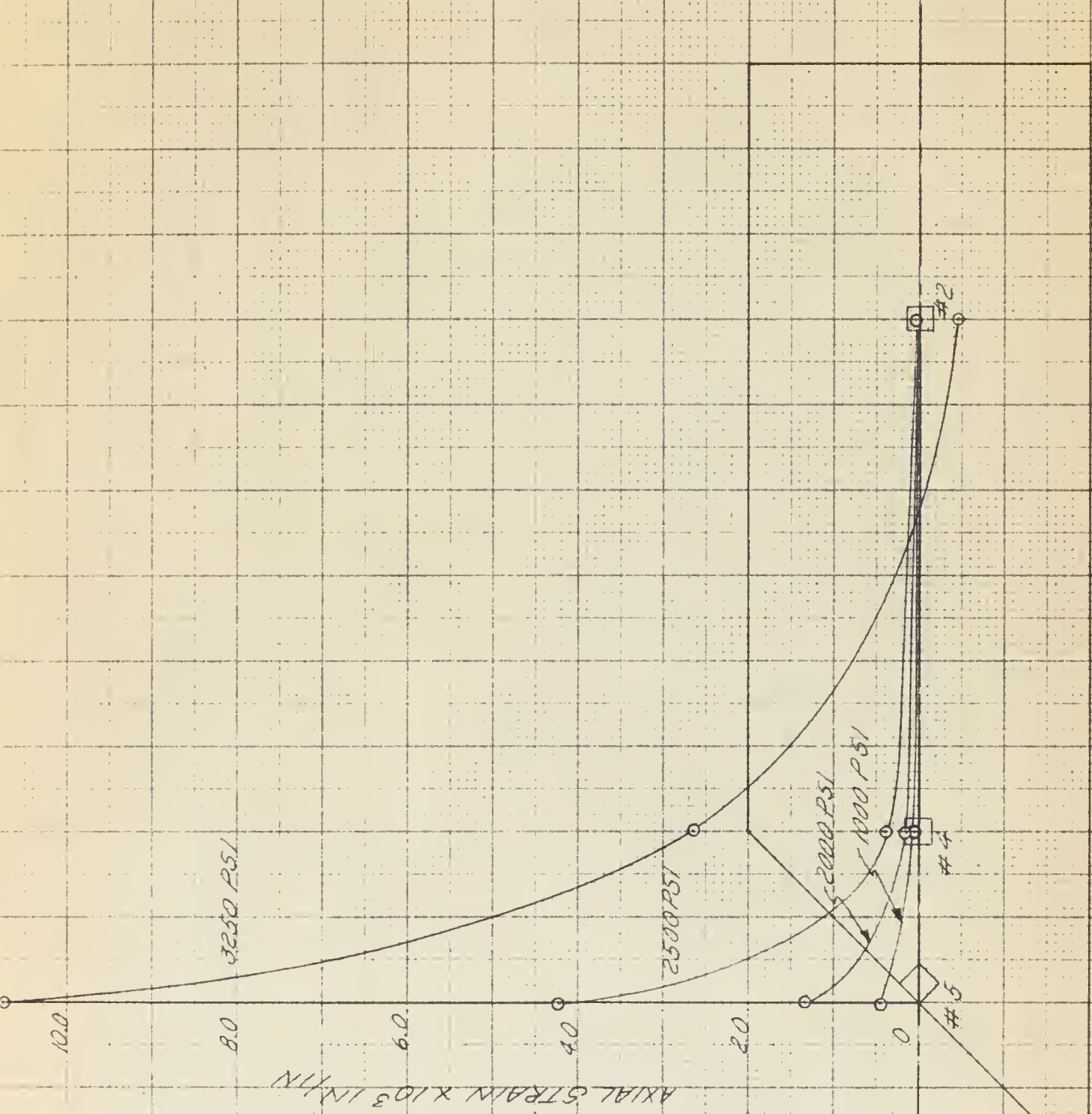


FIG. 34
AXIAL STRAIN VS. AXIAL POSITION
TEST NO. I

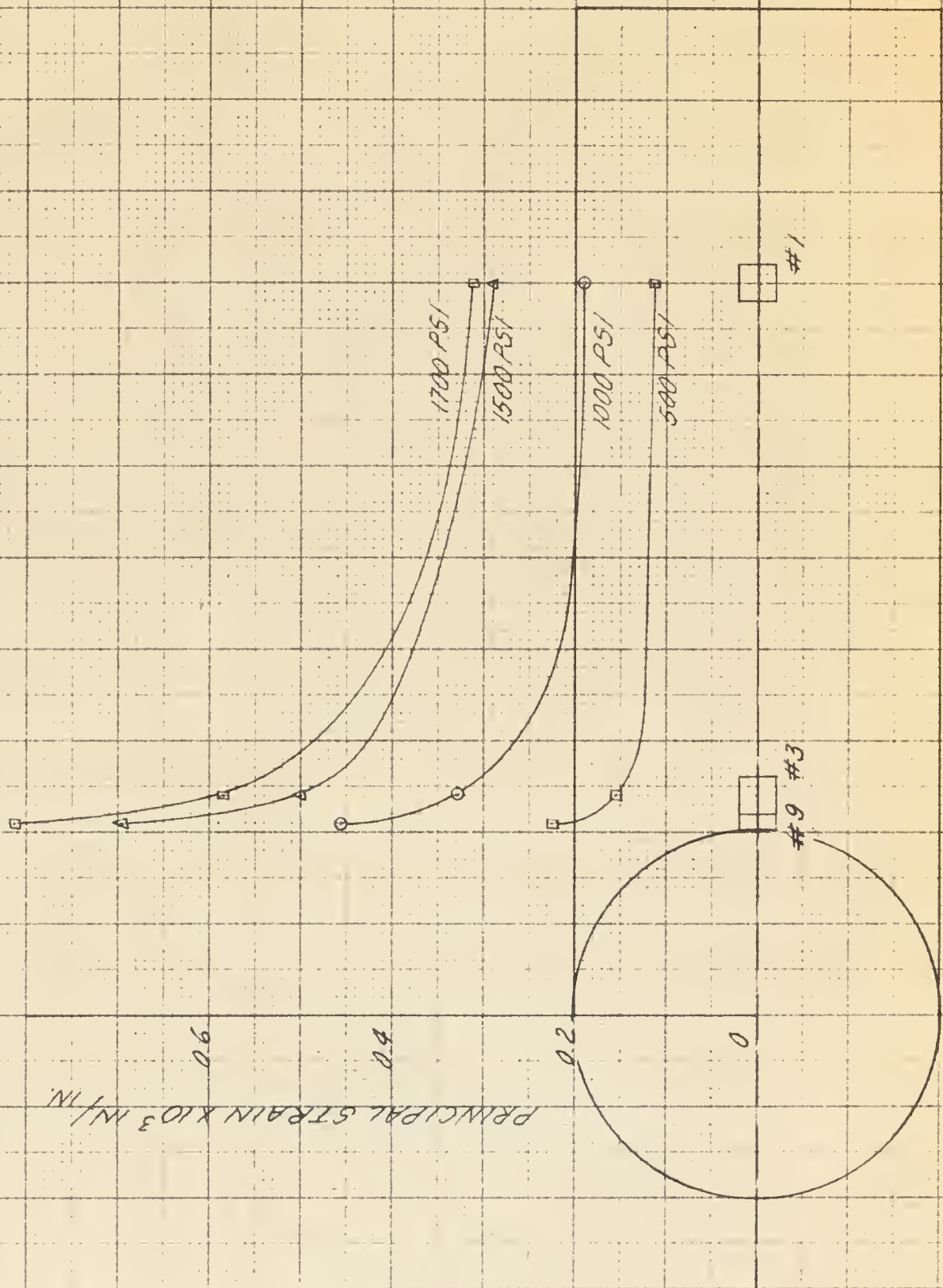


FIG. 35
PRINCIPAL STRAIN VS. AXIAL POSITION
TEST NO. 1

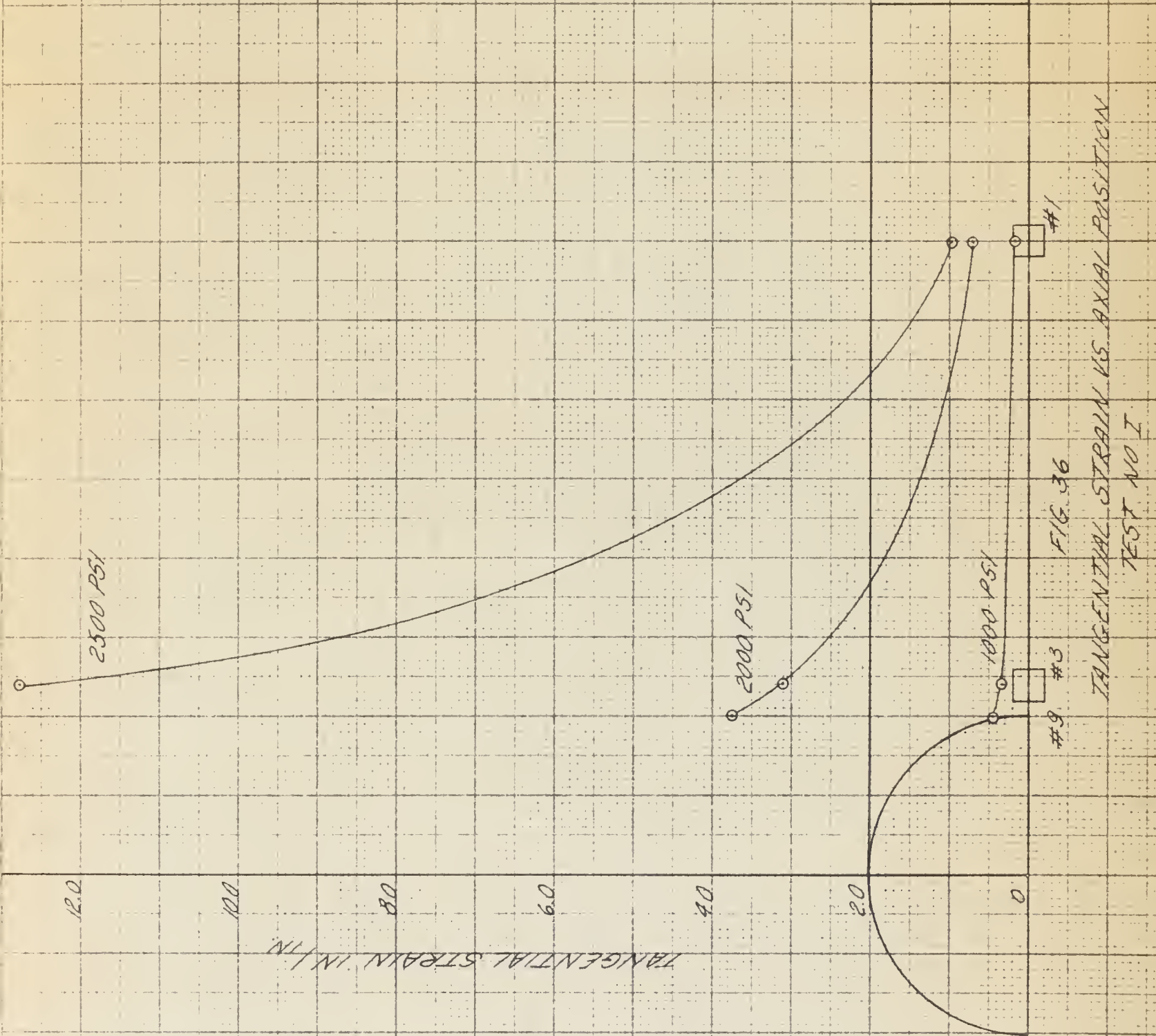


FIG. 36

TANGENTIAL STRAIN VS. AXIAL POSITION
TEST NO I

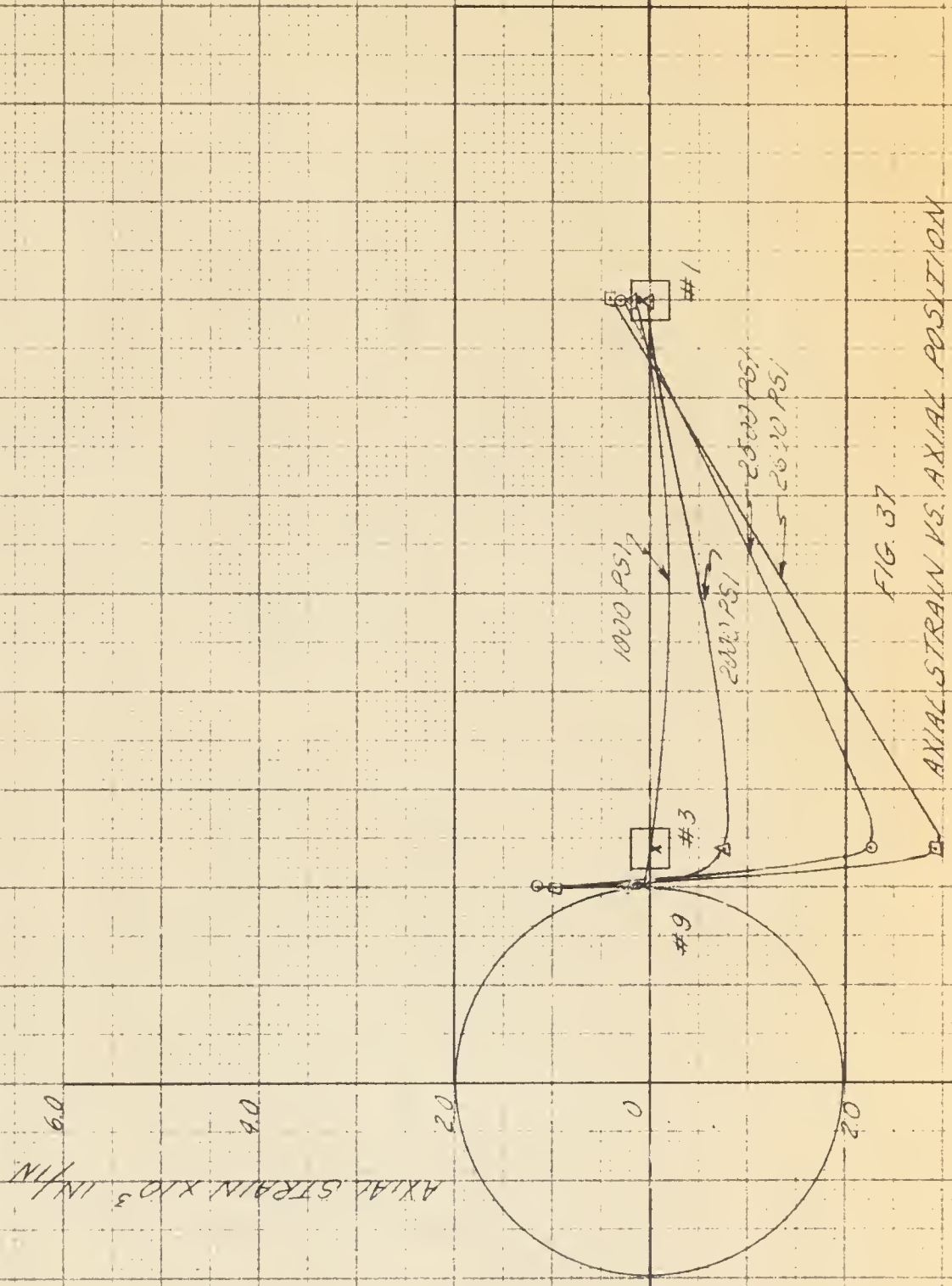


FIG. 37
AXIAL STRAIN VS. AXIAL POSITION
TEST NO. I

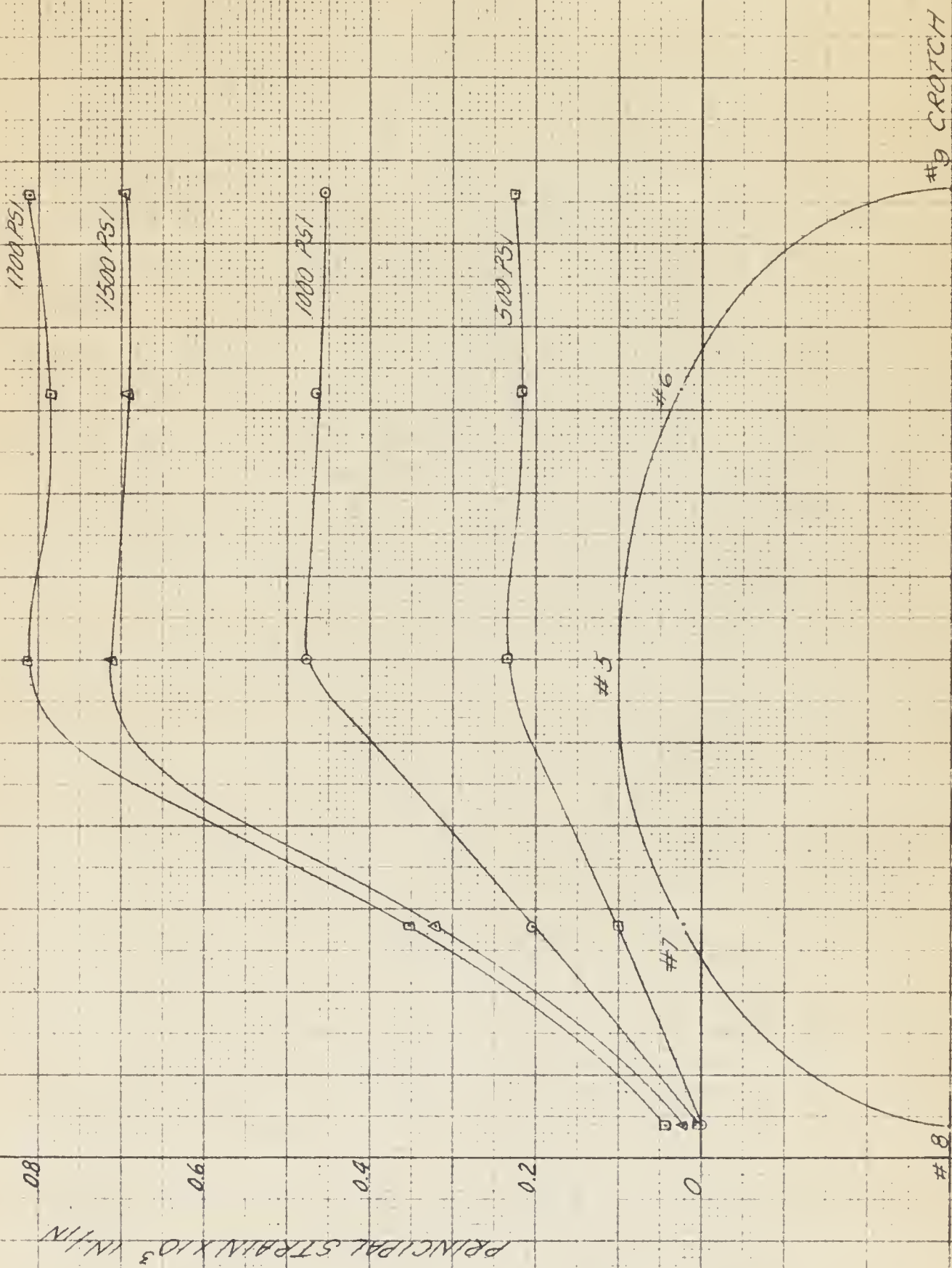


FIG. 38
PRINCIPAL STRAIN VS. POSITION ON INTERSECTION
TEST NO. I

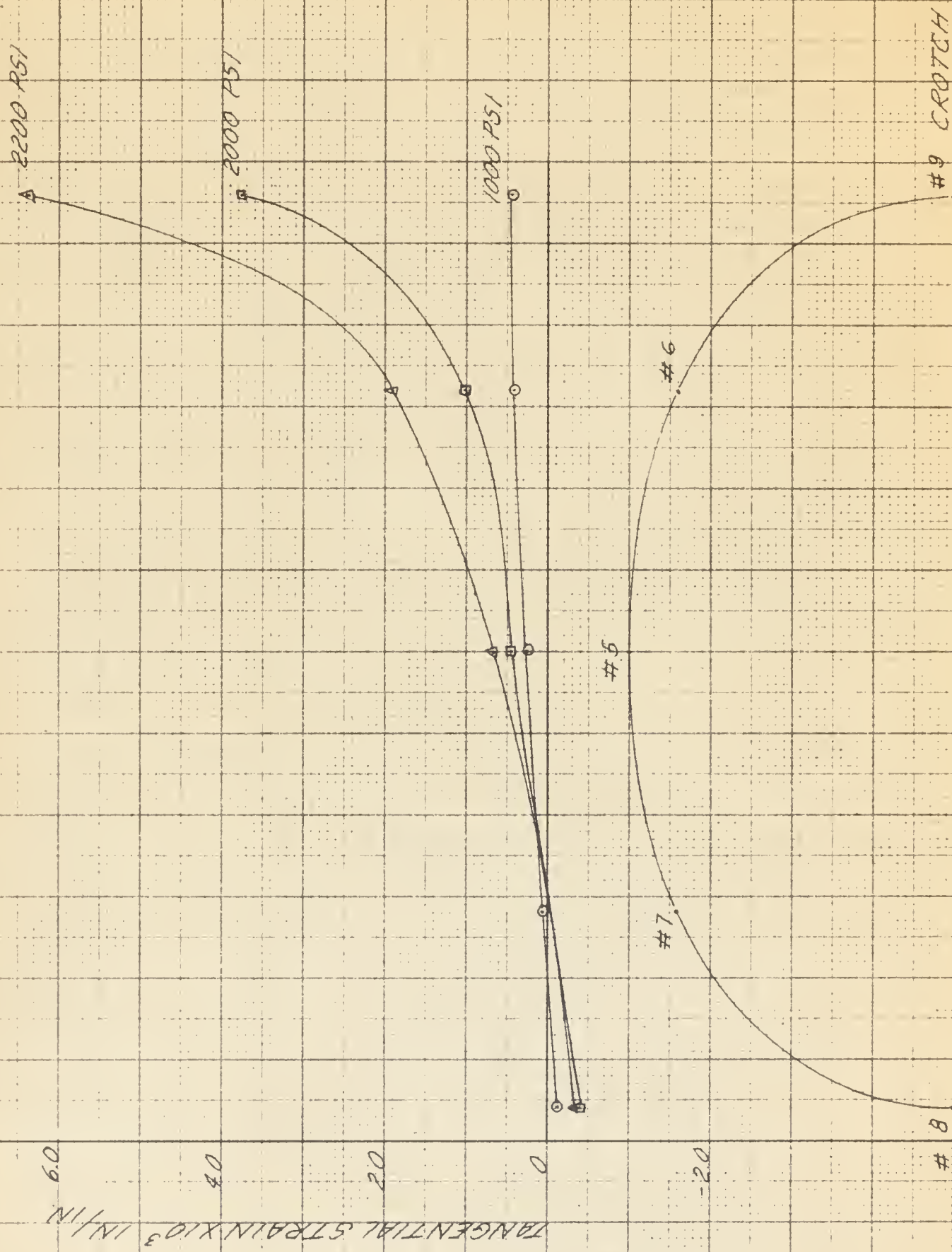


FIG 39
TANGENTIAL STRAIN VS POSITION ON INTERSECTION
TEST NO I

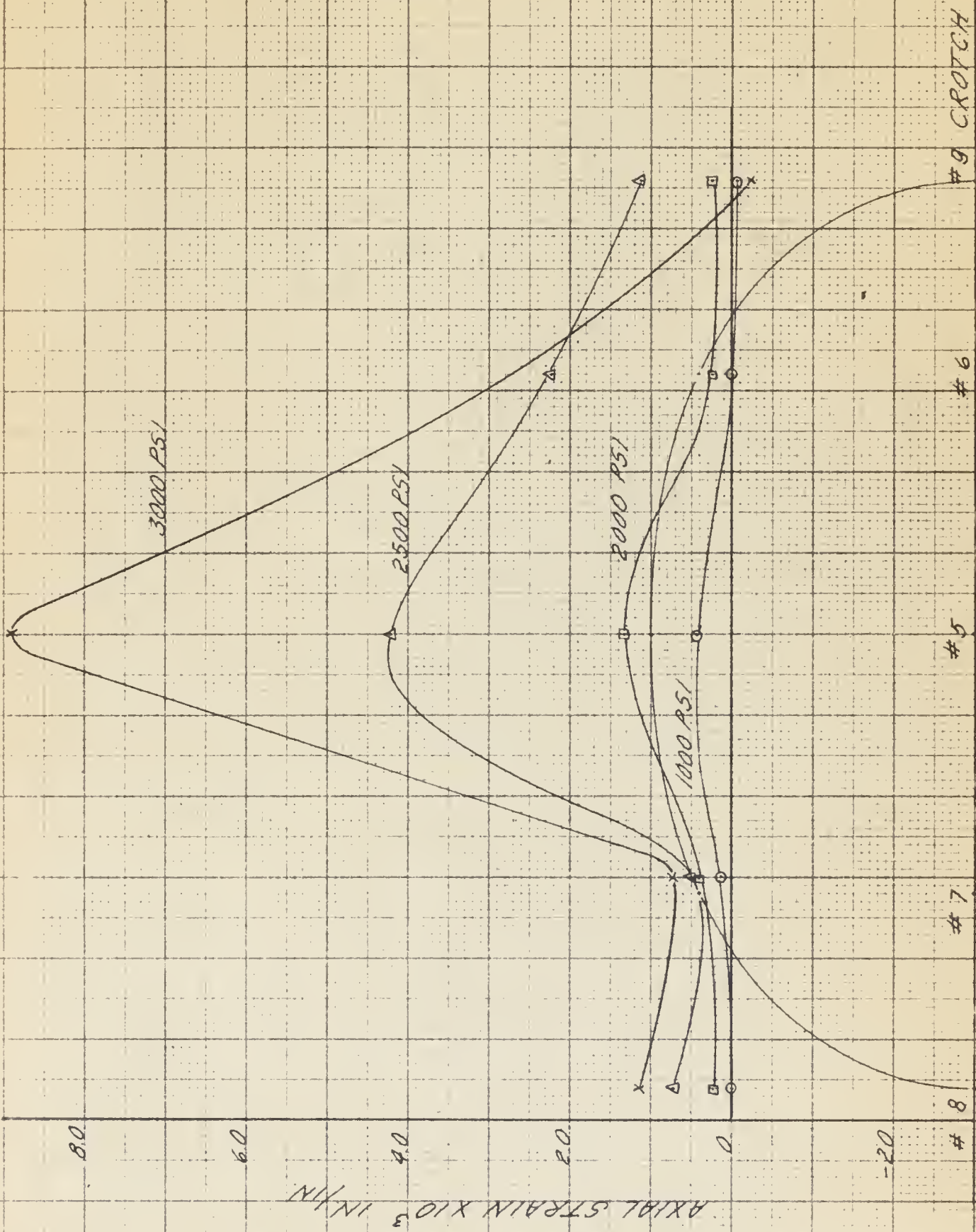
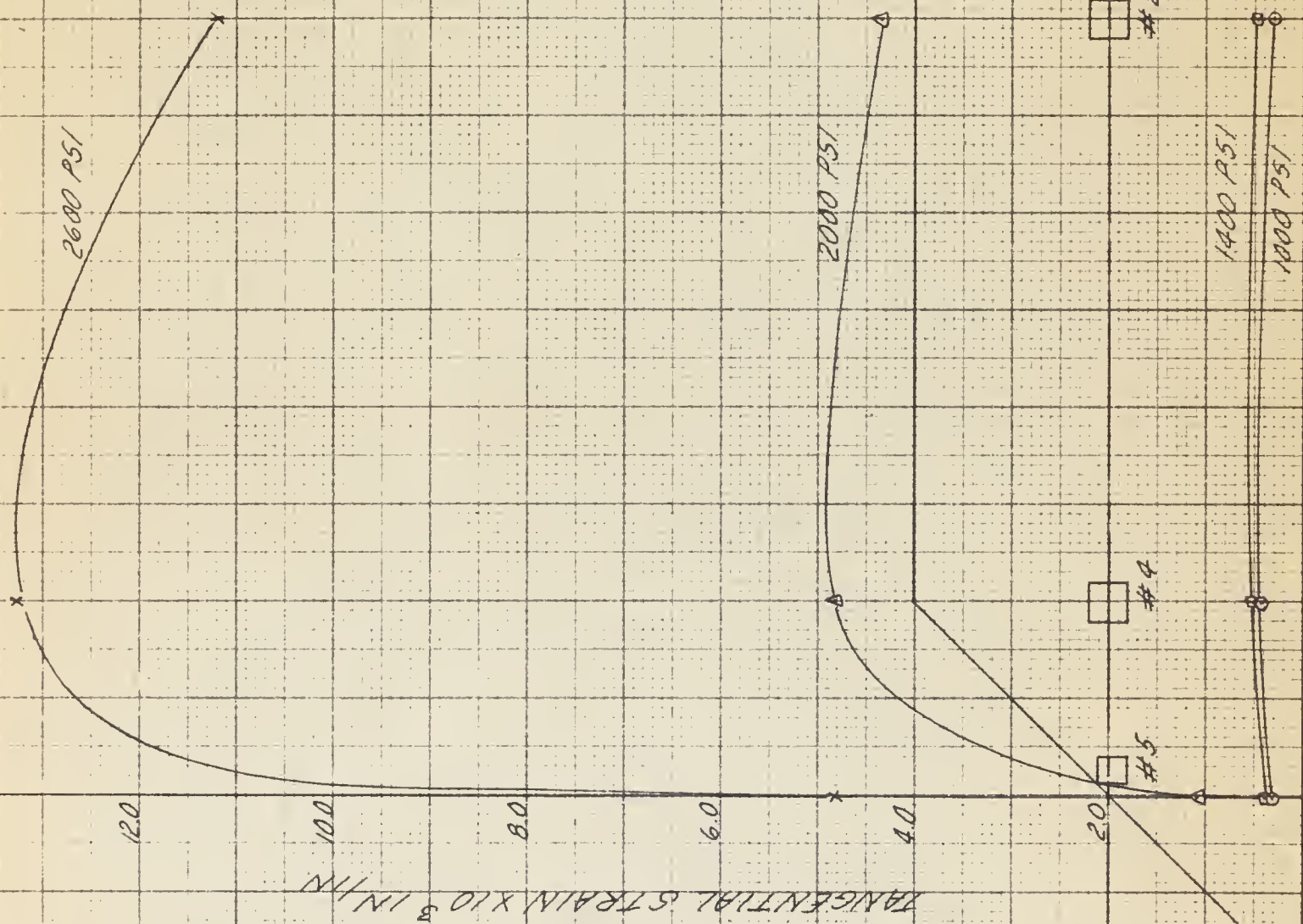


FIG. 40
AXIAL STRAIN VS POSITION OF INTERSECTION
TEST NO. 1

FIG. 42
TANGENTIAL STRAIN
VS. AXIAL POSITION
TEST NO. II



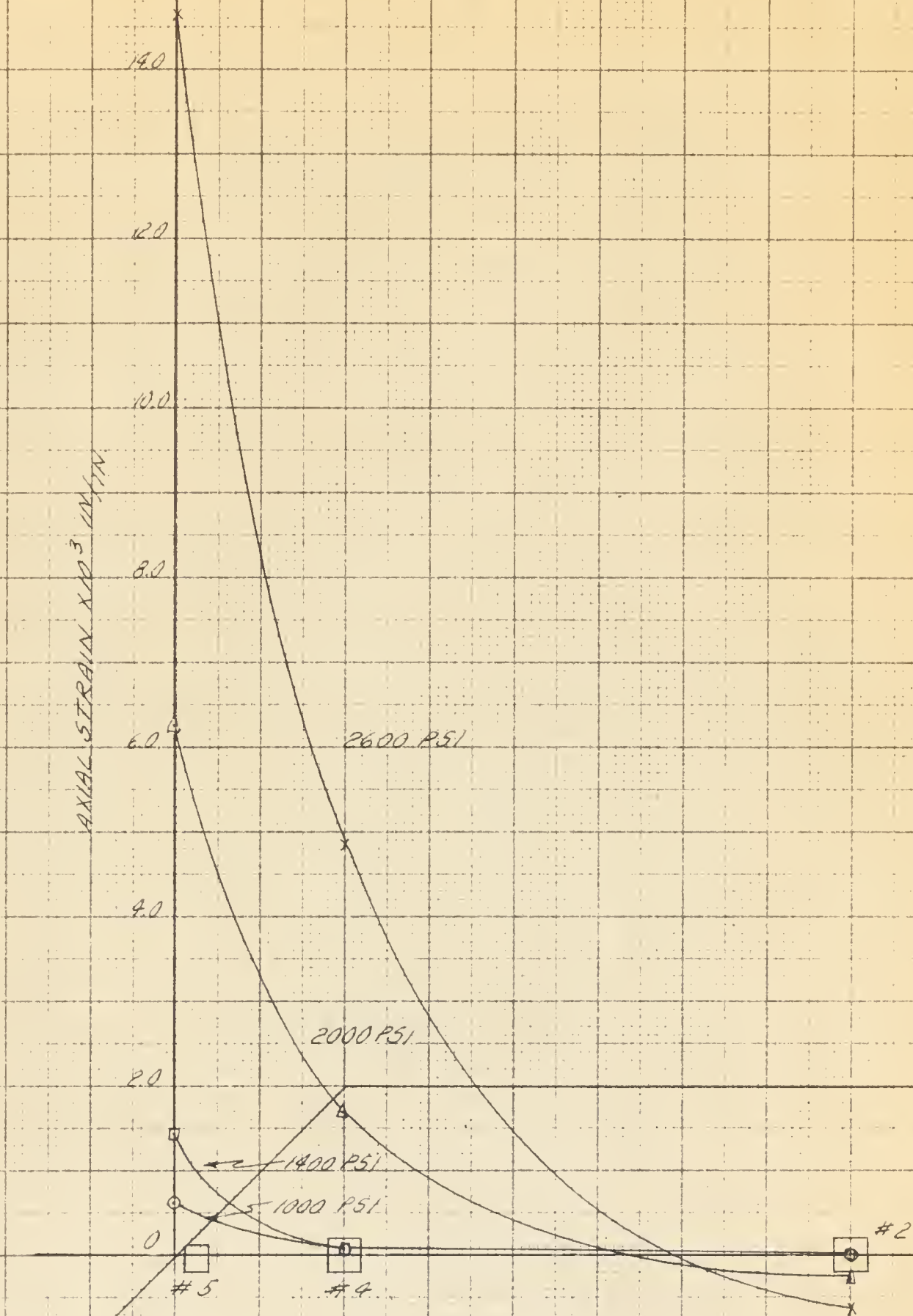


FIG. 43

AXIAL STRAIN VS. AXIAL POSITION
TEST NO. II

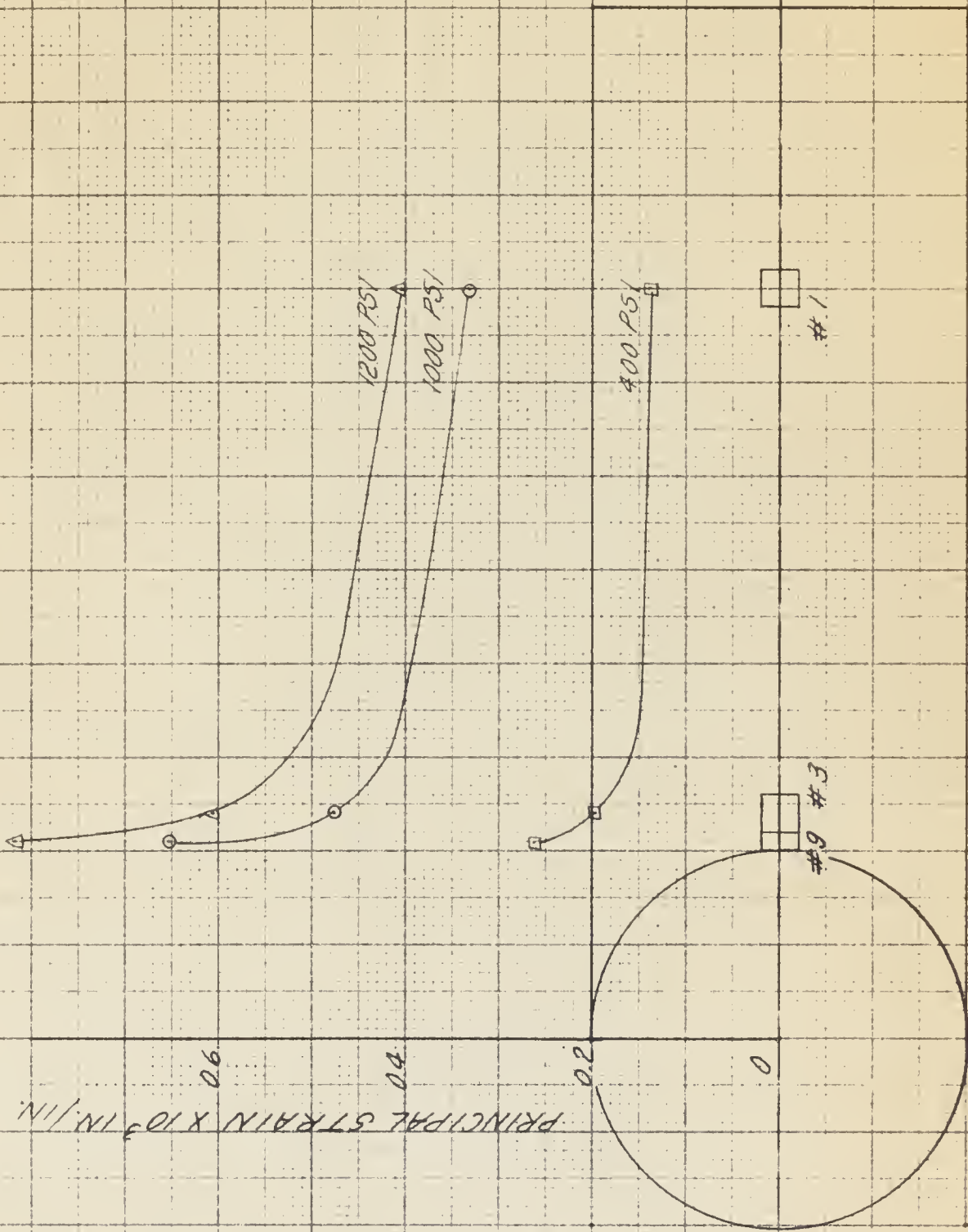


FIG. 44
PRINCIPAL STRAIN VS. AXIAL POSITION
TEST NO. II

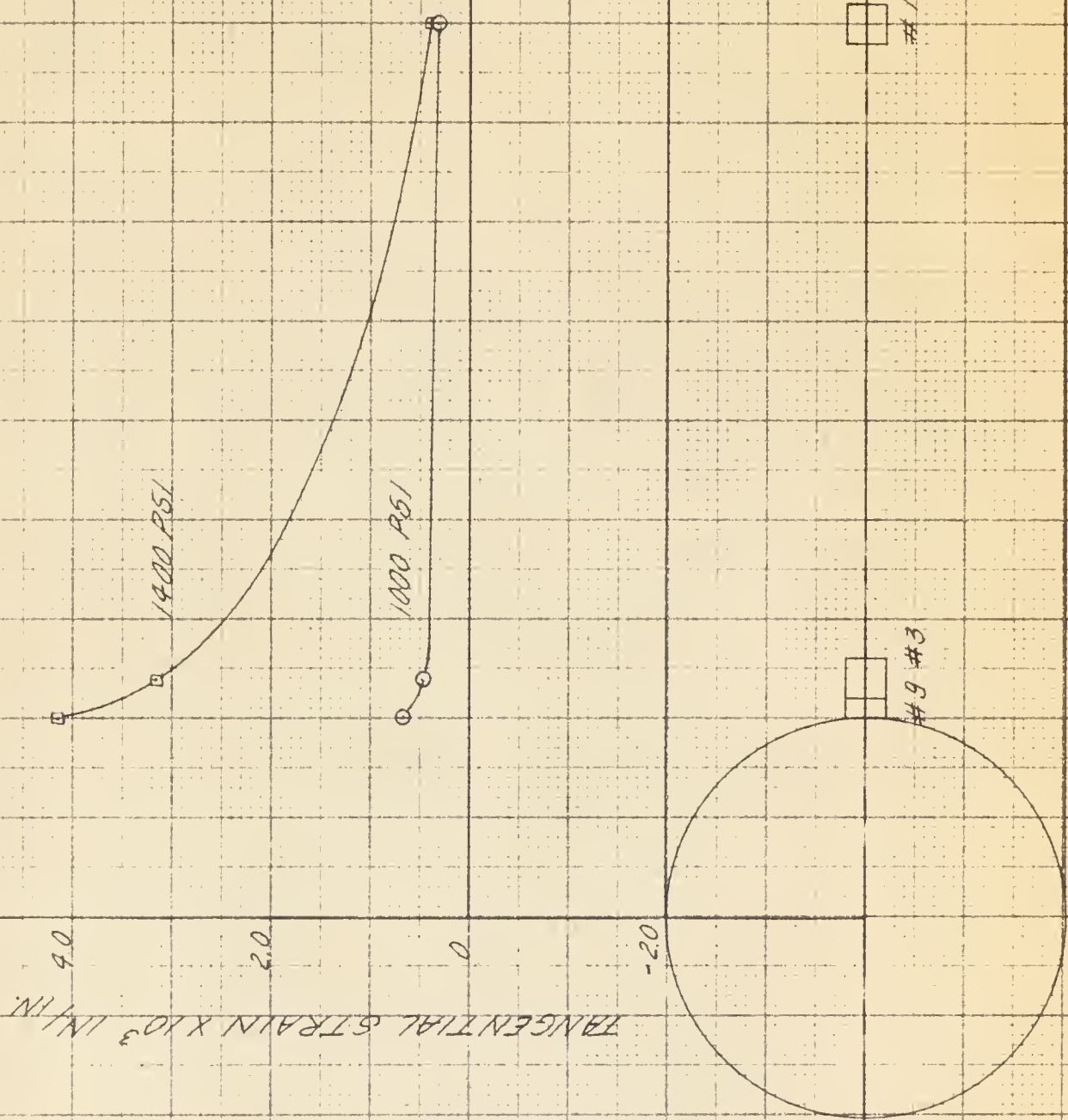


FIG. 45
TANGENTIAL STRAIN VS. AXIAL POSITION
TEST NO. II

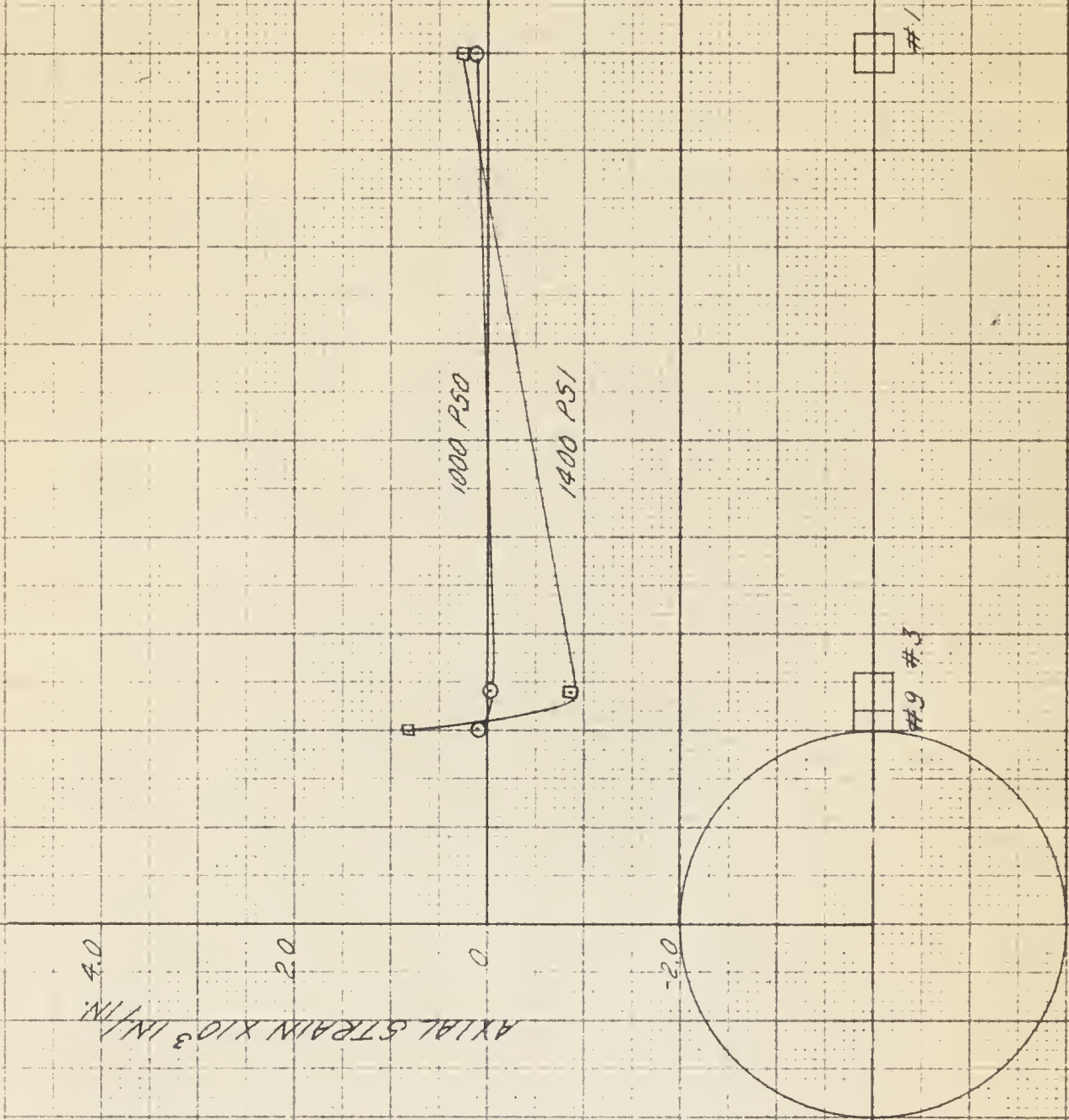


FIG. 46
AXIAL STRAIN VS. AXIAL POSITION
TEST NO. II

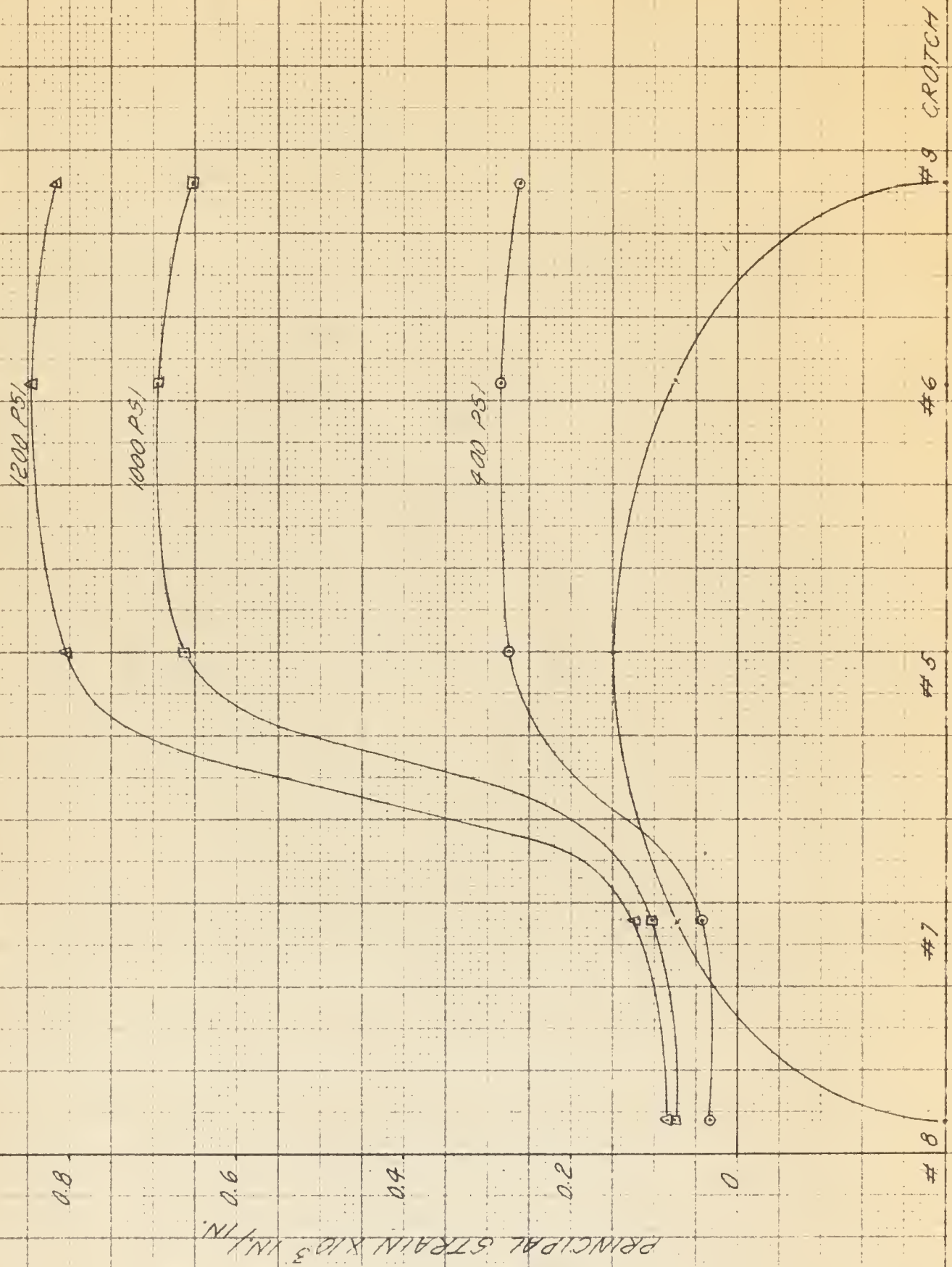


FIG. 47
PRINCIPAL STRAIN VS. POSITION ON INTERSECTION
TEST NO. II

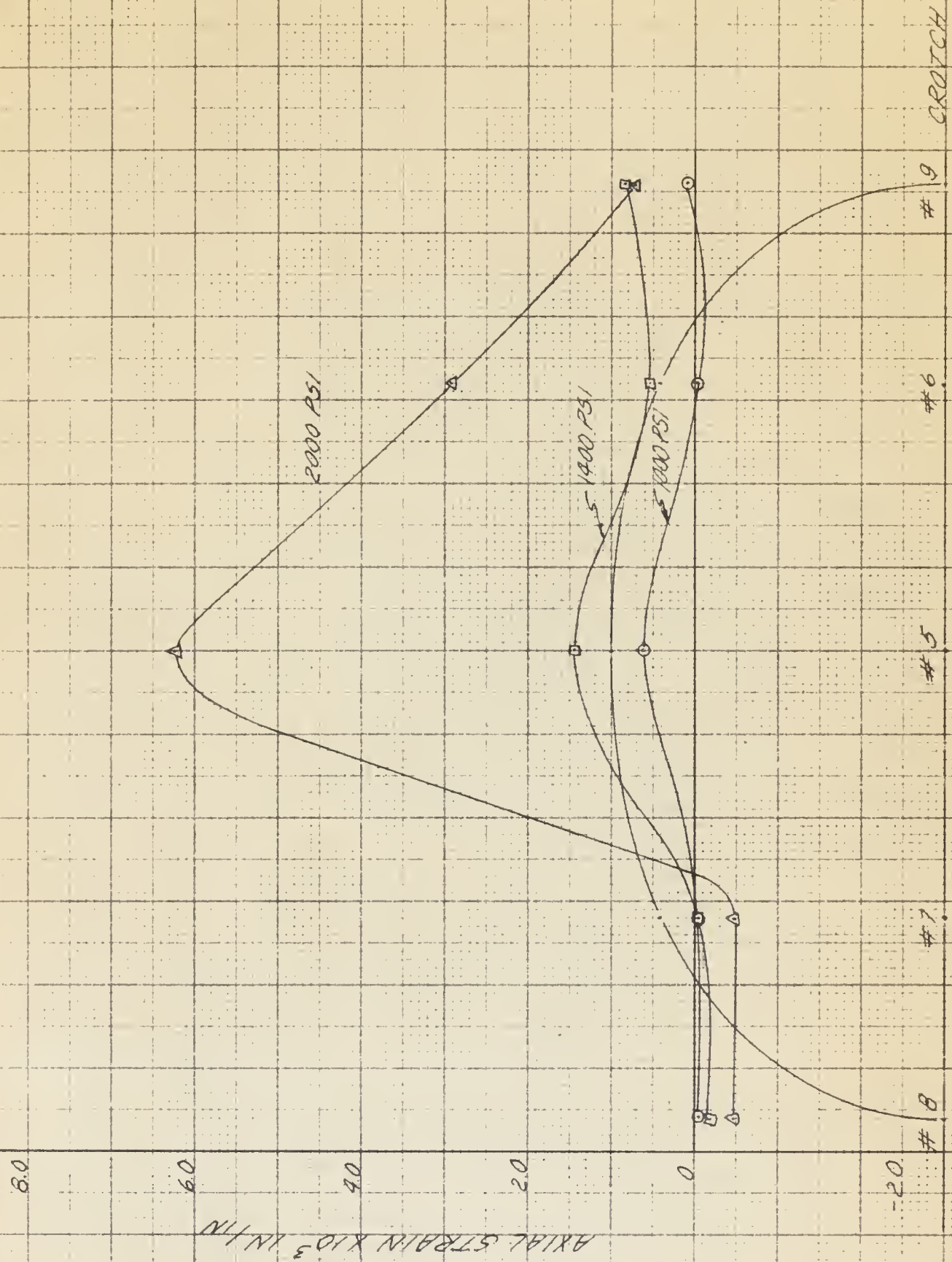


FIG. 48
AXIAL STRAIN VS. POSITION ON INTERSECTION
TEST NO. 22

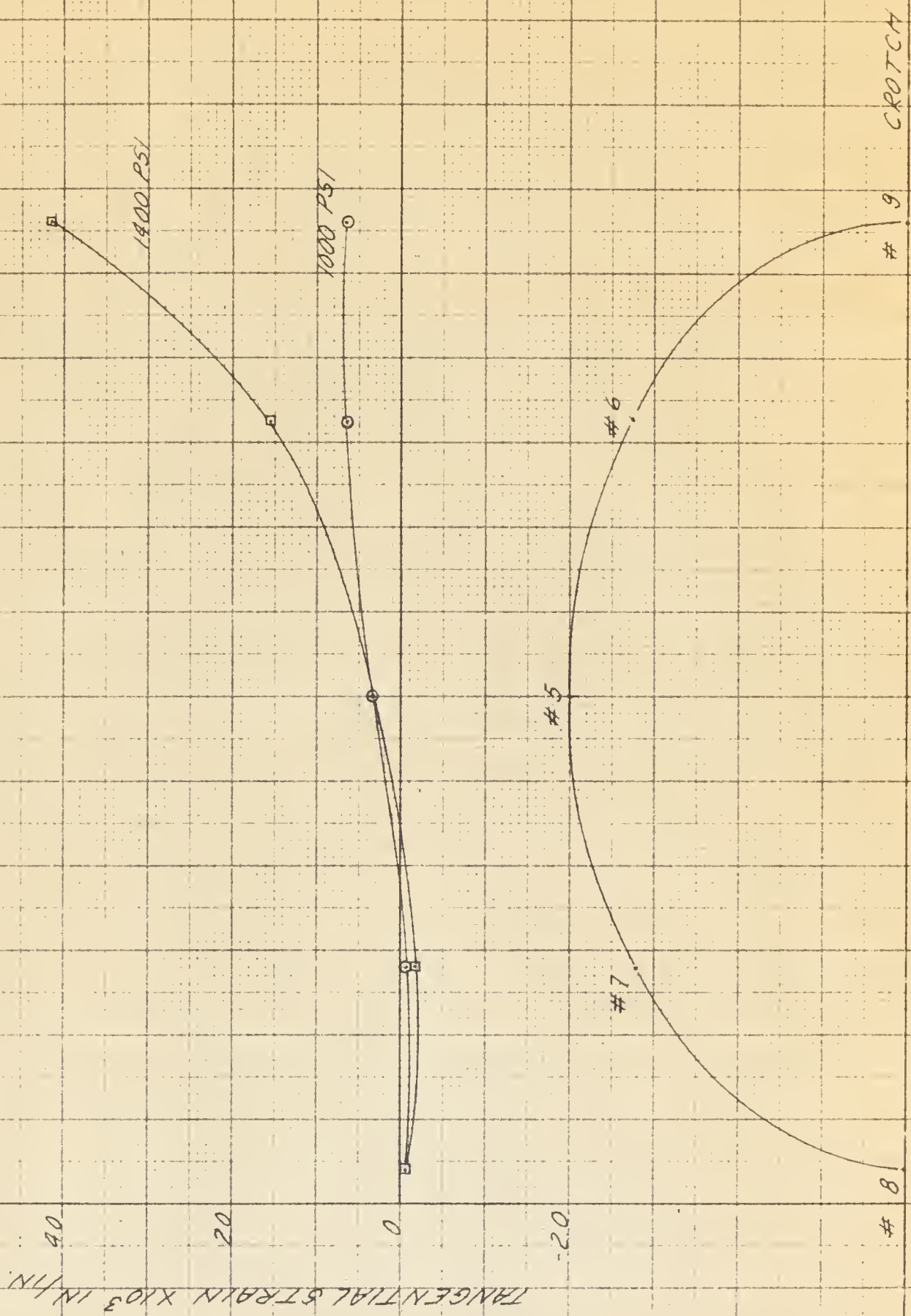
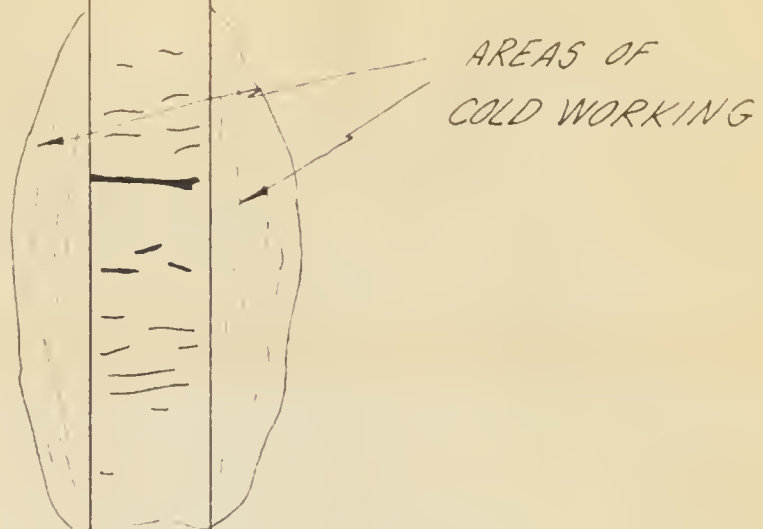
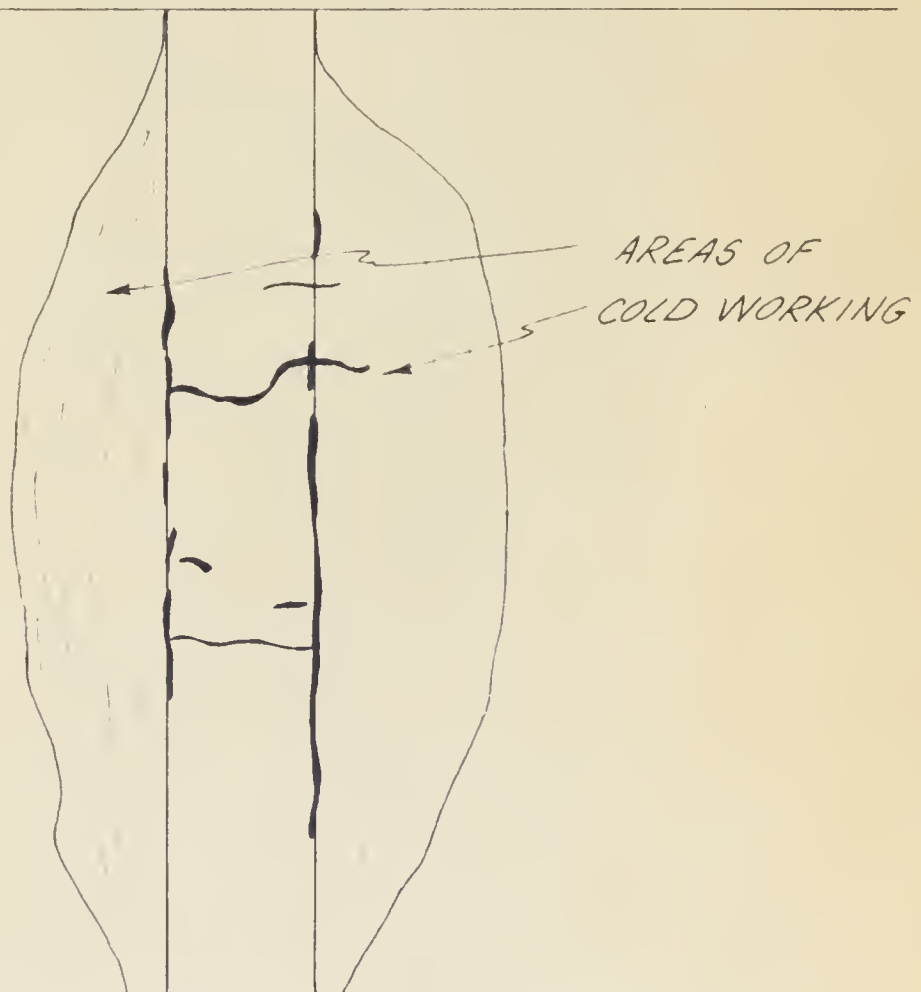


FIG. 49
TANGENTIAL STRAIN VS. POSITION ON INTERSECTION
TEST NO. II



I



II

FIG. 50
SKETCHES OF BREAKS IN WELDS

[illegible]

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T23 Teig
Stress distribution
in two intersecting
cylinders under
pressure.

Thesis 11370
T23 Teig
Stress distribution
in two intersecting
cylinders under
pressure.

thesT23

Stress distribution in two intersecting



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